

Generating Tests by Example

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Unit tests are repetitive

```
Assert.assertTrue(Precision.equals(1.0, nUp1, 1));
Assert.assertTrue(Precision.equals(nUp1, nnUp1, 1));
Assert.assertFalse(Precision.equals(1.0, nnUp1, 1));
Assert.assertTrue(Precision.equals(0.0, FastMath.ulp(0.0), 1));
Assert.assertTrue(Precision.equals(0.0, -FastMath.ulp(0.0), 1));
Assert.assertTrue(Precision.equals(153.0, 153.0, 1));
Assert.assertTrue(Precision.equals(153.0, 153.000000000000003, 1));
Assert.assertFalse(Precision.equals(153.0, 153.000000000000006, 1));
Assert.assertTrue(Precision.equals(153.0, 152.99999999999997, 1));
Assert.assertFalse(Precision.equals(153, 152.99999999999994, 1));
Assert.assertTrue(Precision.equals(-128.0, -127.99999999999999, 1));
Assert.assertFalse(Precision.equals(-128.0, -127.99999999999997, 1));
Assert.assertTrue(Precision.equals(-128.0, -128.000000000000003, 1));
Assert.assertFalse(Precision.equals(-128.0, -128.000000000000006, 1));
Assert.assertTrue(Precision.equals(Double.POSITIVE_INFINITY,
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Tests are examples!

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```

Tests are examples!



**We can synthesize
more tests**

Unit Tests

- A (conventional) unit test
 - Empty precondition
 - Tests a postcondition (assertion, oracle)

```
@Test public void example1() {  
    String a = "abc";  
    String b = "bcd";  
    String sum = a + b;  
    assertEquals(sum.length(), 6);  
}
```

Unit Tests

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@Test public void example1() {  
    String a = "abc";  
    String b = "bcd";  
    String sum = a + b;  
    assertEquals(sum.length(), 6);  
}
```

- A parameterized unit test
 - Precondition on the parameters


```
@Test public void example2(String a, String b) {  
    String sum = a + b;  
    assertEquals(sum.length(), 6);  
}
```

Property-based Tests

```
object UtilsPBT extends Properties("Str") {  
  property("concat") = forAll {  
    (a: String, b: String) =>  
      a.length + b.length == 6 ==>  
        val res = a + b  
        res.length == 6  
  }  
}
```

Property-based Tests

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precondition

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```

assertion



Property-based Tests

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        val res = a + b  
        res.length == 6  
  }  
}
```

Successfully executed for 1000 values

Individual tests are important

- Some tests exist for historical reasons

```
@Test public void testMath1127() {  
    Assert.assertFalse(Precision.equals(2.0, -2.0, 1));  
    Assert.assertTrue(Precision.equals(0.0, -0.0, 0));  
    Assert.assertFalse(Precision.equals(2.0F, -2.0F, 1));  
    Assert.assertTrue(Precision.equals(0.0F, -0.0F, 0));  
}
```

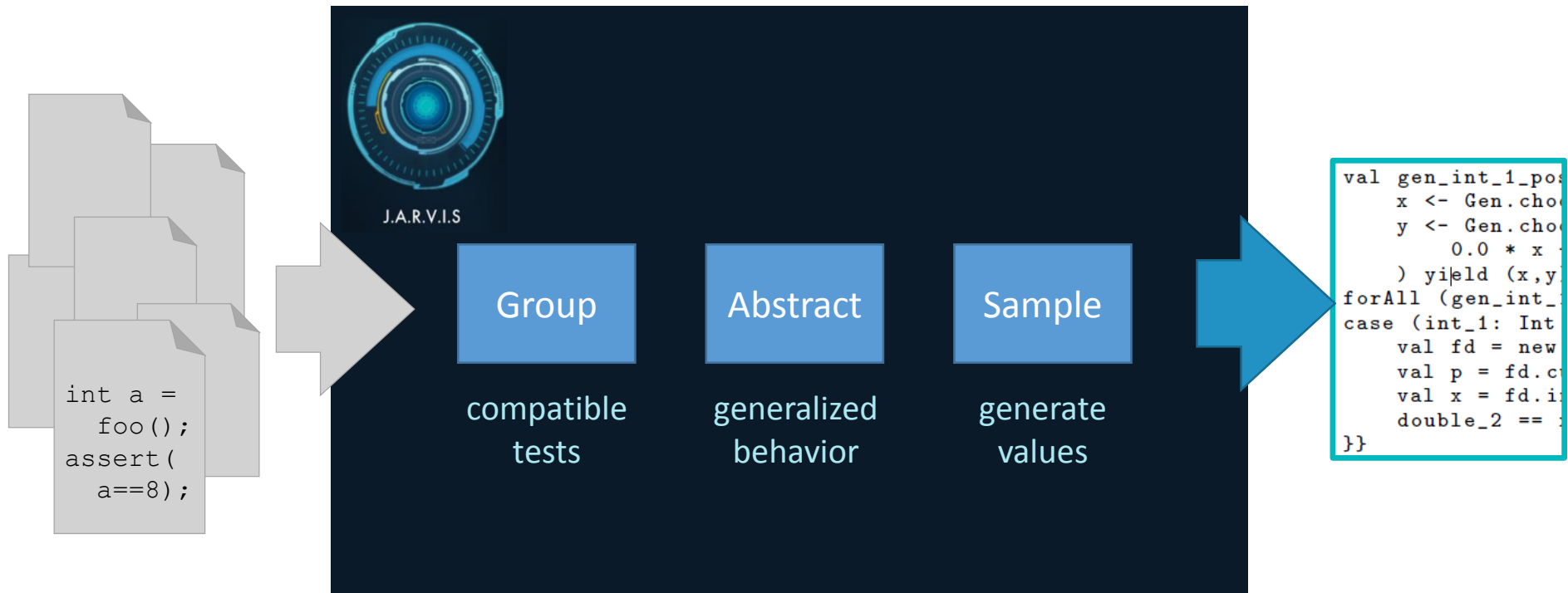
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}
```

- Other tests test some sort of nuance
- We want to keep those in place
- But we also want to generate more tests like them.

We should learn new tests!



Example

```
//test 1
```

```
Interval interval = new Interval(2.3, 5.7);  
assertEquals(3.4, interval.getSize(), 1.0e-10);  
assertEquals(4.0, interval.getBarycenter(), 1.0e-10);  
assertEquals(Region.Location.BOUNDARY,  
    interval.checkPoint(2.3, 1.0e-10));
```

```
//test 2
```

```
Interval interval2 = new Interval(1.0, 1.0);  
assertEquals(0.0, interval2.getSize(), Precision.SAFE_MIN);  
assertEquals(1.0, interval2.getBarycenter(),  
    Precision.EPSILON);
```

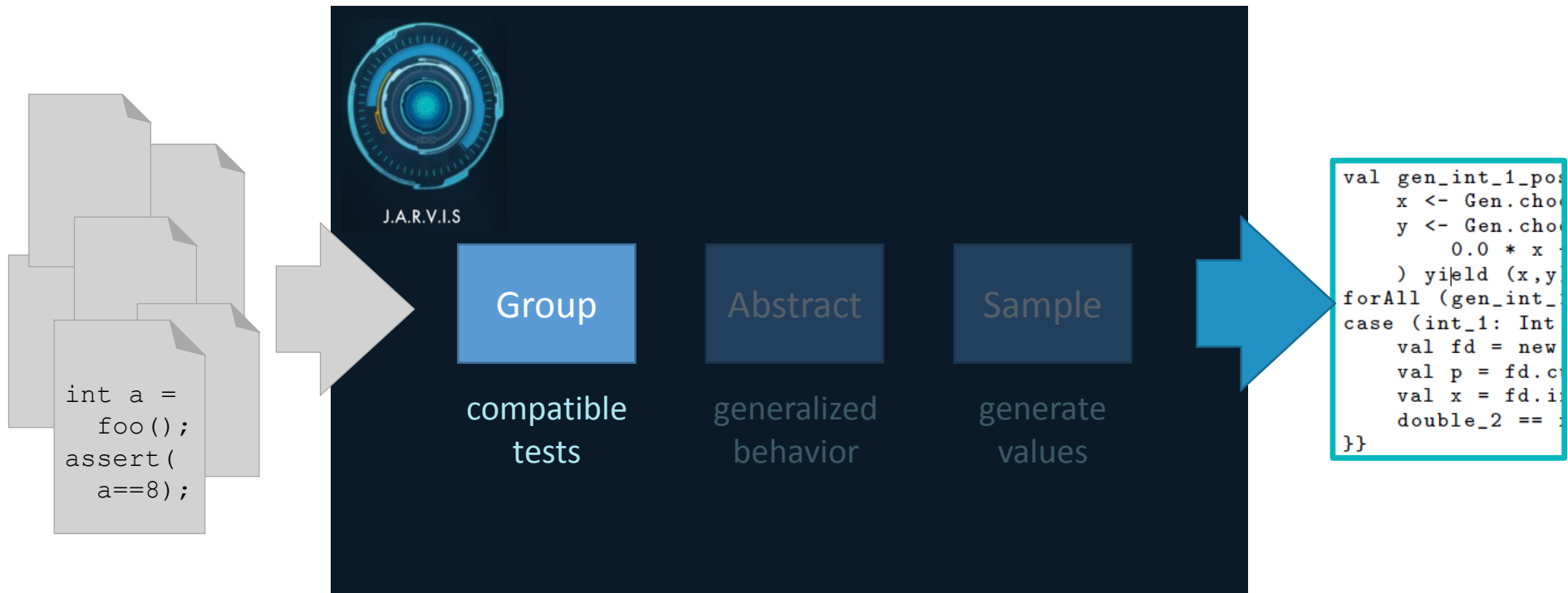
```
//test 3
```

```
Interval interval3 = new Interval(2, 2);  
assertNotEquals(2.1, interval3.getBarycenter(), 1.0e-10);
```

```
//test 4
```

```
Interval interval4 = new Interval(2,3);  
assertEquals(2.5, interval4.getBarycenter(), 1.0e-10);
```

Step 1



Grouping Examples

- Get individual tests that test the same thing
- The constants in each test trace are extracted
- *parameterized test* and a *parameter mapping*

```
//test 1
```

```
Interval interval = new Interval(2.3, 5.7);  
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assertEquals(3.4, interval.getSize());  
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```

$pt_1(x, y, z)$

```
Interval interval = new Interval(x, y);  
assert(z == interval.getBarycenter());  
    type(x) = type(y) = type(z) = double
```

$f_1 = \{x \mapsto 2.3, y \mapsto 5.7, z \mapsto 4.0, res \mapsto +\}$

Grouping Examples

- A more complex example:

```
//test 3
```

```
Interval interval3 = new Interval(2, 2);  
assertNotEquals(2.1, interval3.getBarycenter());
```

$pt_3(x, y)$

```
Interval interval = new Interval(x, x);  
assert(y == interval.getBarycenter());  
    type(x) = int,    type(y) = double
```

$f_3 = \{x \mapsto 2, y \mapsto 2.1, res \mapsto -\}$

Grouping Examples

- A more complex example:

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//test 3
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Interval interval3 = new Interval(2, 2);  
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or x, z
where $x=z$

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Grouping Examples

- A more complex example:

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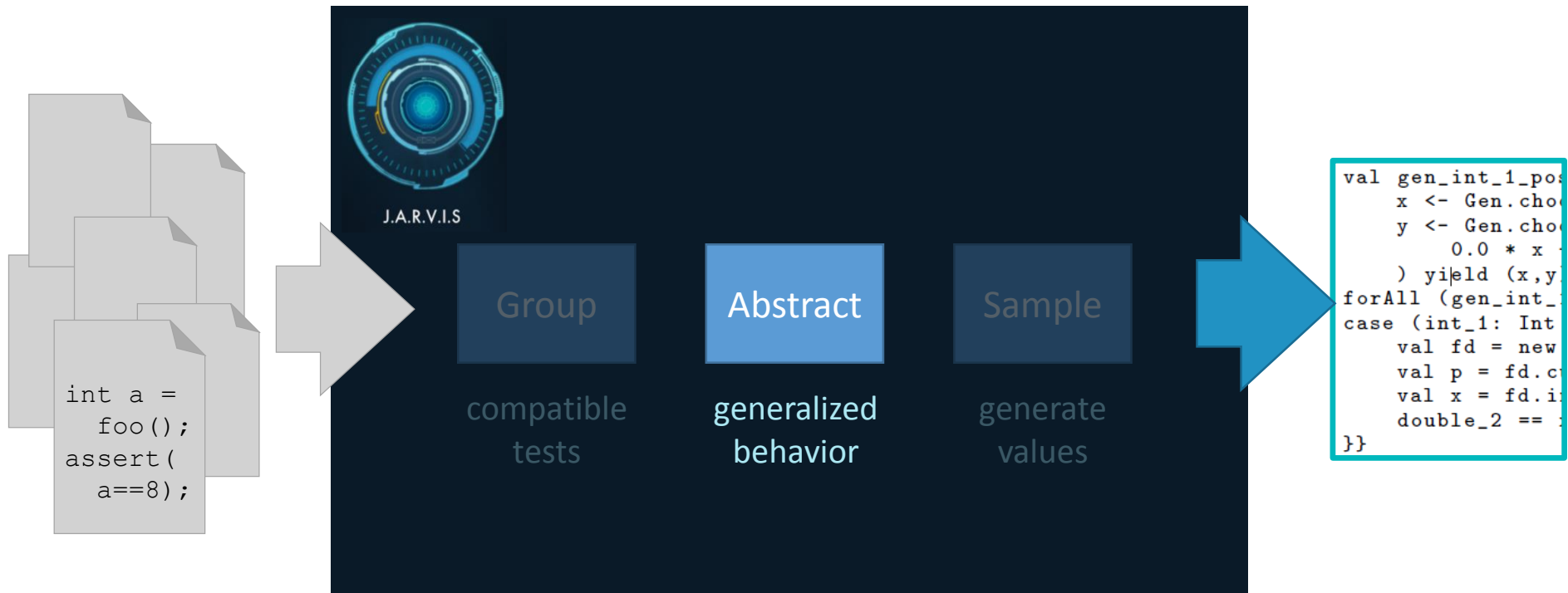
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```

or x, z
where $x=z$

$f_3 = \{x \mapsto 2, y \mapsto 2.1, res \mapsto -\}$

- Convert f_3 to match $pt_1(x: double, y: double, z: double)$ via a generality relation

Step 2



Generalization

- For pt_1 we now have the mappings

$$F = \left\{ \begin{array}{l} \{x \mapsto 2.3, y \mapsto 5.7, z \mapsto 4.0, res \mapsto +\} \\ \{x \mapsto 1.0, y \mapsto 1.0, z \mapsto 1.0, res \mapsto +\} \\ \{x \mapsto 2.0, y \mapsto 2.0, z \mapsto 2.1, res \mapsto -\} \\ \{x \mapsto 2.0, y \mapsto 3.0, z \mapsto 2.5, res \mapsto +\} \end{array} \right\}$$

- Or, $C^+ = \{(2.3, 5.7, 4.0), (1.0, 1.0, 1.0), (2.0, 3.0, 2.5)\}$
 $C^- = \{(2.0, 2.0, 2.1)\}$
- We want an imprecise generalization – restricted widening

Safe Generalization

- Positive and negative examples allow us to examine less precise abstractions, as long as they separate positive from negative
- $(A^+, A^-) \in SG(C, C_{cex})$ if
 - $\forall c \in C. c \in \gamma(A^+), \forall c' \in C_{cex}. c' \in \gamma(A^-)$
 - $\forall c \in C. c \notin \gamma(A^-), \forall c' \in C_{cex}. c' \notin \gamma(A^+)$

Abstraction templates

- Given a library of abstraction templates, we can discard any abstraction that is not in $SG(C^+, C^-)$

$$z = a \cdot x + b \cdot y$$

$$z \geq |a \cdot x - b \cdot y|$$

$$z \leq |a \cdot x - b \cdot y|$$

Reminder: $C^+ = \{(2.3, 5.7, 4.0), (1.0, 1.0, 1.0), (2.0, 3.0, 2.5)\}$
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Abstraction templates

- Given a library of abstraction templates, we can discard any abstraction that is not in $SG(C^+, C^-)$

$$z = a \cdot x + b \cdot y \quad \cdots \longrightarrow \quad z = \frac{1}{2} \cdot x + \frac{1}{2} \cdot y$$

$$z \geq |a \cdot x - b \cdot y|$$

$$z \leq |a \cdot x - b \cdot y|$$

Reminder: $C^+ = \{(2.3, 5.7, 4.0), (1.0, 1.0, 1.0), (2.0, 3.0, 2.5)\}$
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No a, b in $SG(C^+, C^-)$

$$z \leq |a \cdot x - b \cdot y|$$

Reminder: $C^+ = \{(2.3, 5.7, 4.0), (1.0, 1.0, 1.0), (2.0, 3.0, 2.5)\}$
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No a, b in $SG(C^+, C^-)$

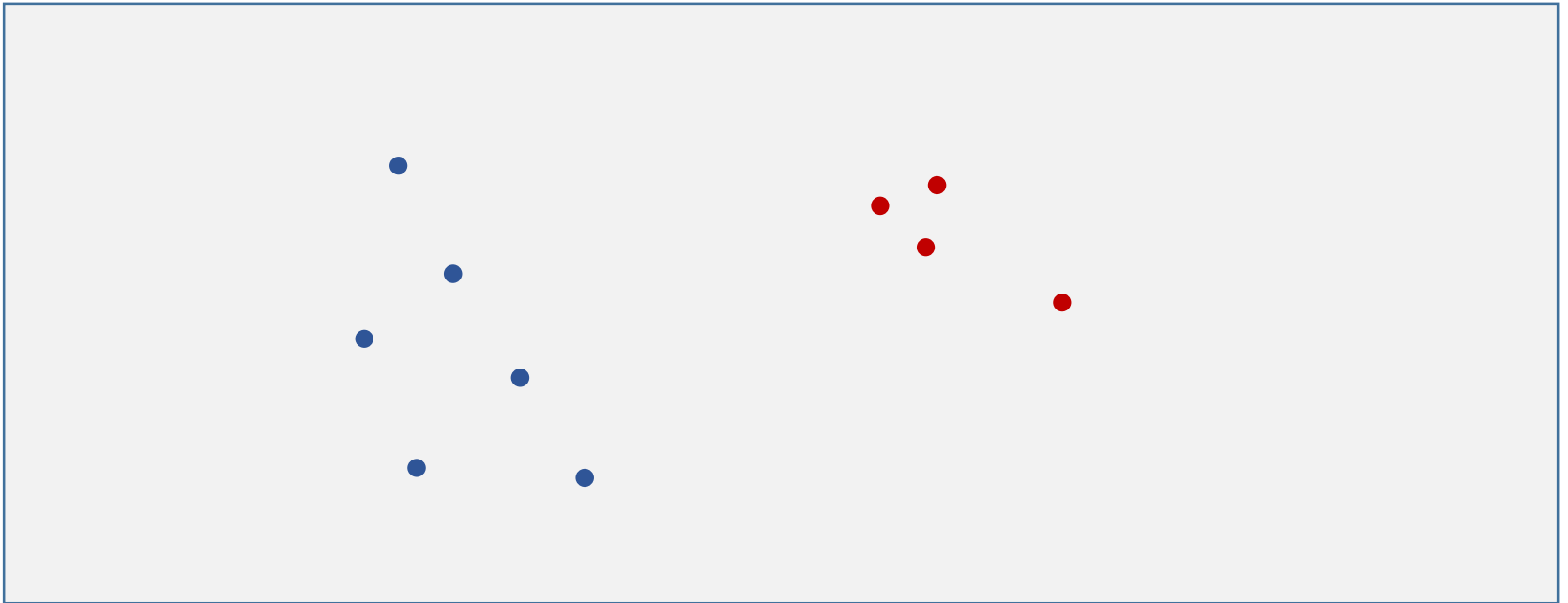
$$z \leq |a \cdot x - b \cdot y|$$



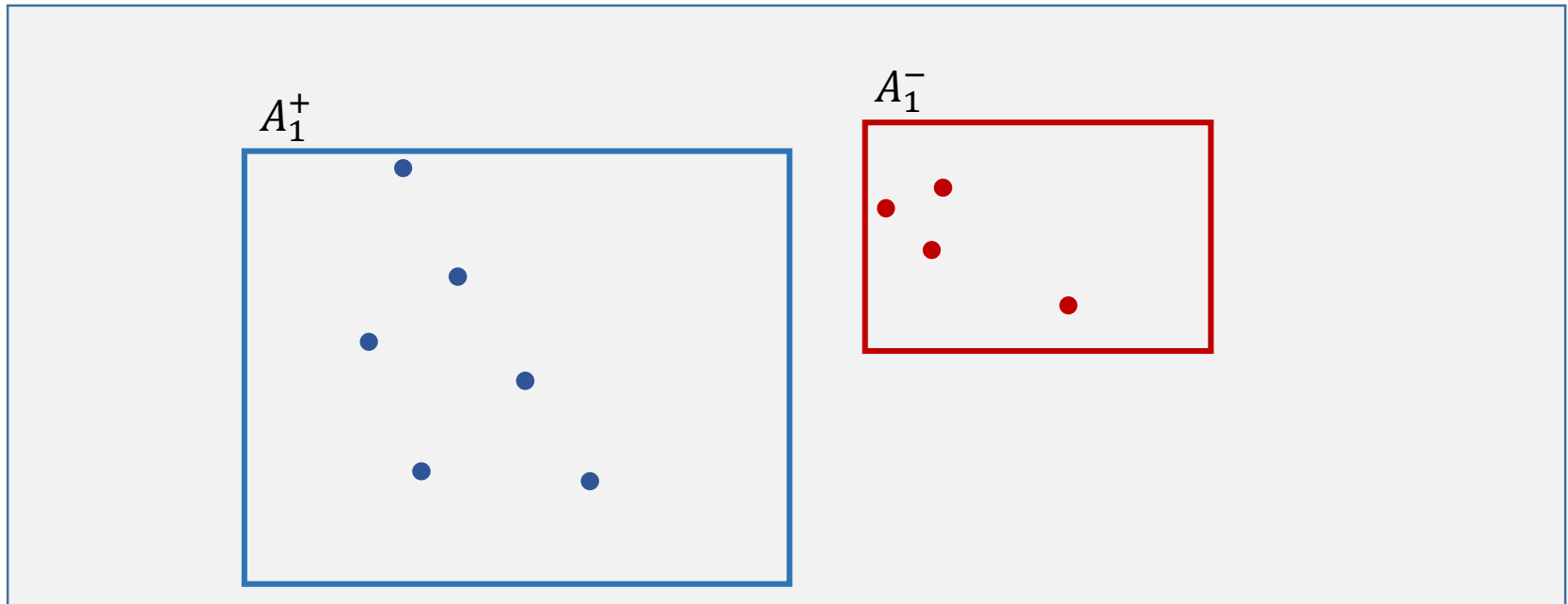
$$z \leq \left| \frac{2}{5} \cdot x + \frac{3}{5} \cdot y \right|$$

Reminder: $C^+ = \{(2.3, 5.7, 4.0), (1.0, 1.0, 1.0), (2.0, 3.0, 2.5)\}$
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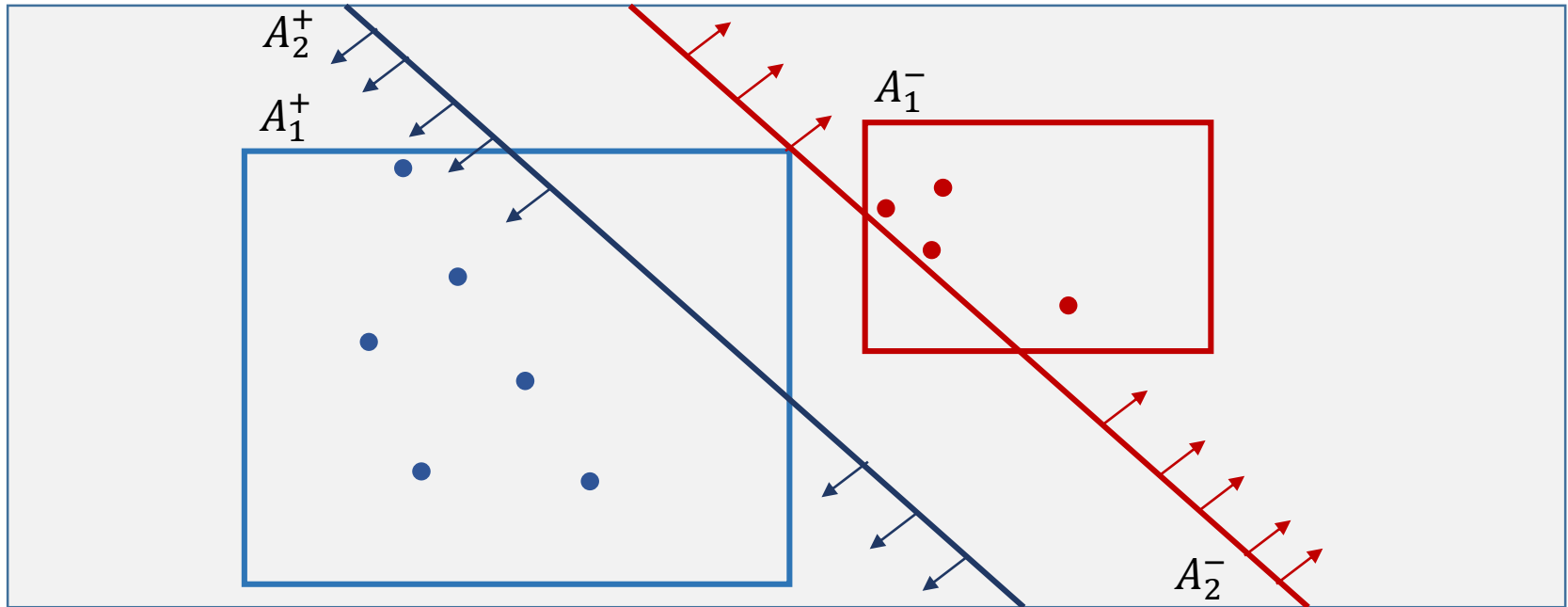
Too Few Examples



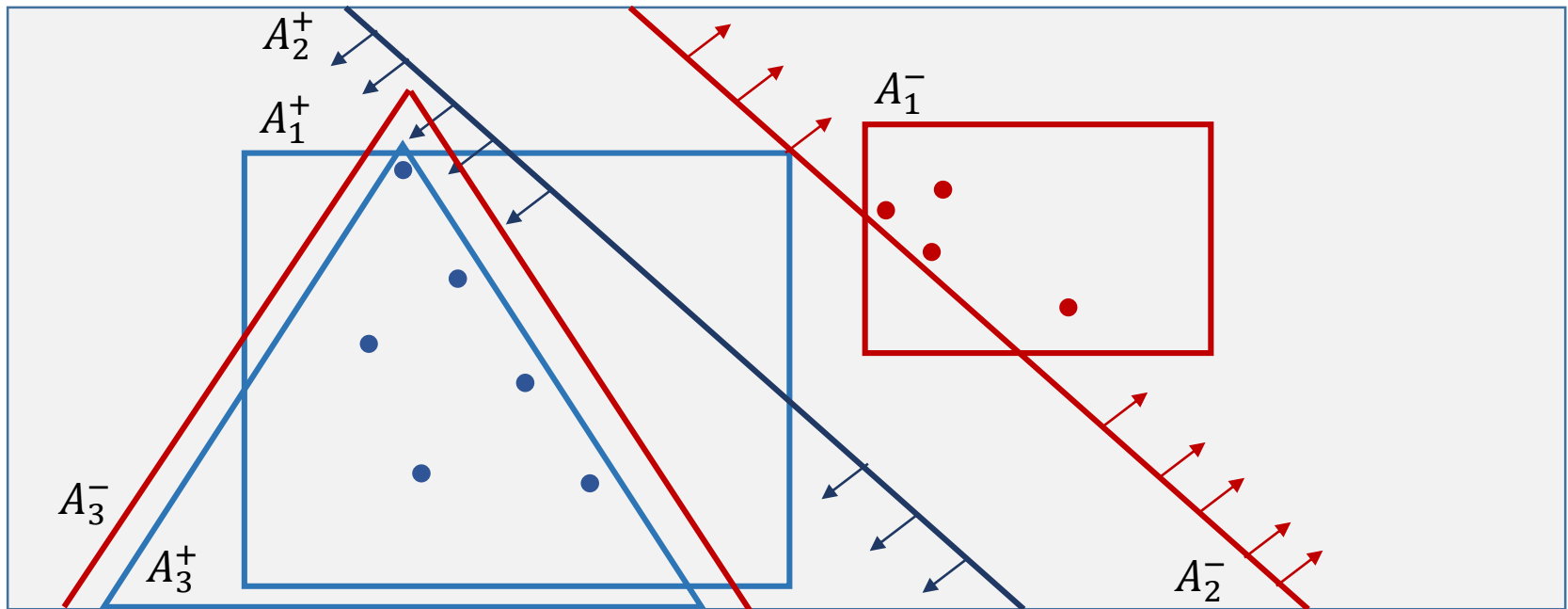
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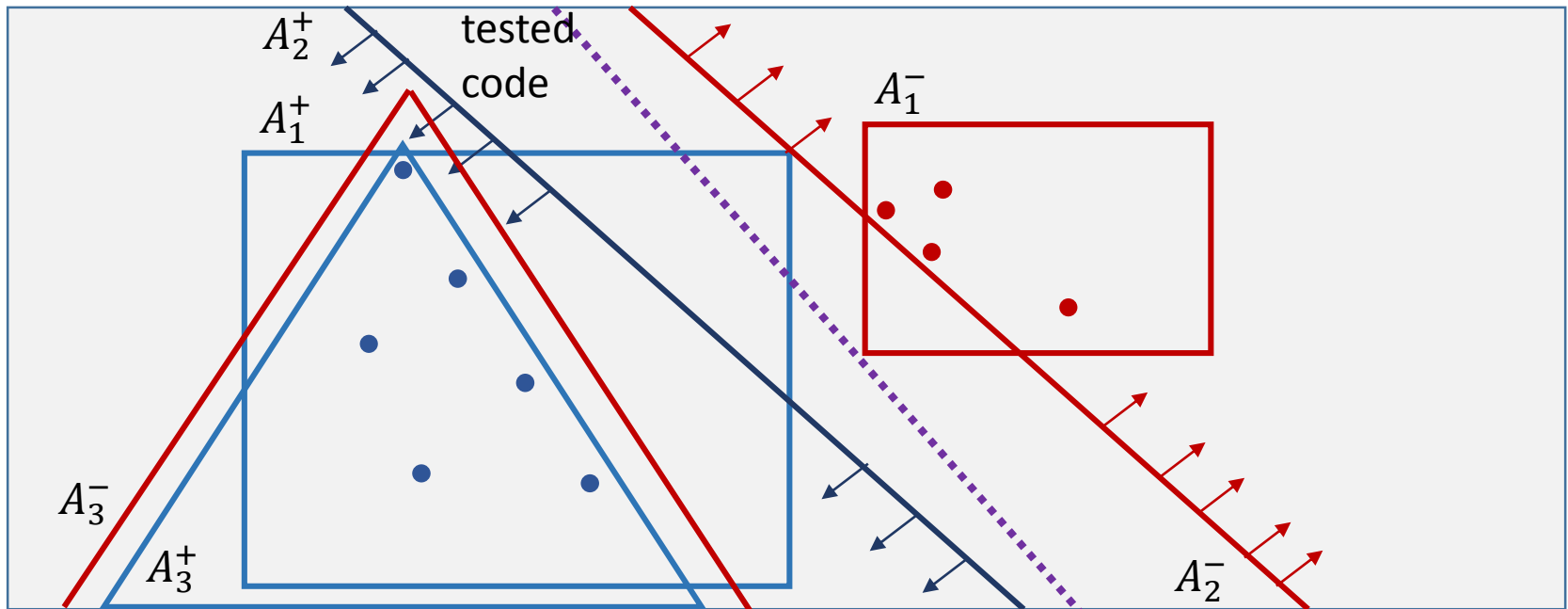
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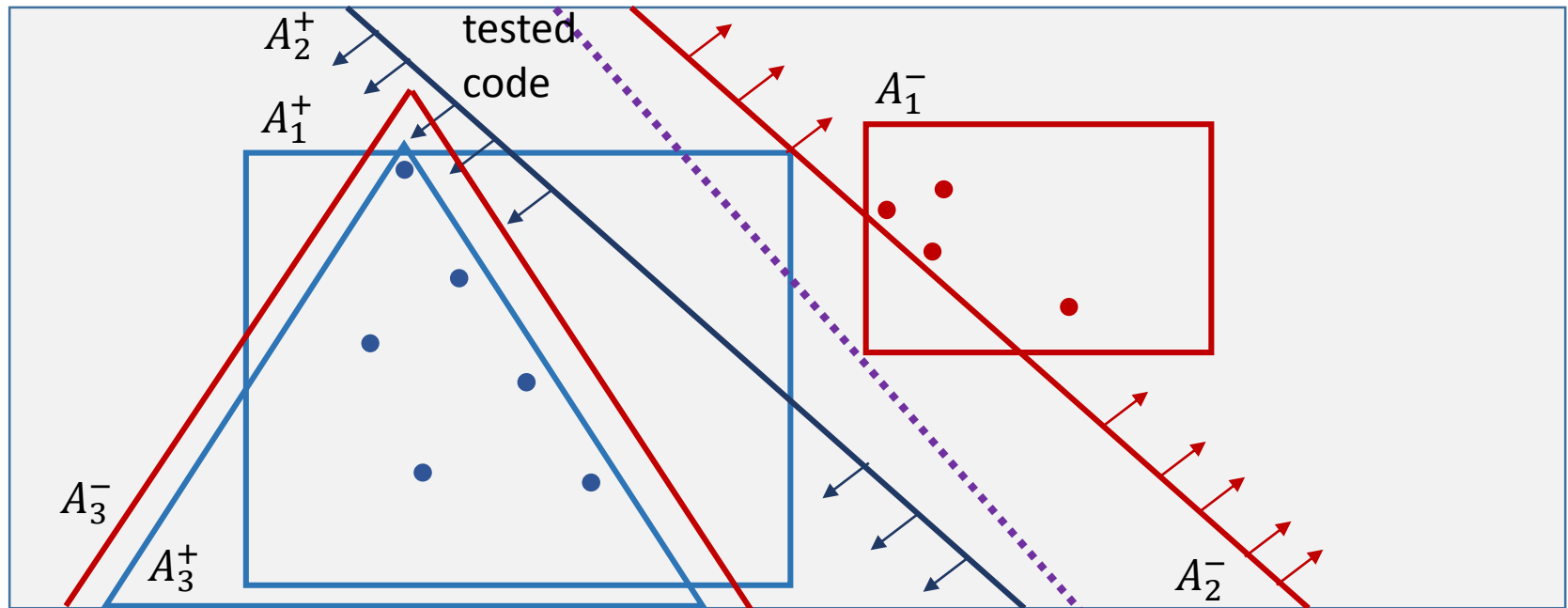
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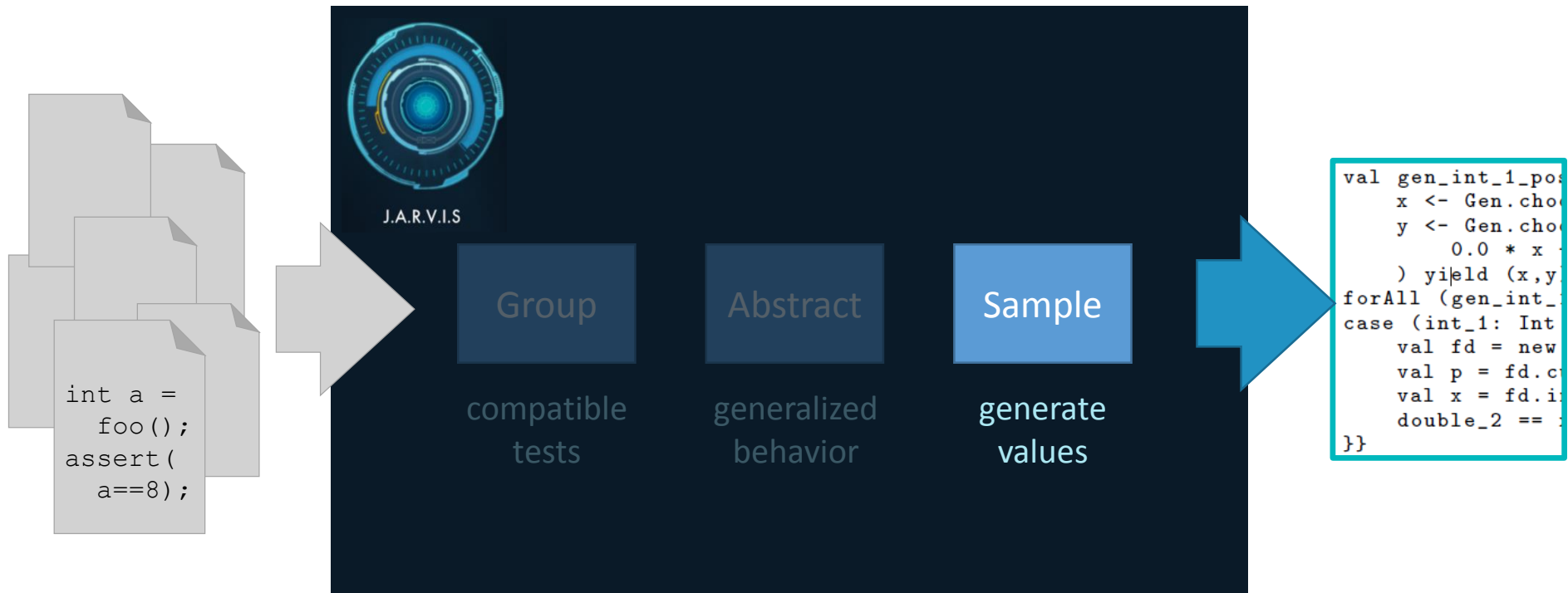
Too Few Examples



- By ranking, we select:

$$(A^+, A^-) = \left(z = \frac{1}{2}x + \frac{1}{2}y, z \neq \frac{1}{2}x + \frac{1}{2}y \right)$$

Step 3



Sampling

- Just sample our abstractions. Done!(?)

Sampling

- Just sample our abstractions. Done!(!?)

```
//test 2
```

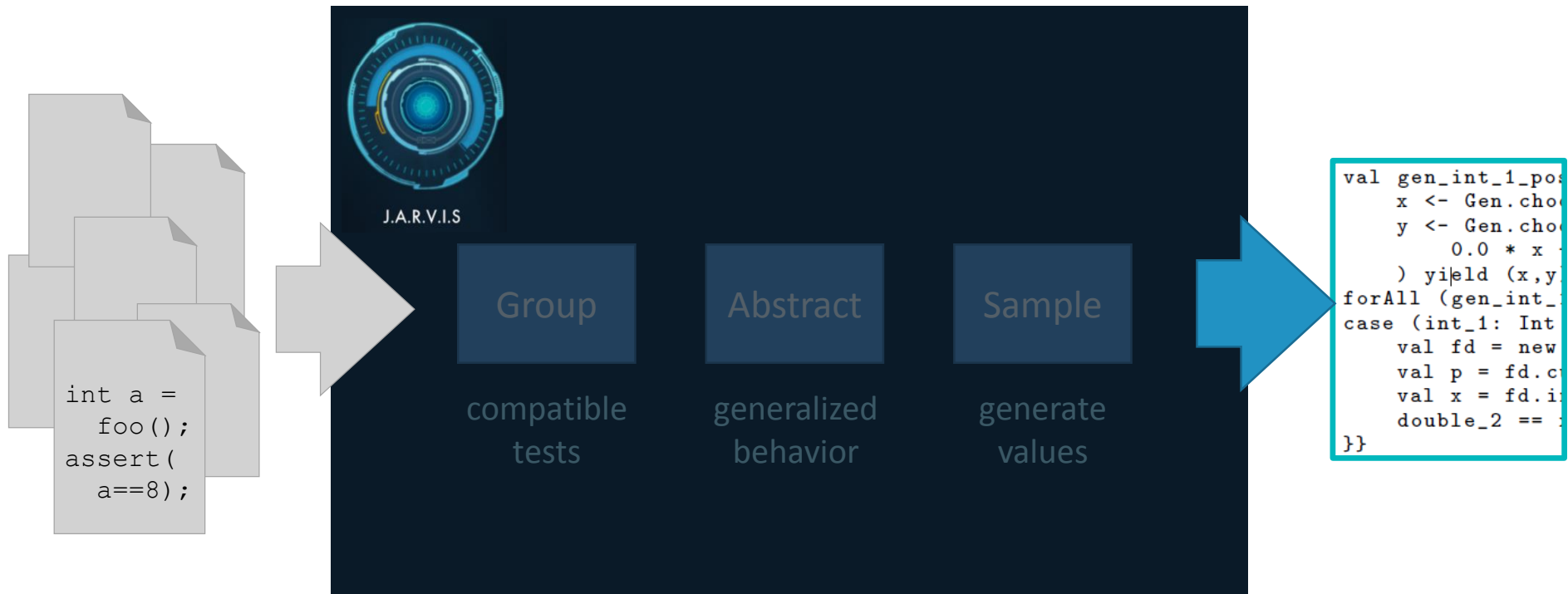
```
Interval interval2 = new Interval(1.0, 1.0);  
assertEquals(1.0, interval2.getBarycenter(),  
Precision.EPSILON);
```

- User tests represent weighted sampling with constraints
 - Passing an int to a double parameter
 - Equality constraint

Sampling: Solution

- Use PT types and constraints
 - If $x = y = z$ exists in the code, sample from $z = \frac{1}{2}x + \frac{1}{2}y$ where $x = y = z$
 - If $(x: int, y: int, z: double)$ sample by type
- This is a little delicate:
 - Only sample A^+ for PTs where $C^+ \neq \emptyset$
 - And the same for A^- and C^-

Output



Putting it all together

```
val gen_pos = for(  
  x <- Arbitrary.arbitrary[Double];  
  y <- Arbitrary.arbitrary[Double];  
  z = 0.5*x + 0.5*y) yield (x,y,z)  
forall (gen_pos) {  
  val interval = new Interval(x,y);  
  z ≈ interval.getBarycenter()  
}
```

parameterized sampling
test

Results: Coverage

Test		Parameter space	Java CUT		Scala PBT	
			IC	PVC	IC	PVC
Lang	CharUtilsTest::isAscii	<i>char</i>	37	6	37	59
	CharUtilsTest::isPrintable	<i>char</i>	40	195	40	45
Commons-Math	FastMathTest::testMinMaxDouble	<i>double</i> ²	782	9	770	400
	FastMathTest::toIntExact	<i>int</i>	738	2001	738	65
	IntervalTest	<i>double</i> ²	38	2	3869	2
	PolynomialFunctionTest::testConstants	<i>double</i>	53	5	53	105
	PolynomialFunctionTest::testfirstDerivativeComparison	<i>double</i>	117	7	117	264
	PolynomialFunctionTest::testLinear	<i>double</i>	71	5	71	160
	PrecisionTest	<i>double</i> ³	871	8	876	102
UnivariateFunctionTest::testAbs	<i>double</i>	739	5	739	506	

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Instruction coverage



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Value coverage

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MATH-1256: Interval bounds

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Interval interval = new Interval(2.3, 5.7);  
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$pt_1(x, y, z)$

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$f_1 = \{x \mapsto 2.3, y \mapsto 5.7, z \mapsto 3.4, res \mapsto +\}$

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$pt_2(x, y)$

```
Interval interval = new Interval(x, x);  
assert(y == interval.getSize());  
    type(x) = type(y) = double
```

$f_2 = \{x \mapsto 1.0, y \mapsto 0.0, res \mapsto +\}$

MATH-1256: Interval bounds

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assertEquals(3.4, interval.getSize());
```



$pt_1(x, y, z)$

```
Interval interval = new Interval(x, y);
assert(z == interval.getSize());
    type(x) = type(y) = type(z) = double
```

$f_1 = \{x \mapsto 2.3, y \mapsto 5.7, z \mapsto 3.4, res \mapsto +\}$

$pt_2(x, y)$

```
Interval interval = new Interval(x, x);
assert(y == interval.getSize());
    type(x) = type(y) = double
```

$f_2 = \{x \mapsto 1.0, y \mapsto 0.0, res \mapsto +\}$

$C^+ = \left\{ \begin{array}{l} (2.3, 5.7, 3.4) \\ (1.0, 1.0, 0.0) \end{array} \right\}$



$|y - z| = x$

MATH-1256: Interval bounds

```
//test 1  
Interval interval = new Interval(2.3, 5.7);  
assertEquals(3.4, interval.getSize());
```



$pt_1(x, y, z)$

```
Interval interval = new Interval(x, y);  
assert(z == interval.getSize());  
    type(x) = type(y) = type(z) = double
```

$f_1 = \{x \mapsto 2.3, y \mapsto 5.7, z \mapsto 3.4, res \mapsto +\}$

$pt_2(x, y)$

```
Interval interval = new Interval(x, x);  
assert(y == interval.getSize());  
    type(x) = type(y) = double
```

$f_2 = \{x \mapsto 1.0, y \mapsto 0.0, res \mapsto +\}$

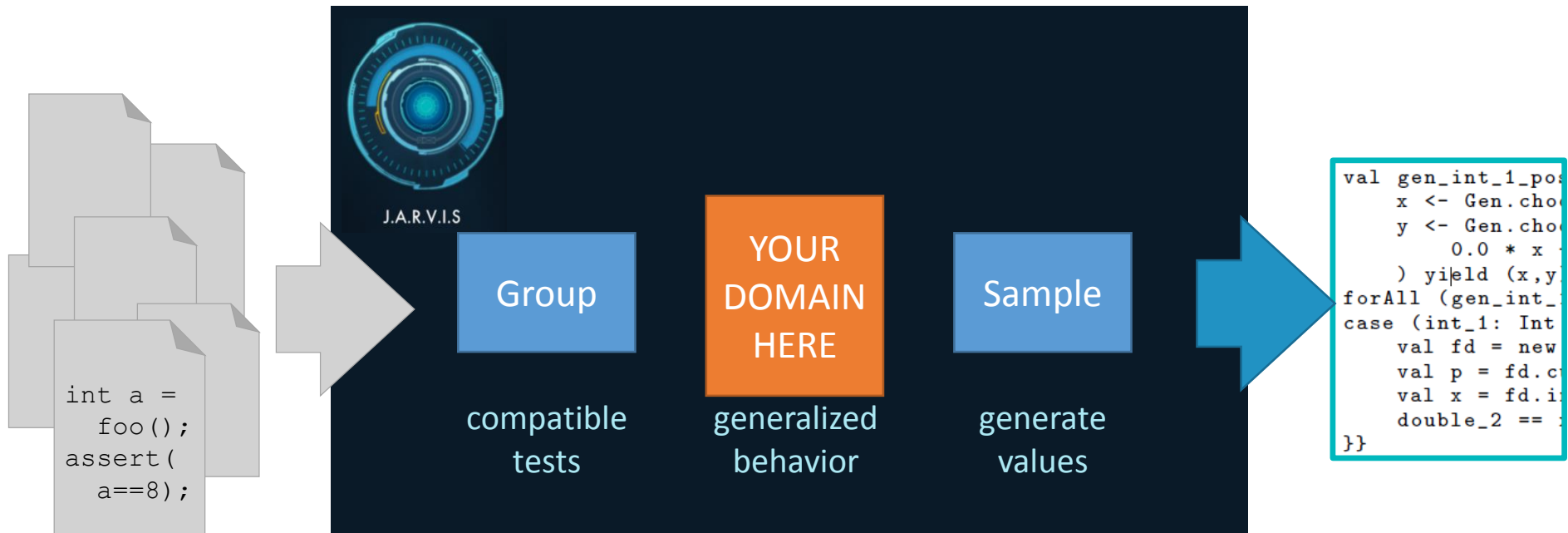
$$C^+ = \left\{ \begin{array}{l} (2.3, 5.7, 3.4) \\ (1.0, 1.0, 0.0) \end{array} \right\}$$



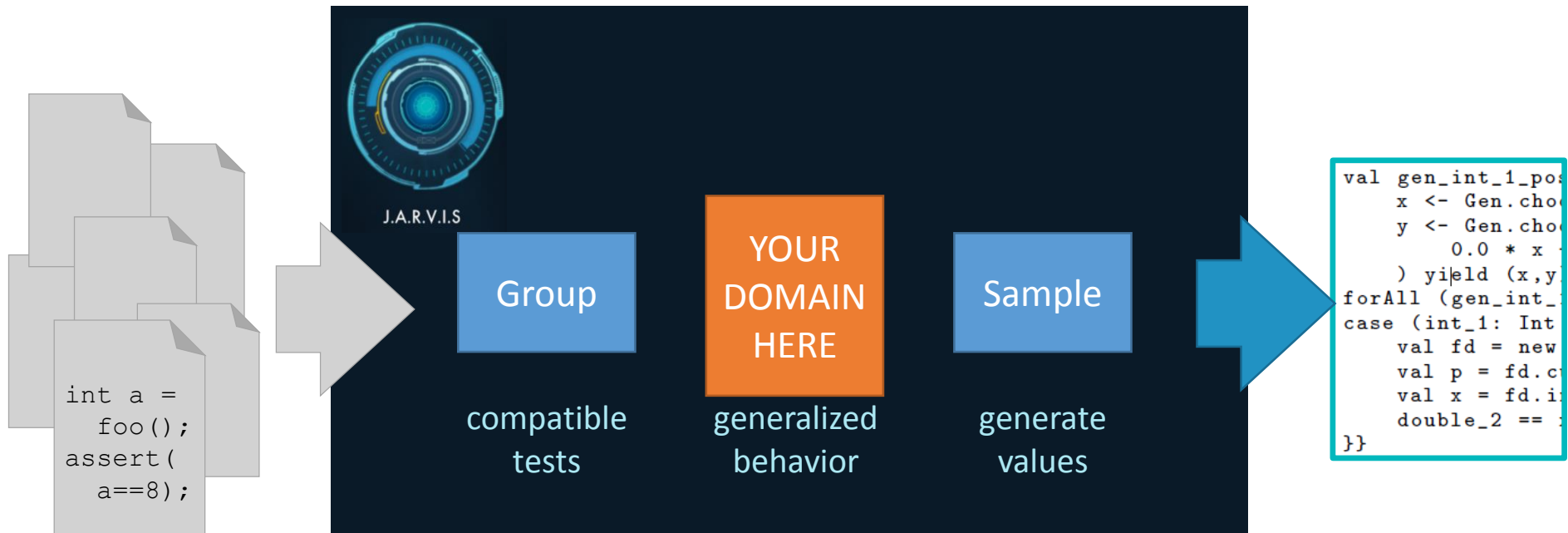
$$|y - z| = x$$

Bug exists in 50% of the space!

Conclusion



Conclusion



@Test

```
public void thankYou() {  
    List<Questions> questions = takeQuestions();  
    Assert.assertFalse(questions.isEmpty());  
}
```