

Subject Index

The style of a page number indicates the nature of the text material:

- the style 123 indicates a definition,
- the style 123 indicates an extended discussion, and
- the style 123 indicates a short discussion or brief mention.

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