# **CSE203B** Convex Optimization

CK Cheng Dept. of Computer Science and Engineering University of California, San Diego

# Outlines

- Staff
  - Instructor: CK Cheng
  - TAs: Po-Ya Hsu, Chester Holtz, James Lin
- Logistics
  - Websites, Textbooks, References, Grading Policy
- Classification
  - History and Category
- Scope
  - Coverage

# Information about the Instructor

- Instructor: CK Cheng
- Education: Ph.D. in EECS UC Berkeley
- Industrial Experiences: Engineer of AMD, Mentor Graphics, Bellcore; Consultant for technology companies
- Research: Design Automation, Brain Computer Interface
- Email: <u>ckcheng+203B@ucsd.edu</u>, Office: Room CSE2130
- Office hour will be posted on the course website
- Websites
  - http://cseweb.ucsd.edu/~kuan
  - http://cseweb.ucsd.edu/classes/wi21/cse203B

#### Staff

Teaching Assistant

- Po-Ya Hsu, p8hsu@ucsd.edu
- Chester Holtz, chholtz@ucsd.edu
- James Lin, til002@ucsd.edu

# Logistics: Class Schedule

Class Time: 2-320 PM TTH,

Discussion Session: 2-250 PM F (Separate zoom link)

Class website: http://cseweb.ucsd.edu/classes/wi21/cse203B

Piazza link: piazza.com/ucsd/winter2021/cse203b/home

Gradescope link: https://www.gradescope.com/courses/221286

Zoom lecture:

https://ucsd.zoom.us/j/98033436384?pwd=Y3UrMDIIY0py OTRmTGovVENQSXpvdz09

For access code of the links, check with TAs or the instructor

# Logistics: Grading

Homeworks (40%)

- Exercises (Grade by completion)
- Assignments (Grade by content)

Project (25%)

- Theory or applications of convex optimization
- Survey of the state of the art approaches
- Outlines, references (W4)
- Report (6PM 3/18/2021, W11)

Exams (35%)

• Midterm, 2/16/2021, T (W7)

# Logistics: Textbooks

Required text:

- Convex Optimization, Stephen Boyd and Lieven Vandenberghe, Cambridge, 2004
- Review appendix A in the first week

References

- Numerical Recipes: The Art of Scientific Computing, Third Edition, W.H. Press, S.A. Teukolsky, W.T. Vetterling, and B.P. Flannery, Cambridge University Press, 2007.
- Functions of Matrices: Theory and Computation, N.J. Higham, SIAM, 2008.
- Fall 2016, Convex Optimization by R. Tibshirani, http://www.stat.cmu.edu/~ryantibs/convexopt/
- EE364a: Convex Optimization I, S. Boyd, http://stanford.edu/class/ee364a/

# Classification: Brief history of convex optimization

Theory (convex analysis): 1900–1970

Algorithms

- 1947: simplex algorithm for linear programming (Dantzig)
- 1970s: ellipsoid method and other subgradient methods
- 1980s & 90s: polynomial-time interior-point methods for convex Optimization (Karmarkar 1984, Nesterov & Nemirovski 1994)
- since 2000s: many methods for large-scale convex optimization Applications
- before 1990: mostly in operations research, a few in engineering
- since 1990: many applications in engineering (control, signal processing, communications, circuit design, . . . )
- since 2000s: machine learning and statistics

#### Classification

Tradition	Linear Programming	Nonlinear Programming	Discrete Integer Programming
	Simplex	Lagrange multiplier	Trial and error
	Primal/Dual	Gradient descent	Cutting plane
This class	Interior point method	Newton's iteration	Relaxation

This class

Convex Optimization	Nonconvex, Discrete Problems	
Primal/Dual, Lagrange multiplier	Local Optimal Solution Search,	
Gradient descent	SA (Simulated Annealing), ILP (Integer Linear Programming),	
Newton's iteration	MLP (Mixed Integer Programming),	
Interior point method	SAT (Satisfiability), SMT (Satisfiability Modulo Theories), etc.	

### Scope of Convex Optimization

For a convex problem, a local optimal solution is also a global optimum solution.

# Scope

Problem Statement (Key word: convexity)

- Convex Sets (Ch2)
- Convex Functions (Ch3)
- Formulations (Ch4)

Tools (Key word: mechanism)

- Duality (Ch5)
- Optimal Conditions (Ch5)

Applications (Ch6,7,8) (Key words: complexity, optimality)

Coverage depends upon class schedule

Algorithms (Key words: **Taylor's expansion**)

- Unconstrained (Ch9)
- Equality constraints (Ch10)
- Interior method (Ch11)

# Scope

CSE203B Convex Optimization

• Optimization of convex function <u>with constraints</u> which form convex domains.

Background

- Linear algebra
- Polynomial and fractional expressions
- Log and exponential functions
- Optimality of continuously differentiable functions

Concepts and Techniques to Master in CSE203B

- Convexity
- Hyperplane
- Duality
- KKT optimality conditions