

# Discussion

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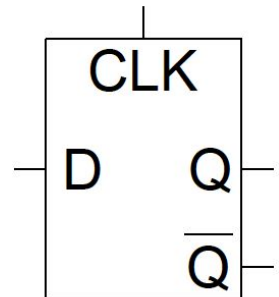
# Outline

- Review of Flip-Flops
- Overview of FSM
- Excitation table -> State Diagram
- State Diagram -> Circuit Implementation

# D Latch

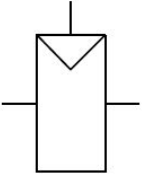
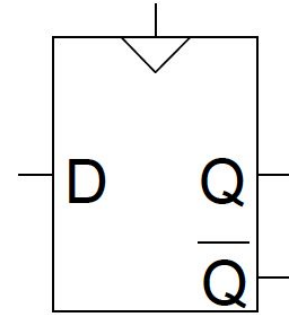
- Two inputs:  $CLK$ ,  $D$ 
  - $CLK$ : controls *when* output changes to
  - $D$  (the data input): controls *what* the output changes to
- Function
  - When  $CLK=1$ ,  $D$  passes through  $Q$  (the latch is *transparent*)
  - When  $CLK=0$ ,  $Q$  holds its previous value (the latch is *opaque*)
- Avoids invalid state when  $Q \neq \overline{Q}$

D Latch Symbol

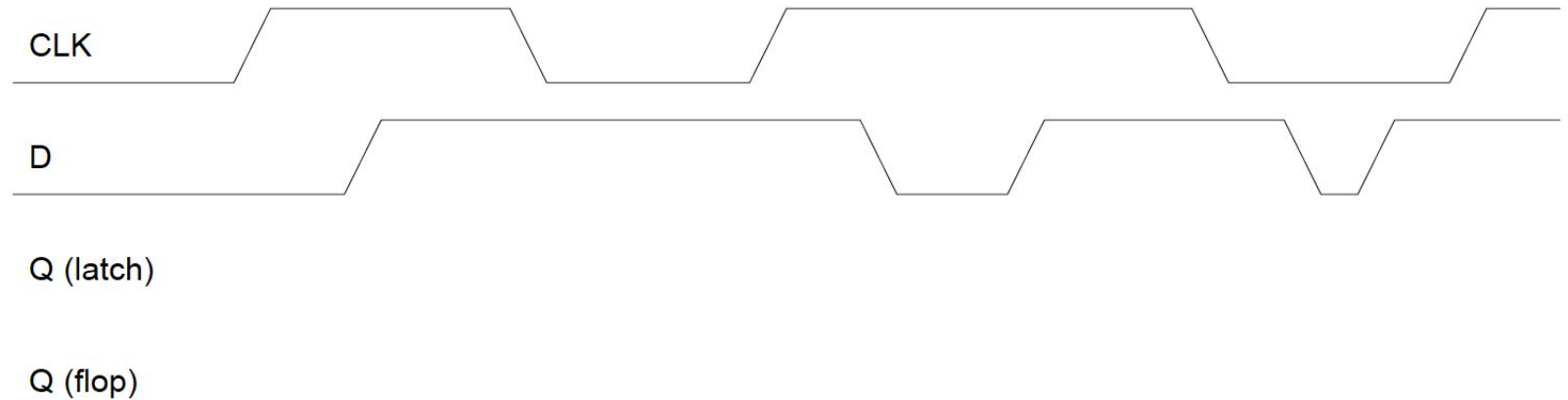
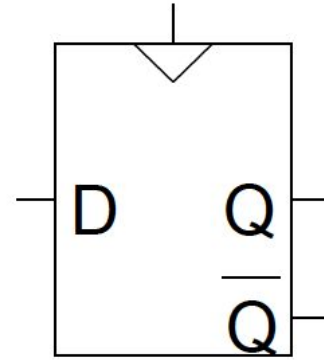
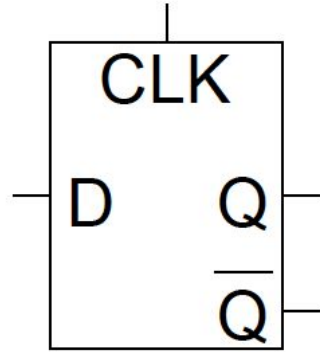


# D Flip-Flop

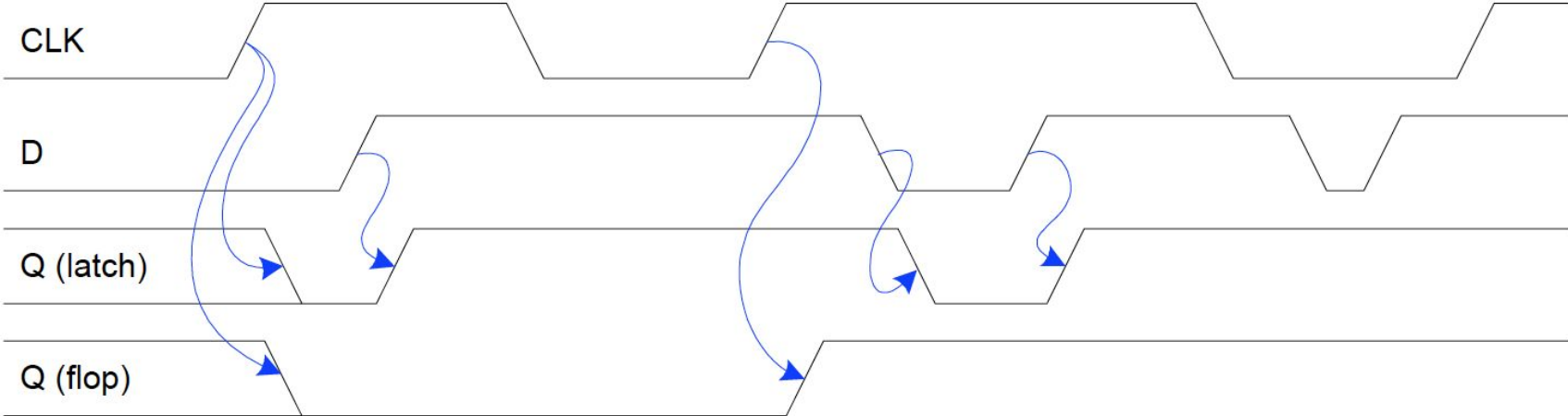
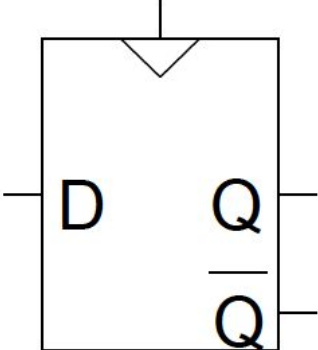
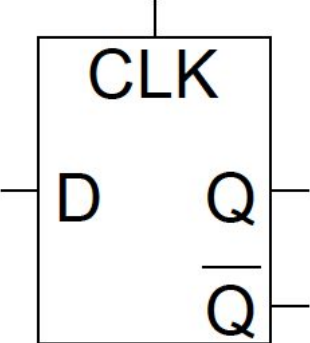
- Two inputs:  $CLK$ ,  $D$
- Function
  - The flip-flop “samples”  $D$  on the rising edge of  $CLK$ 
    - When  $CLK$  rises from 0 to 1,  $D$  passes through to  $Q$
    - Otherwise,  $Q$  holds its previous value
  - $Q$  changes only on the rising edge of  $CLK$
- A flip-flop is an edge-triggered device because it is activated on the clock edge (when  $CLK$  rises from 0 1)



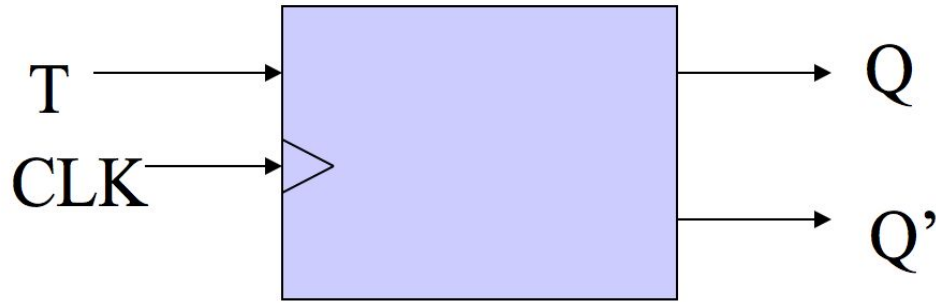
# D Flip-Flop vs D-Latch



# D Flip-Flop vs D-Latch



# T Flip-Flop



State table

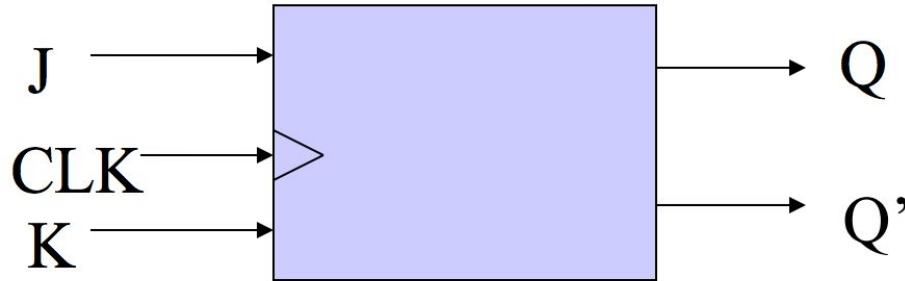
| PS \ T | 0 | 1 |
|--------|---|---|
| 0      | 0 | 1 |
| 1      | 1 | 0 |

← Q(t+1)

Characteristic Expression

$$Q(t+1) = Q'(t)T(t) + Q(t)T'(t)$$

# JK Flip-Flop



State table

| PS \ JK | 00 | 01 | 10 | 11 |
|---------|----|----|----|----|
| 0       | 0  | 0  | 1  | 1  |
| 1       | 1  | 0  | 1  | 0  |

Q(t+1)

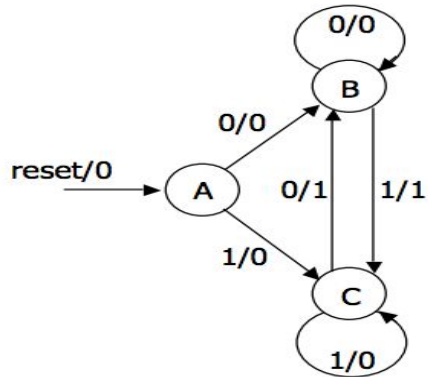
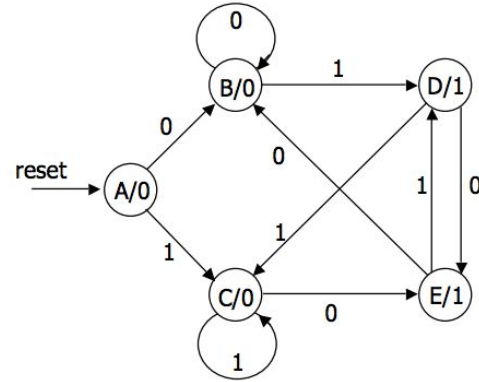
Characteristic Expression

$$Q(t+1) = Q(t)K'(t) + Q'(t)J(t)$$



# Finite State Machines

- Describe circuit behaviour over time
- Moore machine: output depends on current state only
- Mealy machine: output depends on current state and inputs



# #1

- Given : Excitation table
- Identify states and derive a state table
- State diagram
- Input Output Relation

# #1 Excitation Table

| Q2 | Q1 | Q0 | X | D2 | D1 | D0 | Z |
|----|----|----|---|----|----|----|---|
| 0  | 0  | 0  | 0 | 0  | 0  | 0  | 0 |
| 0  | 0  | 0  | 1 | 0  | 0  | 1  | 0 |
| 0  | 0  | 1  | 0 | 0  | 0  | 0  | 0 |
| 0  | 0  | 1  | 1 | 0  | 1  | 0  | 0 |
| 0  | 1  | 0  | 0 | 0  | 0  | 0  | 0 |
| 0  | 1  | 0  | 1 | 0  | 1  | 1  | 0 |
| 0  | 1  | 1  | 0 | 1  | 0  | 0  | 0 |
| 0  | 1  | 1  | 1 | 0  | 1  | 1  | 0 |
| 1  | 0  | 0  | 0 | 0  | 0  | 0  | 0 |
| 1  | 0  | 0  | 1 | 0  | 0  | 1  | 1 |

# Step 1: Identify states and state table

S0 -> 000

S1 -> 001

S2 -> 010

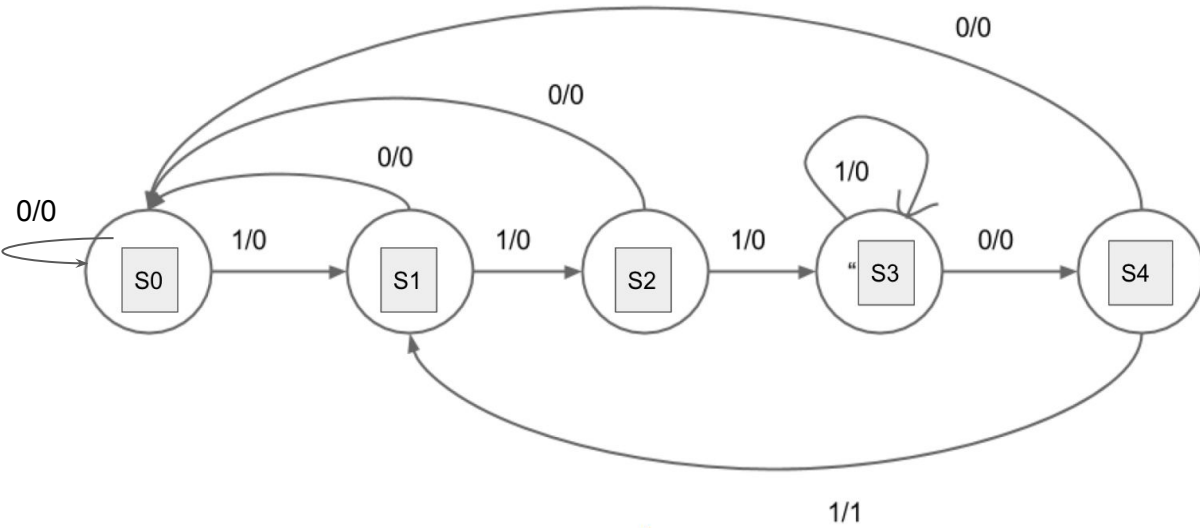
S3 -> 011

S4 -> 100

| PS/ Input | X = 0 | X = 1 |
|-----------|-------|-------|
| S0        | S0,0  | S1,0  |
| S1        | S0,0  | S2,0  |
| S2        | S0,0  | S3,0  |
| S3        | S4,0  | S3,0  |
| S4        | S0,0  | S1,1  |

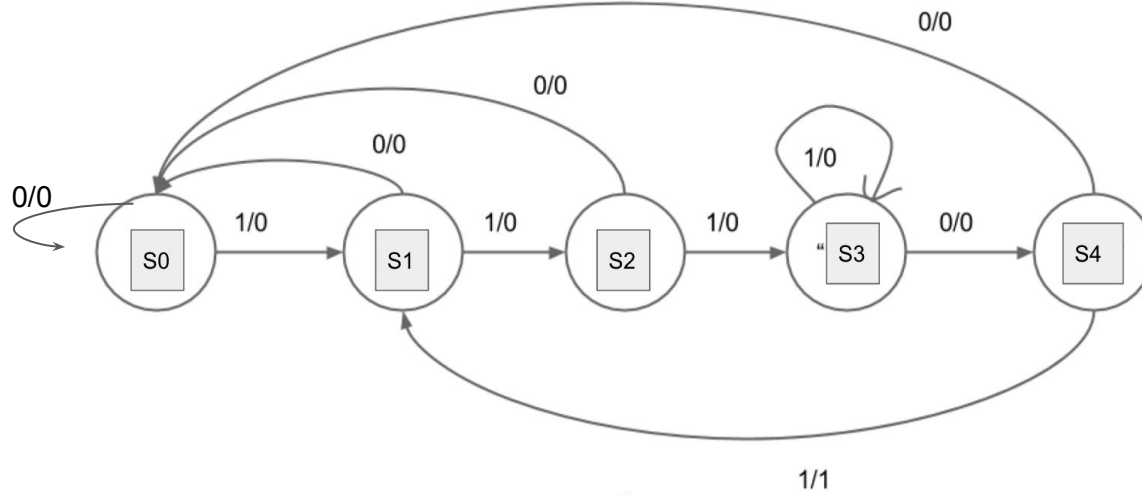
| Q2 | Q1 | Q0 | X | D2 | D1 | D0 | Z |
|----|----|----|---|----|----|----|---|
| 0  | 0  | 0  | 0 | 0  | 0  | 0  | 0 |
| 0  | 0  | 0  | 1 | 0  | 0  | 1  | 0 |
| 0  | 0  | 1  | 0 | 0  | 0  | 0  | 0 |
| 0  | 0  | 1  | 1 | 0  | 1  | 0  | 0 |
| 0  | 1  | 0  | 0 | 0  | 0  | 0  | 0 |
| 0  | 1  | 0  | 1 | 0  | 1  | 1  | 0 |
| 0  | 1  | 1  | 0 | 1  | 0  | 0  | 0 |
| 0  | 1  | 1  | 1 | 0  | 1  | 1  | 0 |
| 1  | 0  | 0  | 0 | 0  | 0  | 0  | 0 |
| 1  | 0  | 0  | 1 | 0  | 0  | 1  | 1 |

# Step 2: State Diagram



| PS/ Input | X = 0 | X = 1 |
|-----------|-------|-------|
| S0        | S0,0  | S1,0  |
| S1        | S0,0  | S2,0  |
| S2        | S0,0  | S3,0  |
| S3        | S4,0  | S3,0  |
| S4        | S0,0  | S1,1  |

# Step 3: Input Output Relation



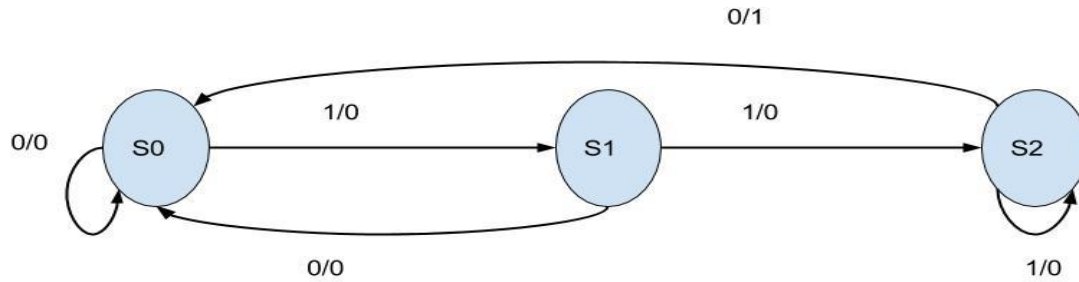
## Example Output Sequence

| Time       | 0  | 1  | 2  | 3  | 4  | 5  |
|------------|----|----|----|----|----|----|
| Input (X)  | 0  | 1  | 1  | 1  | 0  | 1  |
| Next State | S0 | S1 | S2 | S3 | S4 | S1 |
| Output     | 0  | 0  | 0  | 0  | 0  | 1  |

## #2

- Given : State Diagram
- Identify states and derive a state table
- Excitation Table
- Equations (use K-maps if required)
- Circuit Implementation

## #2 State Diagram





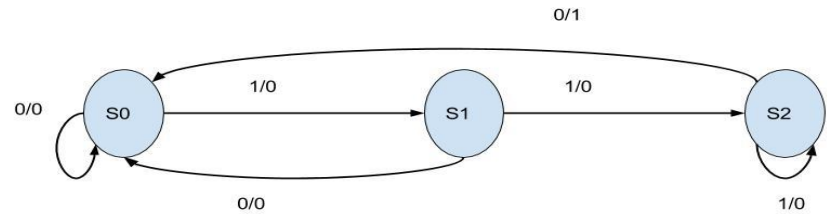
# Step 1: State Assignment and State Table

| S(t) \ X | 0    | 1    |
|----------|------|------|
| S0       | S0,0 | S1,0 |
| S1       | S0,0 | S2,0 |
| S2       | S0,1 | S2,0 |

S0 : 00

S1: 01

S2: 10



## Step 2: Excitation Table

| id | Q1Q0X | D1 | D0 | y |
|----|-------|----|----|---|
| 0  | 000   | 0  | 0  | 0 |
| 1  | 001   | 0  | 1  | 0 |
| 2  | 010   | 0  | 0  | 0 |
| 3  | 011   | 1  | 0  | 0 |
| 4  | 100   | 0  | 0  | 1 |
| 5  | 101   | 1  | 0  | 0 |
| 6  | 110   | X  | X  | X |
| 7  | 111   | X  | X  | X |

| S(t) \ X | 0    | 1    |
|----------|------|------|
| S0       | S0,0 | S1,0 |
| S1       | S0,0 | S2,0 |
| S2       | S0,1 | S2,0 |

S0 : 00

S1: 01

S2: 10

# Step 3: Characteristic Equations

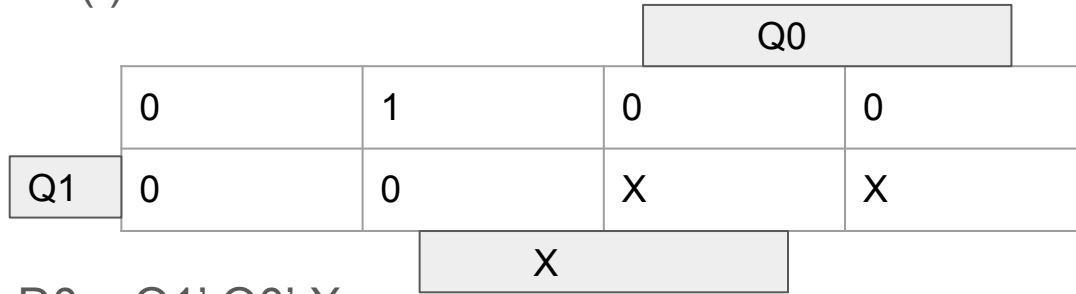
D1(t)

|    |   |   |    |   |
|----|---|---|----|---|
|    |   |   | Q0 |   |
|    | 0 | 0 | 1  | 0 |
| Q1 | 0 | 1 | X  | X |
|    |   | X |    |   |

$$\begin{aligned} D1 &= Q0X + Q1X \\ &= X.(Q0 + Q1) \end{aligned}$$

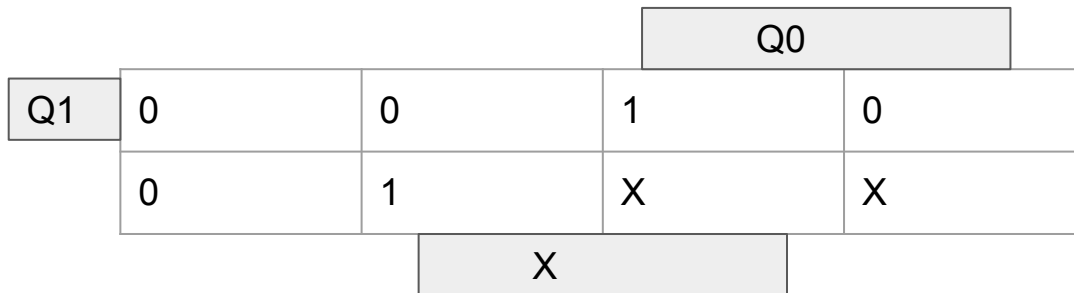
| id | Q1Q0X | D1 | D0 | y |
|----|-------|----|----|---|
| 0  | 000   | 0  | 0  | 0 |
| 1  | 001   | 0  | 1  | 0 |
| 2  | 010   | 0  | 0  | 0 |
| 3  | 011   | 1  | 0  | 0 |
| 4  | 100   | 0  | 0  | 1 |
| 5  | 101   | 1  | 0  | 0 |
| 6  | 110   | X  | X  | X |
| 7  | 111   | X  | X  | X |

D0(t)



$$D0 = Q1'.Q0'.X$$

y



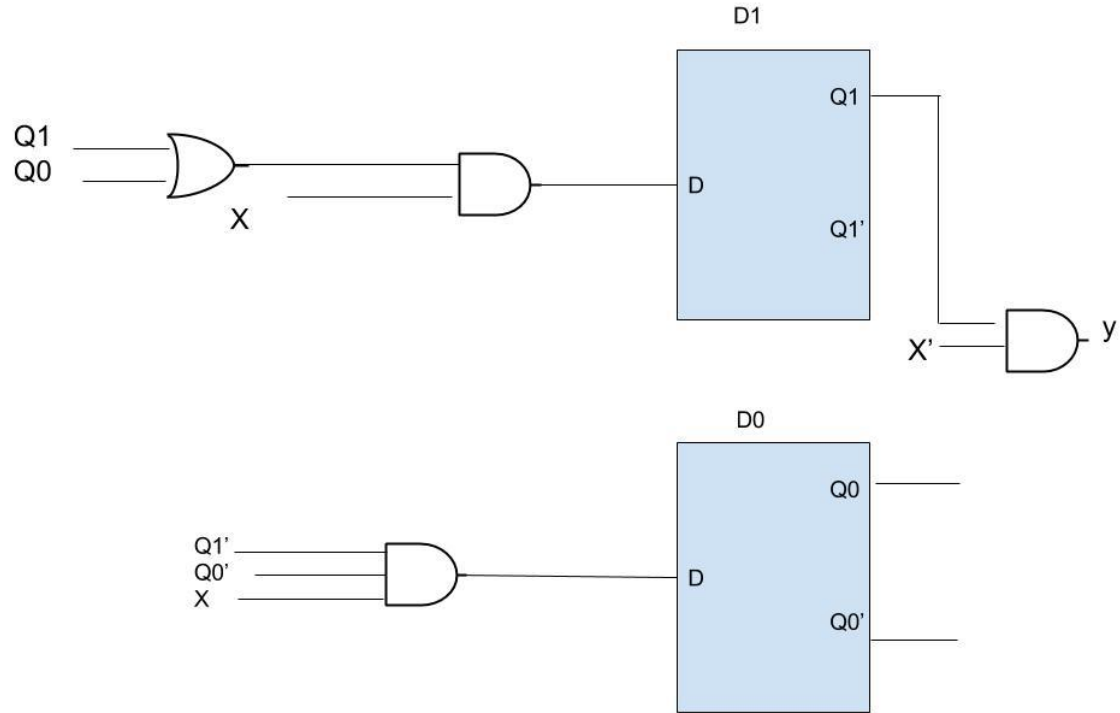
$$y = Q1.X'$$

# Step 4: Circuit Implementation

$$D1 = Q0X + Q1X$$

$$D0 = Q1'Q0'X$$

$$y = Q1X'$$



**Thank you!**