

# Simulating authenticated broadcast

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For round-based algorithms, a protocol that provides the properties of broadcasting authenticated messages.

T. K. Srikanth and S. Toueg. Simulating authenticated broadcasts to derive simple fault-tolerant algorithms. *Distributed Computing* 2:(80-94), 1987.

# Authenticated broadcast

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Synchronous-round based

- $p$  broadcasts  $m$  in round  $k$ :  $broadcast(p, m, k)$
- process  $accept(p, m, k)$  when:
  - receives  $(p, m, k)$
  - verifies  $p$ 's signature.

*Correctness*: If correct  $p$  broadcasts  $(p, m, k)$  in round  $k$  then every correct process accepts  $(p, m, k)$  in the same round.

*Unforgeability*: If correct  $p$  does not broadcast  $(p, m, k)$  then no correct process ever accepts  $(p, m, k)$ .

*Relay*: If correct  $p$  accepts  $(p, m, k)$  in round  $r \geq k$ , then every correct process accepts  $(p, m, k)$  by round  $r + 1$ .

# Authenticated Arbitrary Consensus: I

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//  $m \in \{0, 1\}$ , non-loquacious protocol

process  $p$ :

if ( $p == p_1$ )  $value = m$ ;

else  $value = 0$ ;

for  $r = 1$  to  $t + 1$

if ( $value == 1$  and ( $p$  not broadcast in earlier round))

$broadcast(p, 1, r)$ ;

relay the  $r - 1$  messages accepted in rounds  $1, 2, \dots, r - 1$

that caused  $value$  to be set to 1;

if (in rounds  $r' \leq r$   $accepted(p_k, 1, r_k)$  from  $r$  distinct

processes  $p_k$  including the transmitter  $p_1$ )

$value = 1$ ;

decide  $value$ ;

# Authenticated Arbitrary Consensus: II

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## □ *Validity*

### ■ $m = 1$

□  $p_1$  sets *value* to 1 and broadcasts  $(p_1, 1, 1)$ .

□ By *Correctness* every correct process accepts  $(p_1, 1, 1)$  in round 1 and sets *value* to 1.

□ *value* is never set to another value, so decides *value*.

### ■ $m = 0$

□  $p_1$  sets *value* to 0 and does not broadcast in round 1.

□ Since *value* = 0,  $p_1$  never broadcasts in other rounds and decides on 0.

□ By *Unforgeability* no correct process ever accepts message from  $p_1$ .

□ Hence, no correct process sets *value* to 1, and so decides on 0.

# Authenticated Arbitrary Consensus: III

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## □ *Agreement*

- Some correct  $p$  first sets *value* to 1 at the end of round  $r < t + 1$ :
  - $p$  accepted messages  $(p_k, 1, r_k)$  from at least  $r$  distinct processes  $p_k$  including  $p_1$ .
  - In round  $r + 1$   $p$  broadcasts  $(p, 1, r + 1)$  and relays the  $r - 1$  messages that caused  $p$  to set *value* to 1.
  - By *Correctness* and *Relay*, in round  $r + 1$  all correct processes accept  $(p, 1, r + 1)$  and  $(p_k, 1, r_k)$  for  $1 \leq k \leq r$ , and so sets *value* to 1.
- Some correct  $p$  first sets *value* to 1 at the end of round  $t + 1$ :
  - $p$  accepted  $(p_k, 1, r_k)$  from  $t + 1$  distinct processes, and at least one must be correct. Say was  $p_i$  broadcasting  $(p_i, 1, r_i)$  where  $r_i \leq t + 1$ .
  - So  $p_i$  set *value* to 1 in round  $r_i - 1 < t + 1$ .
  - The first case above therefore holds.
- Otherwise, each correct process has *value* = 0 and decides 0.

# Simulating authenticated broadcast

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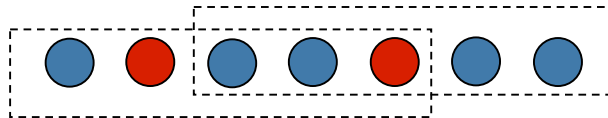
- Implement a broadcast primitive that provides *Correctness*, *Unforgeability*, and *Relay* without using cryptographic methods
  - To broadcast a message, a set of processes need to *witness* the broadcast.
  - A correct process accepts a message only when it knows that there are sufficient witnesses to this broadcast.
  - Doing so prevents a faulty process from claiming to have received a message that was not sent to it, and to allow a correct process to prove why it accepted a message.
  - Requires  $n > 3t$ .

# Handy Facts about $n > 3t$

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- Any subset of  $n - 2t$  processes contains at least one correct process.
  - $n - 2t > 3t - 2t = t$ .
- The intersection of any two subsets of  $n - t$  processes contains at least one correct process.
  - $n - t > 3t - t = 2t$ .

Example:  $n = 7, t = 2: n - 2t = 3, n - t = 5$ .



# Basic Idea

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- Each round consists of two phases.
- $p$  sends  $(init, p, m, k)$  to all.
- Any process that receives this message becomes a witness and sends  $(echo, p, m, k)$ .
- Any non-witness process that receives at least  $n - 2t$   $(echo, p, m, k)$  also becomes a witness and sends  $(echo, p, m, k)$ .
  - Because in any set of  $n - 2t$  processes, one must be correct.
- Any process that receives at least  $n - t$   $(echo, p, m, k)$  accepts the message.
  - Because at least  $n - 2t$  correct processes sent the echo, and so eventually all correct processes will echo.



# Broadcast primitive

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## Round $k$ :

*Phase  $2k - 1$* :  $p$  sends  $(init, p, m, k)$  to all;

*Phase  $2k$* : each process executes:

if received  $(init, p, m, k)$  from  $p$  in phase  $2k - 1$

send  $(echo, p, m, k)$  to all;

if received  $(echo, p, m, k)$  from at least  $n - t$  distinct processes in phase  $2k$

accept  $(p, m, k)$ ;

## Round $r > k$ :

*Phase  $2r - 1, 2r$* : each process executes:

if received  $(echo, p, m, k)$  from at least  $n - 2t$  distinct processes in previous phases

and not sent  $(echo, p, m, k)$

send  $(echo, p, m, k)$  to all;

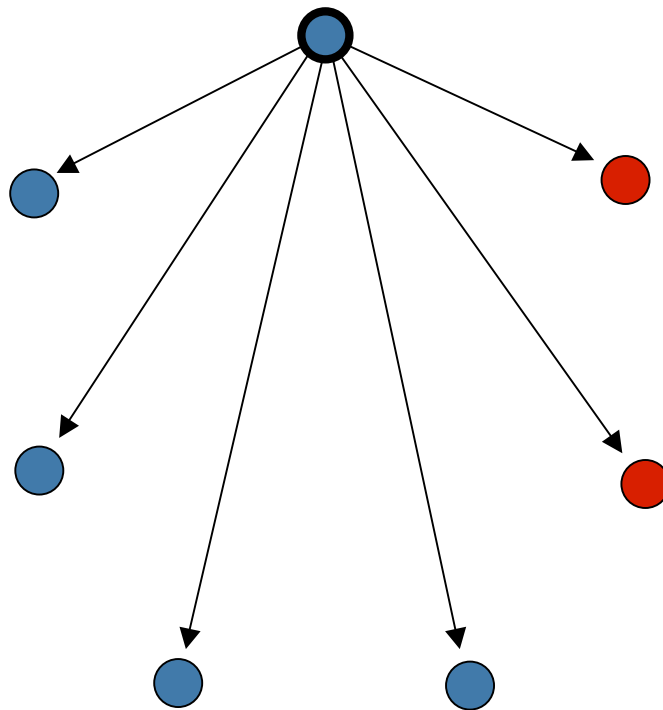
if received  $(echo, p, m, k)$  from at least  $n - t$  distinct processes in this and previous phases

accept  $(p, m, k)$ ;

# Correct process sends *init* in $2k - 1$

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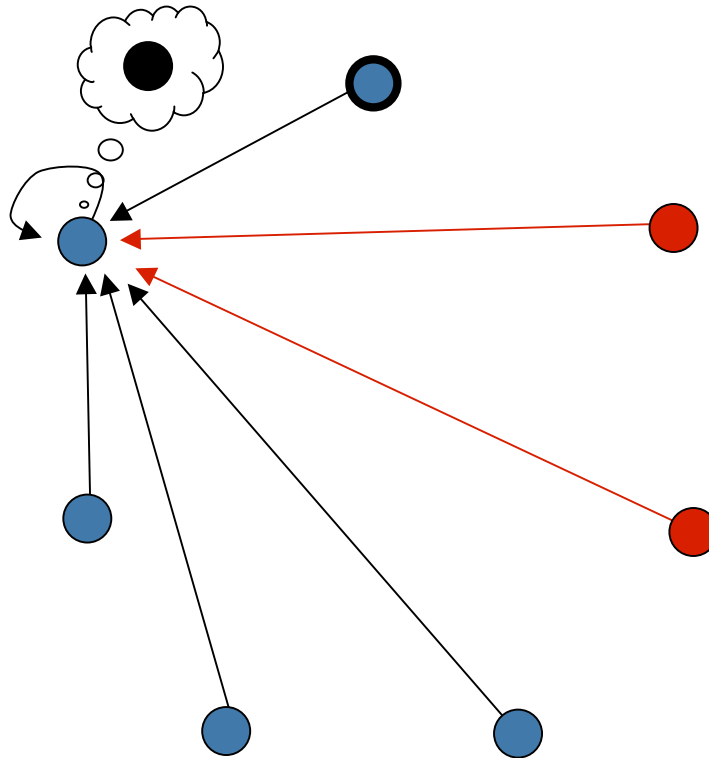
$n = 7, t = 2$   
 $n - t = 5$   
 $n - 2t = 3$



# Correct processes accept in $2k$

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$$\begin{aligned}n &= 7, t = 2 \\n - t &= 5 \\n - 2t &= 3\end{aligned}$$

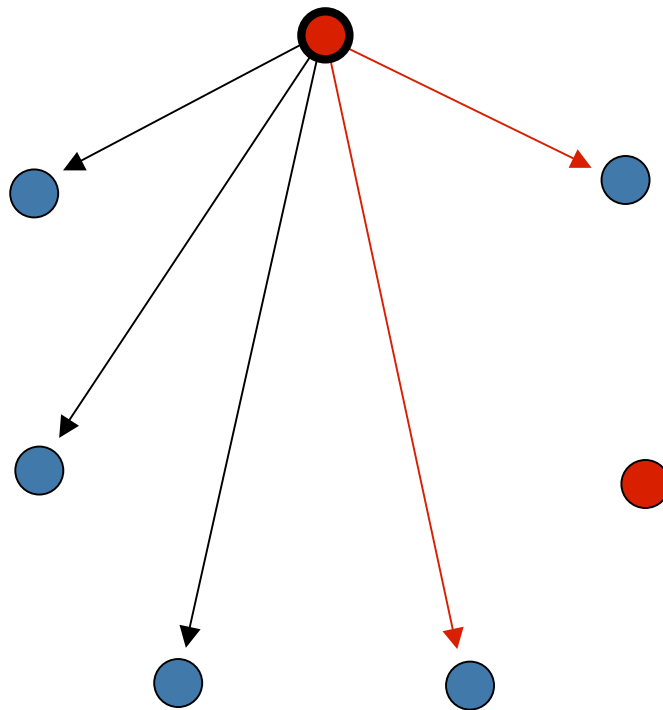


also *Unforgeability*: if correct  $p$  does not send  $(init, p, m, k)$  then each correct process will receive no more than  $t$   $(echo, p, m, k)$  messages. Since  $t < n - 2t$ , there will be no more witnesses.

# Faulty sends *init* in $2k - 1$

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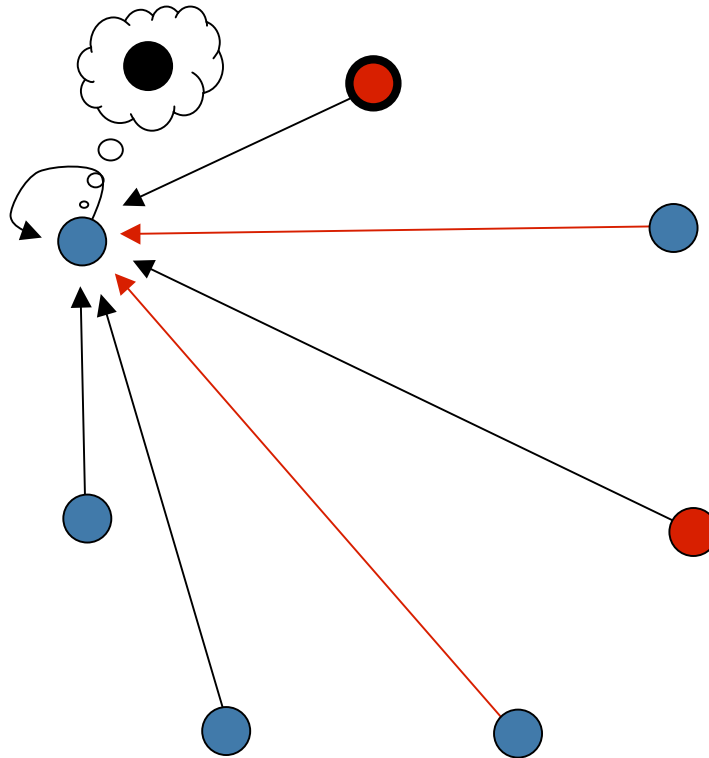
$n = 7, t = 2$   
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# Correct can behave differently in $2k$ : I

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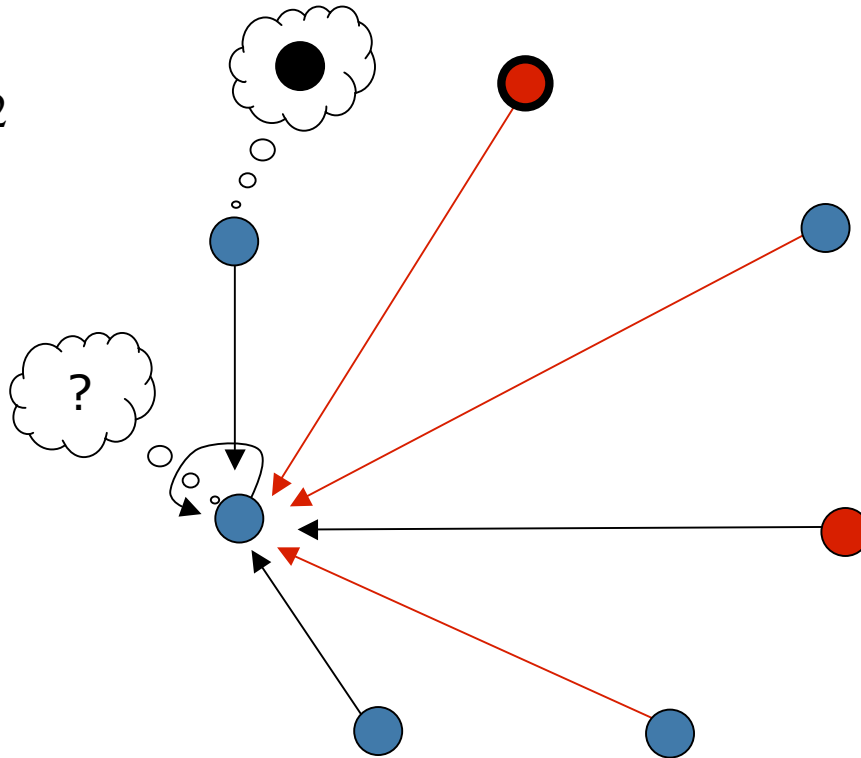
$n = 7, t = 2$   
 $n - t = 5$   
 $n - 2t = 3$



# Correct can behave differently in $2k$ : II

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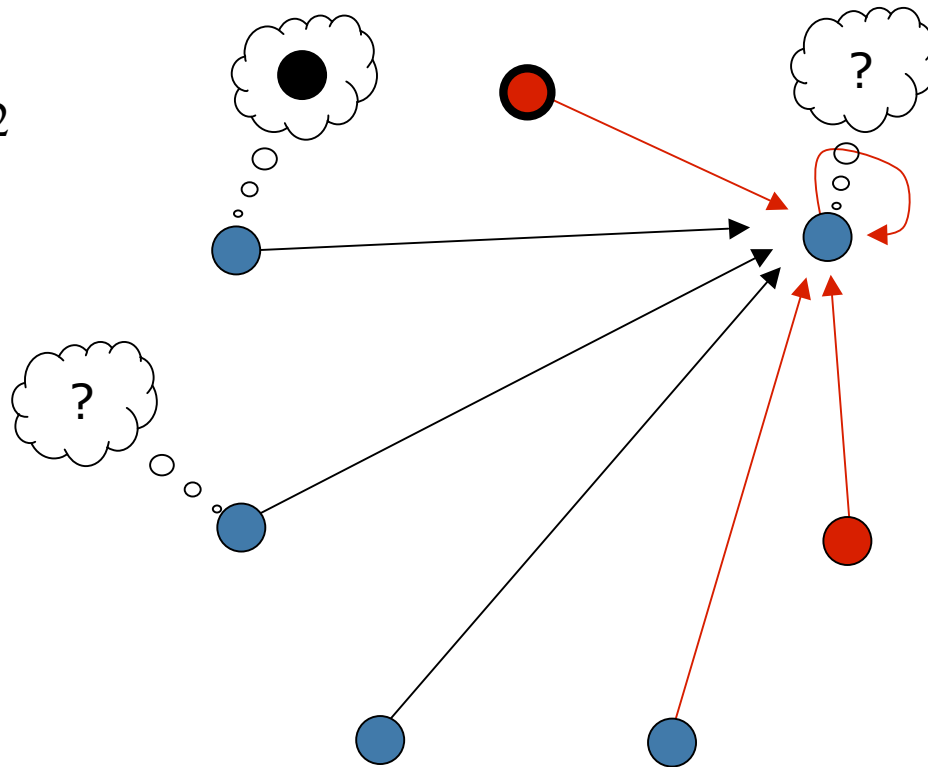
$n = 7, t = 2$   
 $n - t = 5$   
 $n - 2t = 3$



# Correct can behave differently in $2k$ : III

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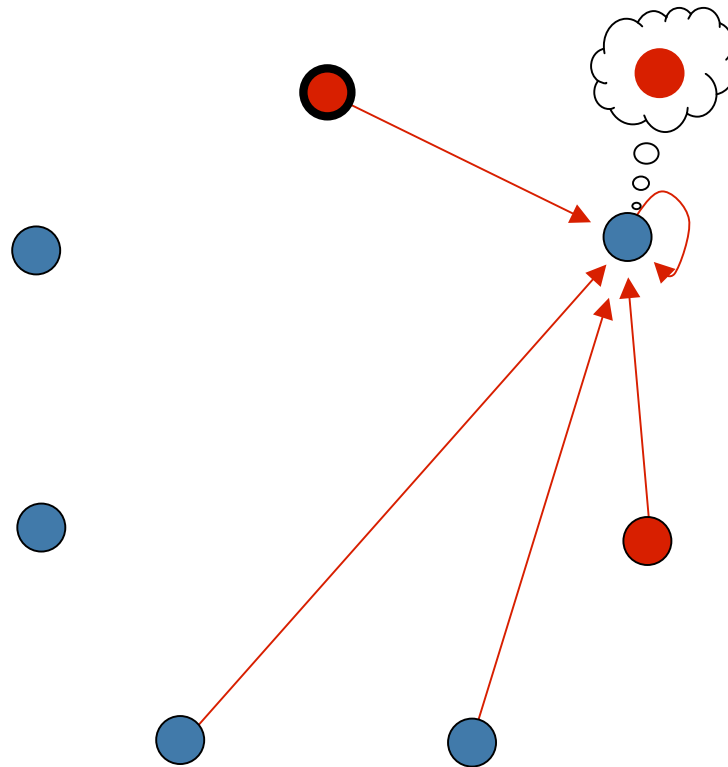
$n = 7, t = 2$   
 $n - t = 5$   
 $n - 2t = 3$



# Relay: phase $i$

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$$\begin{aligned}n &= 7, t = 2 \\n - t &= 5 \\n - 2t &= 3\end{aligned}$$

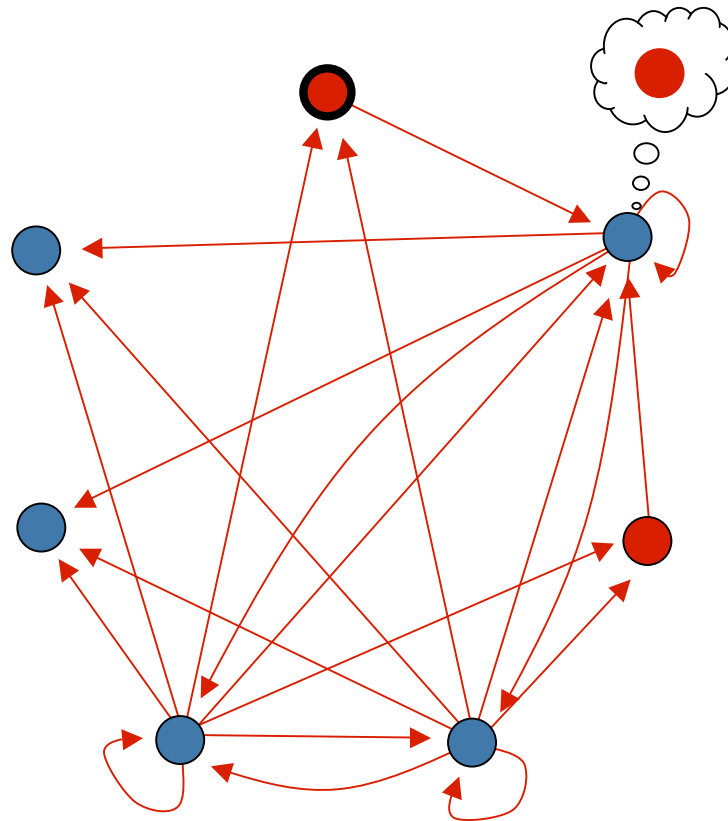




# Relay: phase $i$

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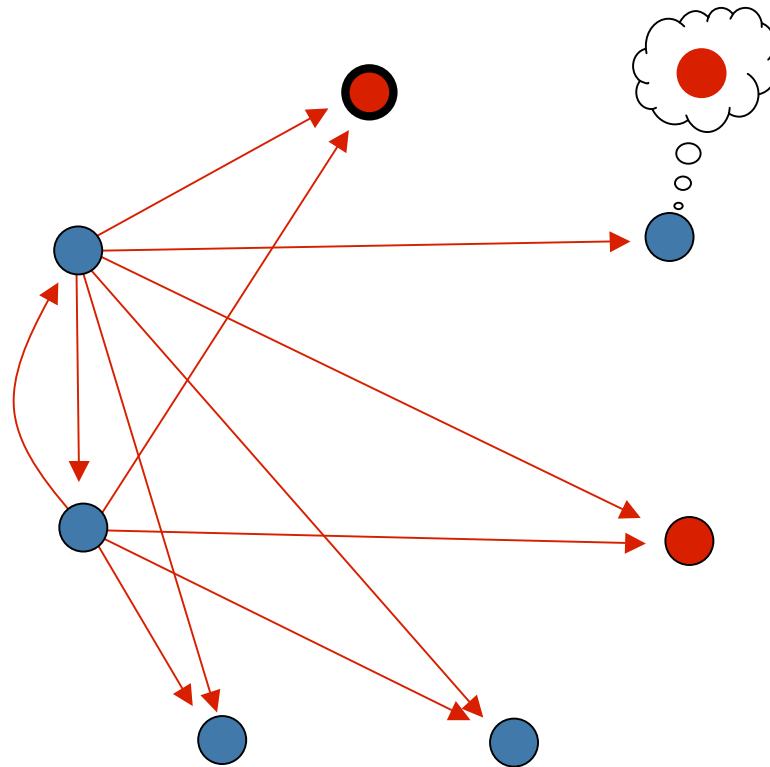
$$\begin{aligned}n &= 7, t = 2 \\n - t &= 5 \\n - 2t &= 3\end{aligned}$$



# Relay: phase $i + 1$

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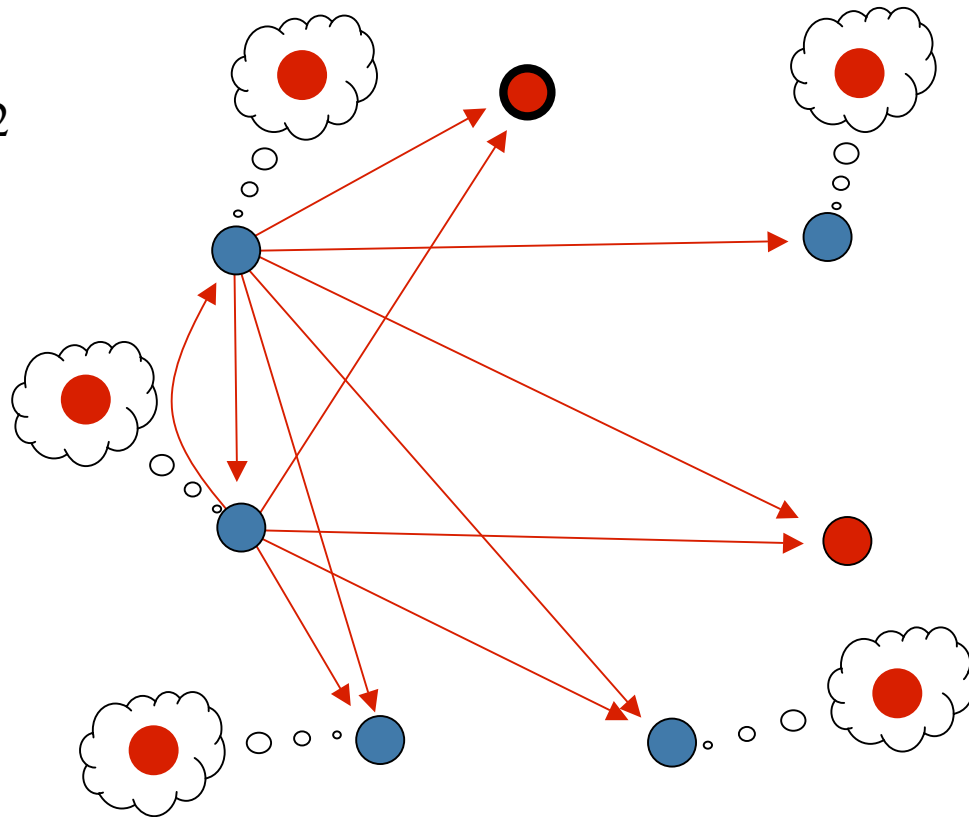
$n = 7, t = 2$   
 $n - t = 5$   
 $n - 2t = 3$



# Relay: phase $i + 1$

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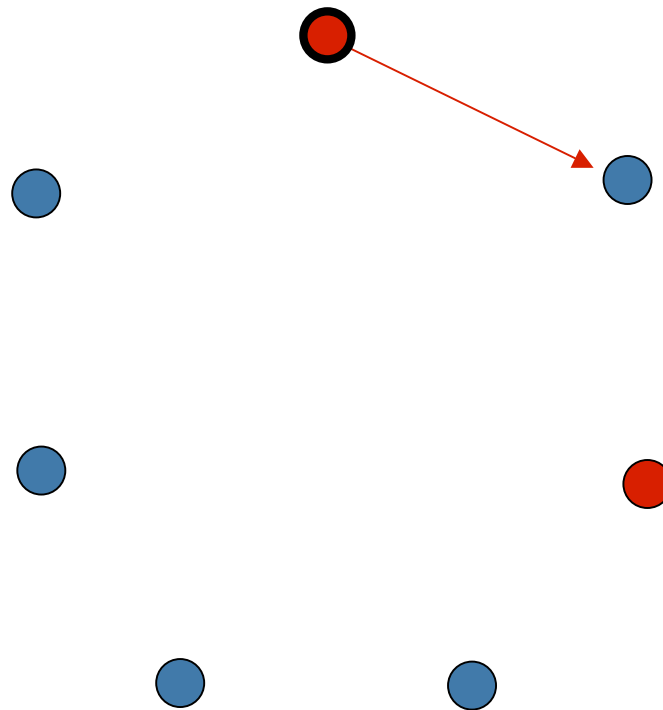
$n = 7, t = 2$   
 $n - t = 5$   
 $n - 2t = 3$



# Delaying accept arbitrarily long: $2k$

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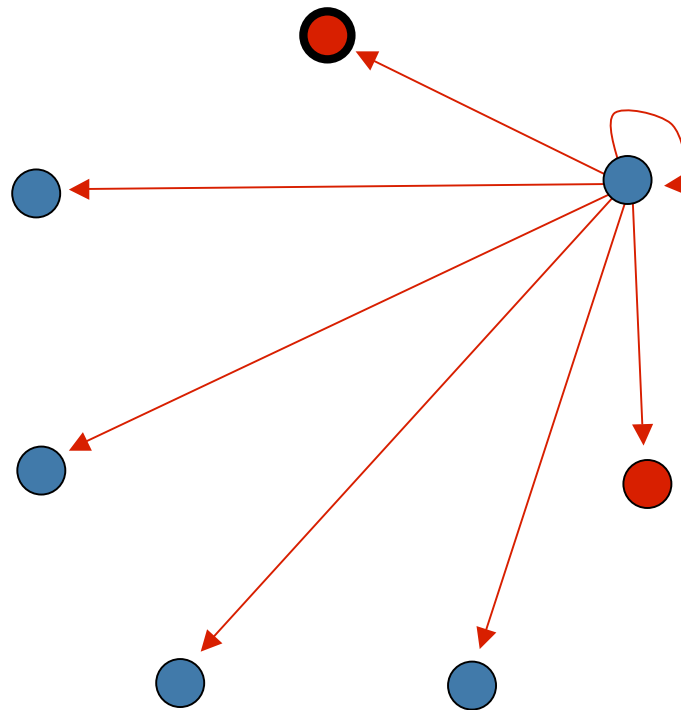
$n = 7, t = 2$   
 $n - t = 5$   
 $n - 2t = 3$



# Delaying accept arbitrarily long: $2k + 1$

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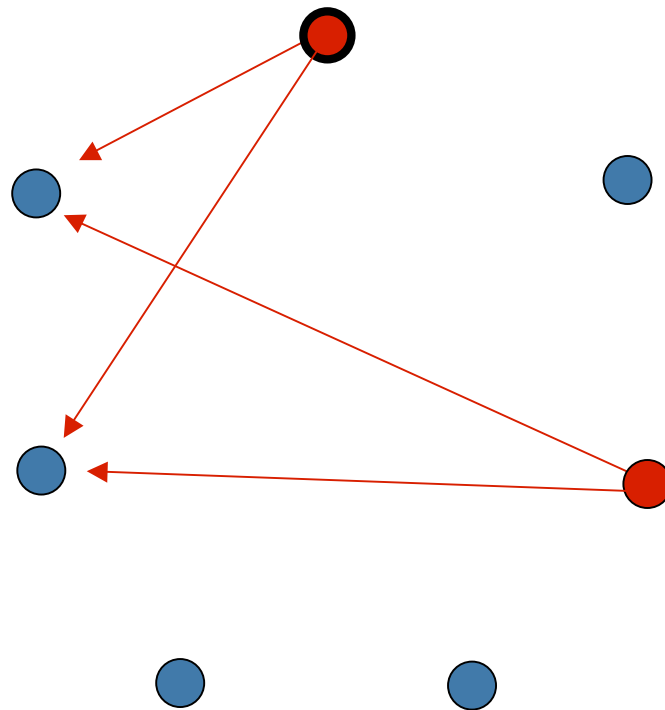
$n = 7, t = 2$   
 $n - t = 5$   
 $n - 2t = 3$



# Arbitrarily later... phase $i$

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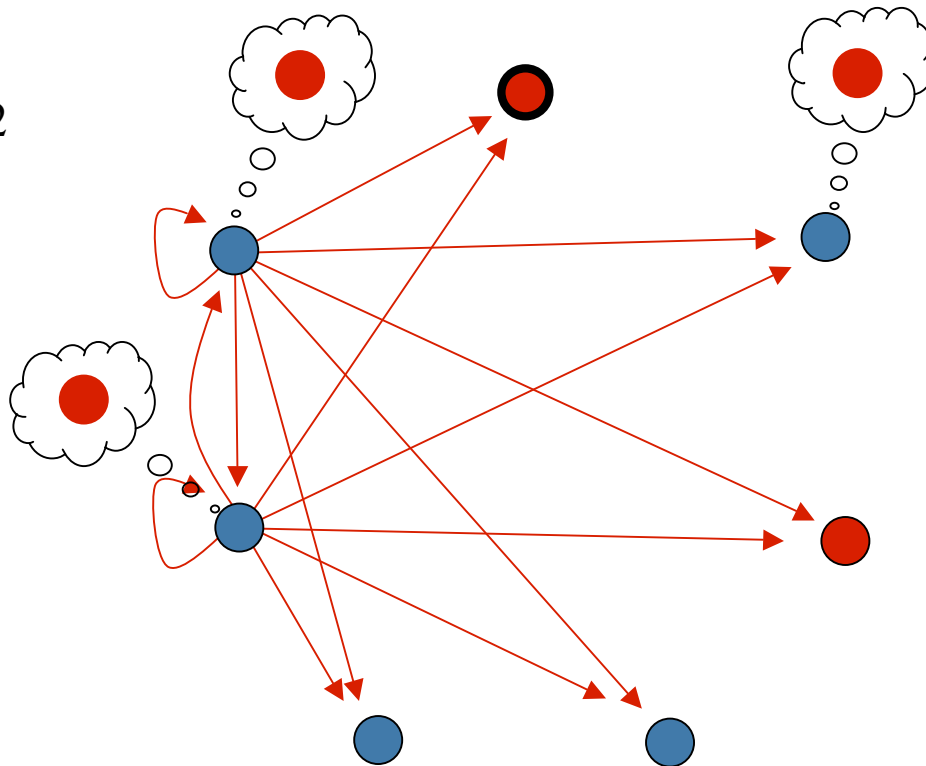
$n = 7, t = 2$   
 $n - t = 5$   
 $n - 2t = 3$



# Arbitrarily later... phase $i + 1$

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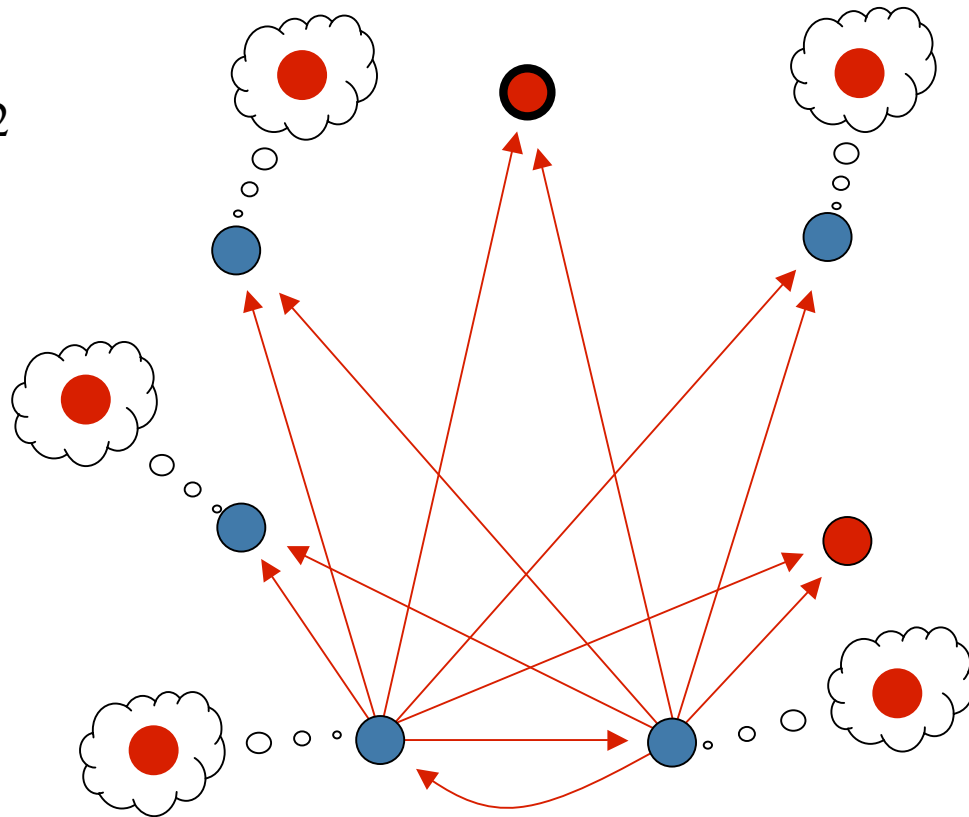
$n = 7, t = 2$   
 $n - t = 5$   
 $n - 2t = 3$



# Arbitrarily later... phase $i + 2$

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$n = 7, t = 2$   
 $n - t = 5$   
 $n - 2t = 3$





# Nonauthenticated Arbitrary Consensus

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//  $m \in \{0, 1\}$ , nonloquacious protocol

process  $p$ :

if ( $p == p_1$ )  $value = m$ ;

else  $value = 0$ ;

for  $r = 1$  to  $t + 1$

if ( $value == 1$  and ( $p$  not broadcast in earlier round))

**broadcast**( $p, 1, r$ );

if (in rounds  $r' \leq r$  *accepted* ( $p_k, 1, r_k$ ) from  $r$  distinct processes  $p_k$  including the transmitter  $p_1$ )

$value = 1$ ;

decide  $value$ ;

# Other results from this approach

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- Multivalued agreement
- Voting
- Asynchronous randomized agreement
- Clock synchronization