

# CSE107: Intro to Modern Cryptography

<https://cseweb.ucsd.edu/classes/sp22/cse107-a/>

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# Lecture 14a

## PKI and session-key exchange

Public Key Infrastructure (PKI)

Session key exchange

# Plan

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Public Key Infrastructure (PKI)

Session key exchange

## The public key setting

Bob's secret key is  $sk[B]$  and its associated public key is  $pk[B]$ . The public key setting **assumes** Alice is in possession of  $pk[B]$ .

$A^{pk[B]}$



$$C \stackrel{\$}{\leftarrow} \mathcal{E}_{pk[B]}(M) \xrightarrow{C} M \leftarrow \mathcal{D}_{sk[B]}(C)$$

$B$



$$\mathcal{V}_{pk[B]}(M, \sigma) \xleftarrow{M, \sigma} \sigma \stackrel{\$}{\leftarrow} \mathcal{S}_{sk[B]}(M)$$

Now Alice can encrypt a message  $M$  under  $pk[B]$  to get a ciphertext  $C$  that B can decrypt using  $sk[B]$ .

Bob can sign a message  $M$  using  $sk[B]$  to get signature  $\sigma$  that Alice can verify using  $pk[B]$ .

But how does Alice get  $pk[B]$ ?

## But who exactly are Alice and Bob?

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Typically, as in most uses of TLS, Bob is a server. Its identity  $B$  is an associated domain name or ip address, for example  $B = \text{google.com}$ .

Alice is a client, also with an associated ip address.

## How does $A$ get $B$ 's public key?

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**How about:**  $B$  runs a prescribed key-generation algorithm  $\mathcal{K}$  to generate  $(pk[B], sk[B])$ . It sends  $(B, pk[B])$  to  $A$ .



$\longleftarrow B, pk[B]$

$(pk[B], sk[B]) \xleftarrow{\$} \mathcal{K}$



# Entity-in-the-middle attack

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A



$\xleftarrow{B, pk[E]} (pk[E], sk[E]) \xleftarrow{\$} \mathcal{K}$

Adversary E



# Entity-in-the-middle attack

A



Adversary  $E$



$$\xleftarrow{B, pk[E]} \quad (pk[E], sk[E]) \xleftarrow{\$} \mathcal{K}$$

So:

$$C \xleftarrow{\$} \mathcal{E}_{pk[E]}(M) \quad \xrightarrow{C} \quad M \leftarrow \mathcal{D}_{sk[E]}(C)$$

$$\mathcal{V}_{pk[E]}(M, \sigma) \xleftarrow{M, \sigma} \quad \sigma \xleftarrow{\$} \mathcal{S}_{sk[E]}(M)$$

Adversary  $E$  can decrypt ciphertexts intended for  $B$  and can forge  $B$ 's signatures. Adversary effectively becomes  $B$ .



## PKI, CAs and certificates

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**Goal:**  $A$  gets an **authentic** copy of  $B$ 's public key, meaning if  $pk$  claims to come from  $B$ , then  $A$  has a proof to that effect.

**Popular Solution:** The PKI (Public Key Infrastructure).

**Certificate authority:** Trusted entity that provides the above proof.

**Certificate:** The proof

**Note:** There are other ways to reach the goal:  $B$  could post its public key on its Facebook; post it on its personal or corporate webpage; include it as an attachment in its emails; put it on a keyserver like openpgp SKS; hand it to  $A$  in person; ... (what do you think of these methods?)

# Let's Encrypt



The image shows a screenshot of the Let's Encrypt website. At the top, the browser address bar displays "https://letsencrypt.org". The website header includes the Let's Encrypt logo (a padlock with a sunburst) and the text "Let's Encrypt". To the right of the logo is the navigation menu with links for "Documentation", "Get Help", "Donate", "About Us", and "Languages". Above the navigation menu, it says "LINUX FOUNDATION COLLABORATIVE PROJECTS". The main content area features a large banner with a geometric, low-poly background in shades of blue, green, and orange. The banner text reads: "Let's Encrypt is a **free, automated, and open** Certificate Authority." Below this text are two buttons: "Get Started" and "Sponsor".

## Some other certificate authorities

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Rank	Issuer	Usage	Market share
1	<a href="#">IdenTrust</a>	20.4%	39.7%
2	<a href="#">Comodo</a>	17.9%	34.9%
3	<a href="#">DigiCert</a>	6.3%	12.3%
4	<a href="#">GoDaddy</a>	3.7%	7.2%
5	<a href="#">GlobalSign</a>	1.8%	3.5%
6	Certum	0.4%	0.7%
7	Actalis	0.2%	0.3%
8	<a href="#">Entrust</a>	0.2%	0.3%
9	<a href="#">Secom</a>	0.1%	0.3%
10	<a href="#">Let's Encrypt</a>	0.1%	0.2%
11	<a href="#">Trustwave</a>	0.1%	0.1%
12	WiSeKey Group	< 0.1%	0.1%
13	<a href="#">StartCom</a>	< 0.1%	0.1%
14	<a href="#">Network Solutions</a>	< 0.1%	0.1%

# Certificate process

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- $B$  generates  $(pk, sk) \xleftarrow{\$} \mathcal{K}$  by running a key-generation algorithm  $\mathcal{K}$
- $B$  sends its identity  $B$ , and  $pk$ , to CA
- CA does identity check to ensure  $pk$  is  $B$ 's
- $B$  proves knowledge of  $sk$  to CA
- CA issues certificate to  $B$
- $B$  sends certificate to  $A$
- $A$  verifies certificate and extracts  $B$ 's public key  $pk$

# RSA Key generation with openssl

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Generate a 3072-bit RSA key, output it to key.pem:

```
$ openssl genrsa -out key.pem 3072
Generating RSA private key, 3072 bit long modulus (2 primes)
.....++++
.....++++
e is 65537 (0x010001)
```

Extract the public key from the key pair, which can be used in a certificate

```
$ openssl rsa -in key.pem -outform PEM -pubout -out public.pem
writing RSA key
```

## EC Key generation with openssl

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Generate an EC (256-bit) private key with the elliptic curve prime256v1, output it to key.pem:

```
$ openssl ecparam -name prime256v1 -genkey -noout -out key.pem
```

Extract the public key from the key pair, which can be used in a certificate

```
$ openssl ec -in key.pem -pubout -out public.pem
read EC key
writing EC key
```

## Checks

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$B$  sends its identity  $B$  (domain name, ip address, email address, ...) and its public key  $pk$  to the certificate authority (CA).

Upon receiving  $(B, pk)$  the CA performs some checks to ensure  $pk$  is really  $B$ 's key.

**Example:** If  $B$  is a domain name, then the CA sends  $B$  a challenge and checks that it can put it on the webpage of the domain name.

**Example:** If  $B$  is an email address, then the CA sends an email to that address with a link for  $B$  to click to verify that it owns the address.

**Example:** If  $B$  is a passport or driver's license, the CA may be able to verify it physically, out of band.

**Proof of knowledge of secret key:** The CA might have  $B$  sign or decrypt something under  $sk$  to ensure that  $B$  knows  $sk$ . This ensures  $B$  has not copied someone else's public key.

# In openssl: certificate requests

```
$ openssl req -newkey rsa:3072
Generating a RSA private key
.....++++
...++++
writing new private key to 'privkey.pem'
Enter PEM pass phrase:
Verifying - Enter PEM pass phrase:
[...]
Country Name (2 letter code) [AU]:
State or Province Name (full name) [Some-State]:
[...]
-----BEGIN CERTIFICATE REQUEST-----
MIIDijCCAf1CAQAwRTELMAkGA1UEBhMCQVUxEzARBgNVBAgMClNvbWUtU3RhdGUx
ITAfBgNVBAoMGEludGVybWV0IFdpZGdpdHMgUHR5IEExOZDCCAaIwDQYJKoZIhvcN
AQEBBQADggGPADCCAyoCggGBAMJx18YOINj9UwmMoFqj4/azaEOwG4DSmDl0Wp8u
ucOox9QQ20d7LI7cSZOMiXF7U50AQ16VwbdPdU14BCS1fG9vP23kgirz6T4Tu0cG
7Yj82Lwqoc0mhbhhdcPYooLbmxx6xu1/Qqhz+9eLYZmLfE+n7MzdmRxxrLeIwPFs
IHQHo1StyD02A2JbyA1VVB8GpXe2Jj+vRTT5pWc1Qq5DBTvhb4IOydekswb3hP6j
GoavlHATP1PostesQCuCGFzjAnInpxdePaNe11IMCqPQ2UiTlssg3KfbueAW0dzS
dl9cly0Dc1Dh3Emriv2mtrS+SBYN6VptTqc1Uu7DwzEOhbVQkFa10fPaNwafJTL0
j+4LBbcywEoHD9baA1ZRUR8ODn3SXsY4fTqXqSR2S5mEK1K7GoEmp917kg2mITRO
o8eoUbERDEWC1h6IHAw9C4u2M7fPbln46AtbbRAOpkbCBTi9IqtsPQvE67XiH3uX
1hvCPsUfrD9sYMMjTxg/fsKCUwIDAQABoAAwDQYJKoZIhvcNAQELBQADggGBAEbL
OBbMJQ6gXGSMGA7UWs7J4I2uZEo9YMzgrCLqxzi9Xuh7BU8JNkL4hD5XgtHAN6A
ZAEgWkP0TUbcLZBVRmiAU+nNH+ZgTicJ7ZJySSQnI+XCi3UsGTus6cpCudikuf9
HoTuil6CI7geUFR5U57o1CvbWfNPM+eOfZcVt3iUixwUrMrNliprMsJwQx703oR
9AohE13QtvJLJysk+XI6X4B9bmm+CJ/YyoMxG+BGNP/Oi5WgGyQMg0iKp4nhozC2
WzqxOe5ECmVzSguInF7hnIJT1UDUsEgwpjgMMZfA9L/NaZj7f4+KD309CjUbZzGw
9zVqjbcuM0weyMNzGTBLuuXvNQVpXPr5jRs8iVwFW+eQaaWAXQH40x75/DYMo3HH
NFm8drk+lhBzERwdHIHg7127x9epzfxkPwz1h1QMBooQKAqNLQ06c3DqvfrYda7z
q/IBpoZpM35PeqsYS8IUCceIjwYAM5GmpQZ4Fsb9VgW1bmK/fUBUf9TGJhUwQ==
-----END CERTIFICATE REQUEST-----
```

key + identity  
=  
certificate request



## In openssl: certificate requests

---

```
$ openssl req -newkey ec:<(openssl ecparam -name prime256v1)
Generating an EC private key
writing new private key to 'privkey.pem'
Enter PEM pass phrase:
Verifying - Enter PEM pass phrase:
[...]
Country Name (2 letter code) [AU]:
State or Province Name (full name) [Some-State]:
[...]
-----BEGIN CERTIFICATE REQUEST-----
MIH/MIGnAgEAMEUxCzAJBgNVBAYTAkFVMRMwEQYDVQQIDApTb211LVNOYXR1MSEw
HwYDVQQKDBhJbnR1cm51dCBXaWRnaXRzIFB0eSBMdGQwWTATBgckhkJOPQIBBggq
hkjOPQMBBwNCAASTLsJ/rKbthNWCo01RF300ZvCVZK0yS60TmJ0o01HL/PXWqL1D
fLNPTGEmuEvdD8Ikch7INzfkz3VE00AYsbHZoAAwCgYIKoZIzj0EAwIDRwAwRAIg
ZzQRe1h42I60l azt+qn2ymx20qe81kJraCEtAkBmp4ICIA6kAIL9wBnB1pk2+v73
L1cNOE9k+eFszl89yVJSaazG
-----END CERTIFICATE REQUEST-----
```

key + identity  
=  
certificate request

Elliptic curve keys and certificate requests are shorter than for RSA, because the DLog problem is very hard on elliptic curves, and 256-bit keys are safe enough.

# Certificate Issuance

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Once CA is convinced that  $pk$  belongs to  $B$ , it forms a certificate

$$\text{CERT}[B] = (\text{CERTDATA}, \sigma),$$

where  $\sigma$  is the CA's signature on CERTDATA, computed under the CA's secret key  $sk[\text{CA}]$ , and CERTDATA contains:

- $B$ 's public key  $pk$ , and its type (RSA, EC, ...)
- Identity  $B$  of  $B$
- Name of CA
- Expiry date of certificate
- ...

The certificate  $\text{CERT}[B]$  is returned to  $B$ .

## Certificate usage

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$B$  can send  $\text{CERT}[B]$  to  $A$ , who is assumed to have the CA's public key  $pk[\text{CA}]$ , and now will:

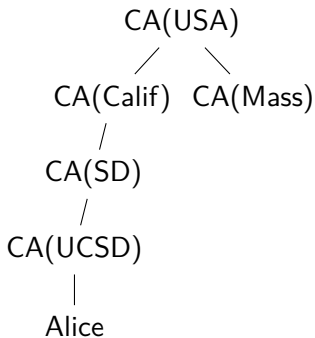
- Parse  $\text{CERT}[B]$  as  $(\text{CERTDATA}, \sigma) \leftarrow \text{CERT}[B]$
- Check that  $\mathcal{V}_{pk[\text{CA}]}(\text{CERTDATA}, \sigma) = 1$
- Extract  $(pk, B, \text{expiry}, \dots) \leftarrow \text{CERTDATA}$
- Check certificate has not expired
- Check that  $B$  is the desired identity
- ...

If all is well,  $A$  accepts the certificate and is ready to use the public key  $pk$  therein.

**How does  $A$  get  $pk[\text{CA}]$ ?** CA public keys are embedded in software such as your browser, or, on Apple, in the keychain.

## Certificate hierarchies

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CERT[Alice]

CERT[CA(USA) : CA(Calif)]

CERT[CA(Calif) : CA(SD)]

CERT[CA(SD) : CA(UCSD)]

CERT[CA(UCSD) : Alice]

$\text{CERT}[X : Y] = ((pk[Y], Y, \dots), \mathcal{S}_{sk[X]}((pk[Y], Y, \dots)))$

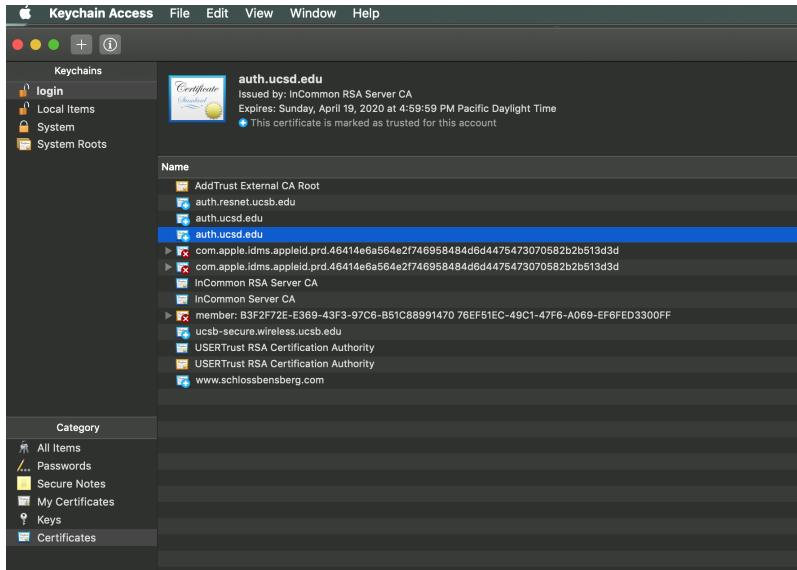
To verify CERT[Alice] you need only  $pk[CA[USA]]$ .

## Why certificate hierarchies?

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- It is easier for CA(UCSD) to check Alice's identity (and issue a certificate) than for CA(USA) since Alice is on UCSD's payroll and UCSD already has a lot of information about her.
- Spreads the identity-check and certification job to reduce work for individual CAs
- Browsers need to have fewer embedded public keys. (Only root CA public keys needed.)

# Certificates on Mac: keychain



# A particular certificate



 **auth.ucsd.edu**  
Issued by: InCommon RSA Server CA  
Expires: Sunday, April 19, 2020 at 4:59:59 PM Pacific Daylight Time  
• This certificate is marked as trusted for this account

▶ Trust

▼ Details

**Subject Name**

Country or Region	US
Postal Code	92093
State/Province	CA
Locality	La Jolla
Street Address	9500 Gilman Drive
Organization	University of California, San Diego
Organizational Unit	UCSD
Common Name	auth.ucsd.edu

**Issuer Name**

Country or Region	US
State/Province	Mi
Locality	Ann Arbor
Organization	Internet2
Organizational Unit	InCommon
Common Name	InCommon RSA Server CA

**Serial Number** 00 B1 28 07 A2 0D 08 E2 27 6E A0 9C 97 47 D0 DF 87  
**Version** 3

**Signature Algorithm** SHA-256 with RSA Encryption ( 1.2.840.113549.1.1.1 )  
**Parameters** None

**Not Valid Before** Thursday, April 19, 2018 at 5:00:00 PM Pacific Daylight Time  
**Not Valid After** Sunday, April 19, 2020 at 4:59:59 PM Pacific Daylight Time

**Public Key Info**

Algorithm	RSA Encryption ( 1.2.840.113549.1.1.1 )
Parameters	None
Public Key	256 bytes : C4 AD 44 82 D1 A1 84 0F ...
Exponent	65537
Key Size	2,048 bits
Key Usage	Encrypt, Verify, Wrap, Derive
Signature	256 bytes : 41 01 7D F8 D1 B0 AC E8 ...

**Extension** Key Usage ( 2.5.29.15 )  
**Critical** YES  
**Usage** Digital Signature, Key Encipherment

# Revocation

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Suppose  $B$  wishes to revoke its certificate  $\text{CERT}[B] = (\text{CERTDATA}, \sigma)$ , perhaps because its secret key  $sk$ , corresponding to the  $pk$  in  $\text{CERTDATA}$ , was compromised. Then:

- $B$  sends  $\text{CERT}[B]$  and revocation request to CA, signed under  $sk$
- CA verifies the signature under  $pk$
- CA puts  $(\text{CERT}[B], \text{RevocationDate})$  on its Certificate Revocation List (CRL)
- This list is disseminated.

Before  $A$  accepts  $B$ 's certificate,  $A$  should check that it is not on the CRL.

The OCSP (Online Certificate Status Protocol) is one way to do this.



# Revocation Issues

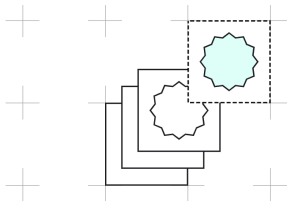
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- May 13:  $B$ 's secret key compromised
- May 16:  $B$ 's  $\text{CERT}[B]$  revoked
- May 17:  $A$  sees CRL

$\text{CERT}[B]$  might be used in the May 13-16 range, compromising security.

In practice, CRLs are large and revocation is a problem.

# Certificate transparency (link)



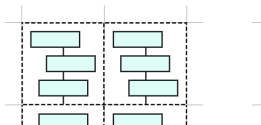
## Who watches the watchers?

Historically, user agents determined if CAs were trustworthy through audits by credentialed third parties. But these tended to look at operational practices and historical performance rather than technical correctness. Such audits can't catch everything. Before CT, there could be a significant time lag between a certificate being wrongly issued, and a CA doing something about it.

That's where  
**Certificate Transparency**  
comes in.

## Independent, reliable logs

CT depends on independent, reliable logs because it is a distributed ecosystem. Built using Merkle trees, logs are publicly verifiable, append-only, and tamper-proof.



# PGP SKS keyserver

## SKS OpenPGP Key server

### Extract a key

You can find a key by typing in some words that appear in the userid (name, email, etc.) of the key you're looking for, or by typing in the keyid in hex format ("0x...")

Search for a public key

String

Show PGP Fingerprints

Show SKS full-key hashes

Get regular index of matching keys

Get verbose index of matching keys

Retrieve ascii-armored keys

Retrieve keys by full-key hash

### Submit a key

You can submit a key by simply pasting in the ASCII-armored version of your key and clicking on submit.

[SKS](#) is a new [OpenPGP](#) keyserver. The main innovation of SKS is that it includes a highly-efficient reconciliation algorithm for keeping the keyserver synchronized.

[SKS statistics](#)

# Plan

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Public Key Infrastructure (PKI)

Session key exchange

## Session key exchange

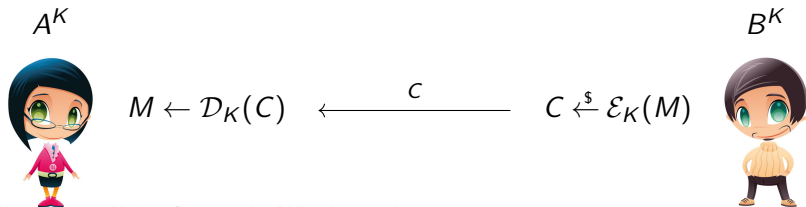
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A large part of secure communication over the Internet is through protocols like TLS (<https>).

Here, public-key cryptography is not used to directly secure data.

Rather, public-key cryptography is used in a *session-key exchange* that provides (client)  $A$  and (server)  $B$  with a shared (symmetric) *session key*  $K$ .

Data is then secured under  $K$  using an authenticated encryption scheme  $\mathcal{AE} = (\mathcal{K}, \mathcal{E}, \mathcal{D})$ :



## Session key exchange

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Why session keys, as opposed to directly securing data with public-key cryptography?

- One reason is performance: symmetric cryptography is more efficient than asymmetric cryptography.

We mentioned that as one of the arguments in favor of hybrid encryption.

- More fundamentally, it reflects the Internet architecture in which  $A$  and  $B$  will engage in multiple, sometimes concurrent communication sessions.

The session key exchange paradigm gives each such session a *fresh* session key, making its security independent of that of other sessions.

## Recall Diffie-Hellman Key Exchange

Let  $G = \langle g \rangle$  be a cyclic group of order  $m$  in which the CDH problem is hard. Let  $\mathbf{H}: \{0, 1\}^* \rightarrow \{0, 1\}^k$  be a hash function.



$$x \xleftarrow{\$} \mathbb{Z}_m; X \leftarrow g^x \xrightarrow{A, X}$$
$$L \leftarrow Y^x \xleftarrow{B, Y}$$

$$y \xleftarrow{\$} \mathbb{Z}_m; Y \leftarrow g^y$$
$$L \leftarrow X^y$$



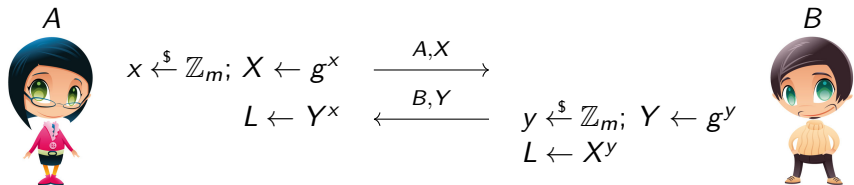
$$Y^x = (g^y)^x = \underbrace{g^{xy}}_L = (g^x)^y = X^y$$

This enables  $A$  and  $B$  to agree on the common  $k$ -bit key  $K = \mathbf{H}(L) = \mathbf{H}(g^{xy})$ .

So is this a suitable session key exchange protocol? Are we done?

# DH Key Exchange is secure under Passive Attack

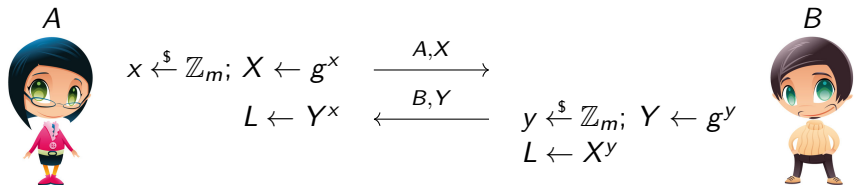
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A passive adversary is one that observes the communication, acquiring  $X = g^x$  and  $Y = g^y$ , and wants to compute  $K = H(g^{xy})$ . But to do so requires solving the CDH problem, which is here assumed hard.



# DH Key Exchange is secure under Passive Attack

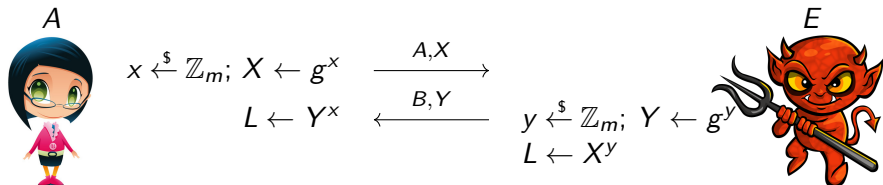


A passive adversary is one that observes the communication, acquiring  $X = g^x$  and  $Y = g^y$ , and wants to compute  $K = H(g^{xy})$ . But to do so requires solving the CDH problem, which is here assumed hard.

However, the problem of **authenticity** remains (recall that KEMs assumed authenticity of  $ek$ ! ( $ek$  = the public key)).

# DH Key Exchange is insecure under Active Attack

Entity-in-the-middle attack:



- Adversary  $E$  impersonates  $B$ .
- $A$  thinks it shares  $K = \mathbf{H}(L)$  with  $B$ , but in fact  $A$  shares  $K$  with  $E$ .

If  $A$  now encrypts, under  $K$ , a message intended for  $B$ , then  $E$  can decrypt the ciphertext and recover the message.

DH in itself does not solve the session key exchange problem.

## Session key exchange requirements

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We consider the unilateral, public-key setting. Here  $B$  has a certificate  $\text{CERT}[B]$  and corresponding public and secret keys  $pk[B], sk[B]$ .  $A$  is not assumed to have a certificate or corresponding keys.

This is the most common setting for TLS, where  $B$  is a server like `google.com` and  $A$  is a client.

The session key exchange should result in a session key  $K$ , known to both  $A$  and  $B$ , and satisfying:

- Authenticity:  $A$  really shares  $K$  with  $B$ , not some other entity
- Secrecy: The adversary does not know  $K$ .

This must hold even if the adversary knows session keys of other sessions and is active, meaning in complete control of the communication.

These basic requirements are supplemented by various others including forward secrecy, anonymity, ...

## Session key exchange secrecy

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Secrecy: The adversary  $E$  cannot distinguish the true session key  $K$  from a random string of the same length.

Suppose the protocol terminates and a party  $X$  outputs a session key  $K$ . Now we let

$K_1 \leftarrow K$ ;  $K_0 \xleftarrow{\$} \{0, 1\}^{|K|}$ ; game returns  $K_0$  or  $K_1$ . Adversary must tell which.

Then the adversary's advantage should be small.

This must hold even if the adversary has obtained the session key of all other instances except the one partnered with  $X$ , and when the adversary is active, in charge of all communication.

Warning: This is not a formal definition, just a glimpse of it. The IND-CCA notion for KEMs comes closer.

## Session key exchange landscape

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Session-key exchange is a subtle problem.

Easy to specify protocols, hard to get them right. One very hard aspect is that an active adversary may have multiple concurrent sessions.

Many security requirements, many proposed protocols, many attacks.

Definitions and provable security treatment started in the mid 1990s and continued well into the 2000s.

Today, standards look for proof-based support.

The TLS 1.3 session key exchange protocol is based on the Sigma (sign-and-mac) protocol of [Kr03].

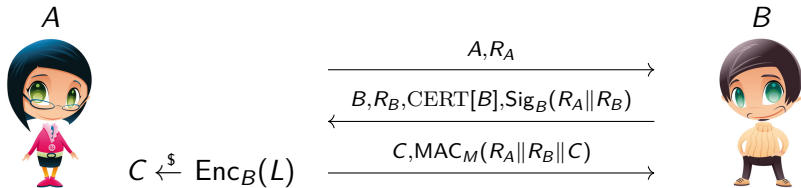
# Plan

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Session key exchange

Key exchange protocols

# Protocol KE1



$R_A, R_B$ , called *nonces*, are randomly chosen by the parties.

$\text{Sig}_B(X)$  is  $B$ 's signature on  $X$ , computed under  $sk[B]$  and verifiable under the  $pk[B]$  that is in  $\text{CERT}[B]$ .

$L$  is randomly chosen by  $A$ . Session key is  $K = \mathbf{H}_1(L)$  and MAC key is  $M = \mathbf{H}_2(L)$  where  $\mathbf{H}_1, \mathbf{H}_2$  are public hash functions.

$\text{Enc}_B(L)$  is encryption of  $L$  under  $B$ 's public key  $pk[B]$ . Decryption uses  $sk[B]$ .

# Identity mis-binding attack on KE1



A accepts B and thinks it shares  $K$  with B.

But B accepts E and thinks it shares  $K$  with E.

This is viewed as a problem, even though E does not know  $K$ , because there is a mis-binding of identities.

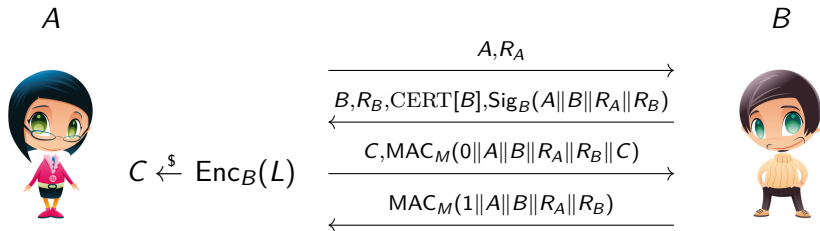
A good definition would view this as a successful attack.

A good protocol should ensure that if A accepts B with  $K$ , then B either accepts A with  $K$ , or accepts nobody with  $K$  or a key related to  $K$ .



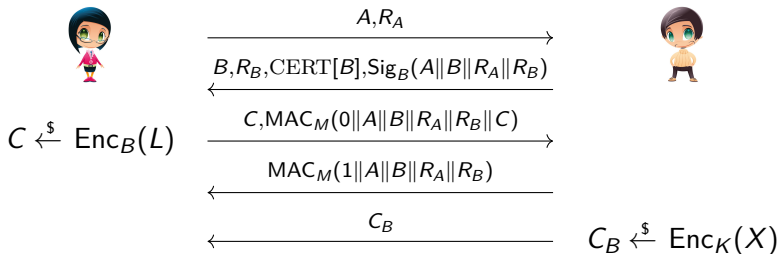
## Protocol KE2

Identity mis-binding is circumvented by inclusion of identities in the signature and the MAC, and addition of a MAC from the server:



Session key is  $K = \mathbf{H}_1(A\|B\|R_A\|R_B\|L)$  and MAC key is  $M = \mathbf{H}_2(A\|B\|R_A\|R_B\|L)$ .

## KE2 is not forward secure



Apr. 17: Adversary  $E$  records above flows.

May. 13:  $E$  compromises  $B$ 's system and obtains  $sk[B]$

May. 17:  $B$  revokes  $\text{CERT}[B]$ , and thus  $pk[B]$

However, at any time after May. 13,  $E$  can obtain session key  $K$  and decrypt  $C_B$  to obtain  $X$  via:  $K \leftarrow \text{Dec}_{sk[B]}(C)$  ;  $X \leftarrow \text{Dec}_K(C_B)$ .

This is a violation of what's called **forward secrecy**.

# Forward secrecy

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## Definition (Forward Secrecy)

**Forward secrecy** asks that exposure of  $sk[B]$  does not allow recovery of session keys  $K$  exchanged prior to the time of exposure.

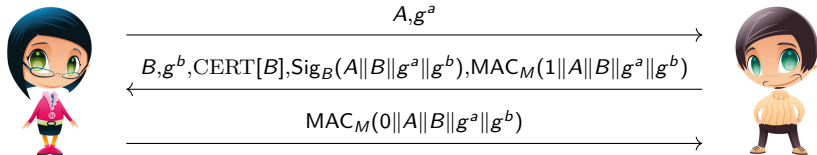
FS is achieved using the DH key exchange inside the session key exchange protocol.

Forward secrecy is considered **necessary** in modern session key exchange, and is present in the TLS 1.3 protocol.

Session-key exchange protocols using DH for forward secrecy are often called authenticated DH key exchange protocols.

## Protocol KE3

Let  $G = \langle g \rangle$  be a cyclic group of order  $m$  in which the CDH problem is hard.



Here  $a, b \xleftarrow{\$} \mathbb{Z}_m$  are chosen by  $A, B$ , respectively, and  $g^a, g^b$  play the role of nonces.

$\text{Sig}_B(X)$  is  $B$ 's signature on  $X$ , computed under  $sk[B]$  and verifiable under the  $pk[B]$  that is in  $\text{CERT}[B]$ .

Let  $L = g^{ab}$  be the DH key. Then session key is  $K = \mathbf{H}_1(A\|B\|g^a\|g^b\|L)$  and MAC key is  $M = \mathbf{H}_2(A\|B\|g^a\|g^b\|L)$  where  $\mathbf{H}_1, \mathbf{H}_2$  are as before.

## Protocol KE3



$A, g^a$

$B, g^b, \text{CERT}[B], \text{Sig}_B(A\|B\|g^a\|g^b), \text{MAC}_M(1\|A\|B\|g^a\|g^b)$

$\text{MAC}_M(0\|A\|B\|g^a\|g^b)$



There is no public-key encryption used here, only signatures.

Compromise of  $sk[B]$  only gives  $E$  the ability to forge signatures. Even given  $sk[B]$ , it cannot recover the DH key  $L = g^{ab}$  from a prior exchange, and thus cannot distinguish from random the session key  $K = \mathbf{H}_1(A\|B\|g^a\|g^b\|L)$ .

Accordingly this provides forward secrecy.

This is roughly the core of the unilateral session-key exchange in the TLS 1.3 handshake.