

CSE 105

THEORY OF COMPUTATION

Spring 2018 Exam 1 review class

Today's learning goals

- Summarize key concepts, ideas, themes from Chapter 1.
- Approach your exam studying with confidence.
- Identify areas to focus on while studying for the exam.

Reminders

- Seat map & study guide on Piazza.
 - Review session tonight will go over practice questions.
- Please arrive early & put backpacks near front of room.
- Index card with handwritten notes ok.

Roadmap of examples

- A. Regular language: design
- B. Transforming machines
- C. Proving nonregularity

Given L , prove it is regular

Construction

Strategy 1: Construct DFA

Strategy 2: Construct NFA

Strategy 3: Construct regular expression

Proof of correctness

WTS 1 if w is in L then w is accepted by

WTS 2 if w is not in L then w is rejected by ...

$L = \{ w \text{ in } \{0,1\}^* \mid w \text{ has exactly one } 0 \text{ and an even number of } 1\text{s} \}$

Regular expression:

NFA:

$L = \{ w \text{ in } \{0,1\}^* \mid w \text{ has exactly one } 0 \text{ and an even number of } 1\text{s} \}$

DFA, directly:

DFA, via construction:

Alternate regular expressions?

- A. $(011)^* \cup (101)^* \cup (110)^*$
- B. $(11)^*0(11)^*$
- C. $(\epsilon \cup 1)(11)^* 0 (\epsilon \cup 1)(11)^*$
- D. All of the above
- E. None of the above

New model

Define a “TFA” given by a state diagram that has **at most one outgoing arrow** from each state labelled by each alphabet symbol. Formally, as (Q, Σ, R, q_0, F) where R is a subset of $Q \times \Sigma \times Q$ such that each pair of q in Q and x in Σ appear at most once in the first & second components of a tuple in R .

Claim: Any TFA is equivalent to a DFA

New model

Define a “TFA” given by a state diagram that has **at most one outgoing arrow** from each state labelled by each alphabet symbol. Formally, as (Q, Σ, R, q_0, F) where R is a subset of $Q \times \Sigma \times Q$ such that each pair of q in Q and x in Σ appear at most once in the first & second components of a tuple in R .

Claim: Any TFA is equivalent to a DFA

Proof: Given (Q, Σ, R, q_0, F) , build

- A. $(Q, \Sigma, \delta, q_0, F)$ where δ maps (q,x) to q' if (q,x,q') is in R , and to q otherwise.
- B. $(Q, \Sigma, \delta, q_0, \{q_0\})$ where δ maps (q,x) to q' if (q,x,q') is in R , and to q_0 otherwise.
- C. $(Q \cup \{q_{\text{new}}\}, \Sigma, \delta, q_0, \{q_{\text{new}}\})$ where δ maps (q,x) to q' if (q,x,q') is in R , and to q_{new} otherwise (assuming q_{new} is not in Q)
- D. $(Q \cup \{q_{\text{new}}\}, \Sigma, \delta, q_0, F)$ where δ maps (q,x) to q' if (q,x,q') is in R , and to q_{new} otherwise (assuming q_{new} is not in Q)
- E. None of the above

Claim: If L is regular, so is L^R

Claim: The set $\{0^j 1^k \mid j, k \geq 0 \text{ and } k \geq j\}$ is not regular.

(Using) Pumping Lemma

Theorem: $L = \{0^j 1^k \mid j, k \geq 0 \text{ and } k \geq j\}$ is not regular.

Proof (by contradiction): Assume, towards a contradiction, that L is regular. Then by the Pumping Lemma, there is a pumping length, p , for L . Choose s to be the string _____ . The Pumping Lemma guarantees that s can be divided into parts $s=xyz$ such that $|xy| \leq p$, $|y| > 0$, and for any $i \geq 0$, $xy^i z$ is in L . But, if we let $i = \underline{\hspace{2cm}}$, we get the string _____ which is not in L , a contradiction. Thus L is not regular.



