

CSE208: Advanced Cryptography

Daniele Micciancio

UCSD

Fall 2020



CSE208:
Advanced
Cryptography

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Introduction

Defining FHE

Bootstrapping

LWE

Linearity

Key Switching

Multiplication

FHE!!

Ring LWE

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Section 1

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Ring LWE

- Graduate Level Advanced Cryptography
- Prerequisites:
 - CSE207 or equivalent
 - Solid theoretical background, cryptographic definitions, etc.
 - Some programming

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 - Solid theoretical background, cryptographic definitions, etc.
 - Some programming
- Past topics: Zero Knowledge, Functional Encryption, Secure Computation, etc.
- Not required: CSE206A (Lattice Algorithms)

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 - Some programming
- Past topics: Zero Knowledge, Functional Encryption, Secure Computation, etc.
- Not required: CSE206A (Lattice Algorithms)
- Reading:
 - no textbook
 - mostly research papers
 - see course webpage, canvas, etc.

Fall 2020 Topic

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- Fully Homomorphic Encryption:
 - Encryption schemes that supports the evaluation of arbitrary programs on encrypted inputs
- Applications:
 - secure outsourced computing
 - building block for MPC and more

Brief History of Homomorphic Encryption

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- 1978: Rivest, Adleman & Dertouzos posed the problem
- 2009: Gentry 2009 proposed the first candidate solution
- 2010-2020: Work towards more efficient solutions based on standard complexity assumptions (Brakerski, Vaikuntanathan, Gentry, Halevi, Smart, ...)

Software libraries

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- IBM **HElib** (Halevi & Shoup)
- Microsoft **SEAL**
- NJIT/Duality **PALISADE** (Rohloff, Cousins & Polyakov)
- Functional Lattice Cryptography **LoL** (Crockett & Peikert)
- Fastest FHE of the West **FHEW** (Ducas & Micciancio)
- FHE over the Torus **TFHE** (Chillotti, Gama, Georgieva & Izabachene)
- Approximate FHE **HEAAN** (Cheon, Kim, Kim & Song)

Software libraries

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- In the News:
 - February 21, 2019: Microsoft **SEAL** open source homomorphic encryption library gets even better for .NET developers!
 - June 4, 2020: IBM releases FHE toolkit for MacOS and iOS; Linux and Android Coming Soon

Homework and Evaluation

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- Homework assignments:
 - 3 assignments, due within one week from assignment date
 - Cover theoretical/mathematical topics

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- Homework assignments:
 - 3 assignments, due within one week from assignment date
 - Cover theoretical/mathematical topics
- Small Project:
 - Goal: Try to use one of the many HE libraries
 - Not much coding, but you will have to write and compile a few lines of code
 - Evaluated primarily based on written report

Administrivia:

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- Course webpage: <http://cseweb.ucsd.edu/classes/fa20/>
 - general course information
 - pointers to papers and other reading material
- Canvas:
 - recording of lectures
 - homework distribution/collection
 - grades
 - discussion board

Course Schedule (Tentative)

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Week 1: Introduction and Definition

- FHE Definition
- Gentry's Bootstrapping theorem
- Homework 1 out

Week 2-4: Fundamental techniques based on general lattices

- LWE encryption
- Linear Homomorphic computations
- Key Switching and Proxy re-encryption
- Nested encryption and homomorphic multiplication
- Ciphertext Tensoring and homomorphic multiplication
- Homomorphic Decryption and Bootstrapping algorithms
- Homework 2 out

Week 5: Algebraic Number Theory

- I really hope you like math!
- Homework 3 out

Week 6-10: Efficient FHE from Ring LWE

- Message packing techniques
- Linear transformations on structured matrices
- Other FHE schemes: GHS, BFV, FHEW, AP13, TFHE, CKKS ...