

CSE 20 Discussion

Week 2

1. Fill in the blanks of the definition of the recursive function *ones*, which takes a bitstring as input and gives the number of 1s in the bitstring as output. Note that the set of all bitstrings is denoted as $\{0, 1\}^*$.

Basis Step:

Recursive Step:

ones : \rightarrow

2. Base Conversion Practice

(a) Please fill out the following table below for fixed width representations:

base 10 (width 2)	base 16 (width 1)	base 2 (width 4)
$(10)_{10,2}$		
$(11)_{10,2}$		
$(12)_{10,2}$		
$(13)_{10,2}$		
$(14)_{10,2}$		
$(15)_{10,2}$		

(b) Find the base 2 expansions of the following:

i. $(1337)_8$

ii. $(A96B1)_{16}$

(c) Find the base 8 expansion of $(110101011110)_2$

(d) Find the base 16 expansion of $(101011100011001110)_2$

(e) Find the base 2, fixed-width binary expansion of 0.1 with integer part width 1 and fractional part width 8.

3. When we have two positive integers n and m , dividing n by m means writing n as $mq + r$ where q is the (integer) quotient and r is the (integer) remainder, with $0 \leq r < m$. We can also write q as $n \mathbf{div} m$ and r as $n \mathbf{mod} m$.

(a) Compute $11 \mathbf{div} 3$ and $11 \mathbf{mod} 3$

(b) Compute $-7 \mathbf{div} 4$ and $-7 \mathbf{mod} 4$

4. For each of the numbers below, write the number in:

- binary expansion
- binary fixed-width 4
- sign-magnitude width 4
- 2's complement width 4

or determine that it is not possible.

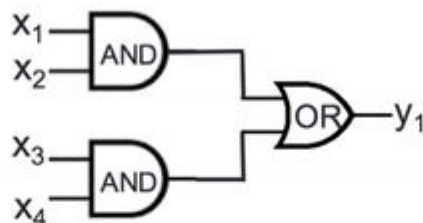
(a) 5

(b) -7

(c) -8

(Optional)

Consider the logic circuit

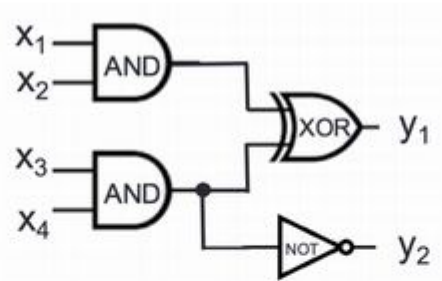


For which of the following settings(s) of input values is the output $y_1 = 0$? (Select all and only those that apply.)

- i. $x_1 = 0$, $x_2 = 0$, $x_3 = 0$, and $x_4 = 0$
- ii. $x_1 = 1$, $x_2 = 1$, $x_3 = 1$, and $x_4 = 1$
- iii. $x_1 = 1$, $x_2 = 0$, $x_3 = 0$, and $x_4 = 1$
- iv. $x_1 = 0$, $x_2 = 0$, $x_3 = 1$, and $x_4 = 1$

(Optional)

Consider the logic circuit



For which of the following settings(s) of input values is the output $y_1 = 1$ and $y_2 = 1$? (Select all and only those that apply.)

- i. $x_1 = 0$, $x_2 = 0$, $x_3 = 0$, and $x_4 = 0$
- ii. $x_1 = 1$, $x_2 = 0$, $x_3 = 1$, and $x_4 = 1$
- iii. $x_1 = 1$, $x_2 = 1$, $x_3 = 0$, and $x_4 = 0$
- iv. $x_1 = 0$, $x_2 = 0$, $x_3 = 1$, and $x_4 = 1$