

Definition: A **predicate** is a function from a given set (domain) to $\{T, F\}$.

A predicate can be applied, or **evaluated** at, an element of the domain.

Two predicates over the same domain are **equivalent** means they evaluate to the same truth values for all possible assignments of domain elements to the input.

Input	Output			Input	$E(x)$	$L(x)$	$M(x)$
x	$P(x)$	$N(x)$	$Mystery(x)$	x	" $(x)_2$ is even"	" $(x)_2 < 3$ "	Note: $256 = 2^8$ " $(x)_2 > 256$ "
000	F		T	1	F	T	F
001	T		T	10	T	T	F
010	T		T	11	F	F	F
011	T		F	100	T	F	F
100	F		F	101	F	F	F
101	F		T	110	T	F	F
110	F		F
111	F		T		No last row!		

The domain for each of the predicates $P(x)$, $N(x)$, $Mystery(x)$ is _____.

Extra example:

The domain for each of the predicates $E(x)$, $L(x)$, $M(x)$ is _____.

Definition: The **truth set** of a predicate is the collection of all elements in its domain where the predicate evaluates to T .

The truth set for the predicate $P(x)$ is _____.

The truth set for the predicate $N(x)$ is _____.

The truth set for the predicate $Mystery(x)$ is _____.

Extra example:

Three (distinct) elements in the truth set of $E(x)$ are _____.

Three (distinct) elements in the truth set of $L(x)$ are _____.

Three (distinct) elements in the truth set of $M(x)$ are _____.

Definitions (Rosen 40-45):

The **universal quantification** of $P(x)$ is the statement “ $P(x)$ for all values of x in the domain” and is written $\forall xP(x)$. An element for which $P(x) = F$ is called a **counterexample** of $\forall xP(x)$.

The **existential quantification** of $P(x)$ is the statement “There exists an element x in the domain such that $P(x)$ ” and is written $\exists xP(x)$. An element for which $P(x) = T$ is called a **witness** of $\exists xP(x)$.

Example: _____ is a true existential quantification.

Statements involving predicates and quantifiers are **logically equivalent** means they have the same truth value no matter which predicates (domains and functions) are substituted in.

Quantifier version of De Morgan’s laws: $\boxed{\neg\forall xP(x) \equiv \exists x(\neg P(x))}$ $\boxed{\neg\exists xQ(x) \equiv \forall x(\neg Q(x))}$

Example: _____ is a false universal quantification. It is logically equivalent to _____

Recall: Each RNA strand is a string whose symbols are elements of the set $B = \{\mathbf{A}, \mathbf{C}, \mathbf{G}, \mathbf{U}\}$. The **set of all RNA strands** is called S . The function *rnalen* that computes the length of RNA strands in S is:

	$rnalen : S \rightarrow \mathbb{Z}^+$
Basis Step: If $b \in B$ then	$rnalen(b) = 1$
Recursive Step: If $s \in S$ and $b \in B$, then	$rnalen(sb) = 1 + rnalen(s)$

Example predicates on S

$H(s) = T$	Truth set of H is _____
$L_3(s) = \begin{cases} T & \text{if } rnalen(s) = 3 \\ F & \text{otherwise} \end{cases}$	Strand where L_3 evaluates to T is e.g. _____ Strand where L_3 evaluates to F is e.g. _____
F_A is defined recursively by: Basis step: $F_A(\mathbf{A}) = T, F_A(\mathbf{C}) = F_A(\mathbf{G}) = F_A(\mathbf{U}) = F$ Recursive step: If $s \in S$ and $b \in B$, then $F_A(sb) = F_A(s)$	Strand where F_A evaluates to T is e.g. _____ Strand where F_A evaluates to F is e.g. _____
P_{AUC} is defined as the predicate whose truth set is the collection of RNA strands where the string AUC is a substring (appears inside s , in order and consecutively)	Strand where P_{AUC} evaluates to T is e.g. _____ Strand where P_{AUC} evaluates to F is e.g. _____