Input		Output		
		Conjunction	**Exclusive or**	**Disjunction**
p	q	$p \wedge q$	$p \oplus q$	$p \vee q$
T	T	T	F	T
T	F	F	T	T
F	T	F	T	T
F	F	F	F	F

Input	Output
	Negation
p	$\neg p$
T	F
F	T

Input			Output	
p	q	r	$(p \wedge q) \oplus (\ (p \oplus q) \wedge r\ )$	$(p \wedge q) \vee (\ (p \oplus q) \wedge r\ )$
T	T	T		
T	T	F		
T	F	T		
T	F	F		
F	T	T		
F	T	F		
F	F	T		
F	F	F		

Extra Example: Add a column for the compound proposition $(r \wedge p) \oplus (\ (r \oplus p) \wedge q\ )$ (see last day's worksheet)

Definition: Two compound propositions are **logically equivalent** means that they have the same truth values for all settings of truth values to their propositional variables.

Definition: A **tautology** is a compound proposition that evaluates to true for all settings of truth values to its propositional variables; it is abbreviated T.

Example

Definition: A **contradiction** is a compound proposition that evaluates to false for all settings of truth values to its propositional variables; it is abbreviated F.

Example

Extra Example: Which of the compound propositions in the table below are logically equivalent?

Input		Output				
p	q	$\neg(p \wedge \neg q)$	$\neg(\neg p \vee \neg q)$	$(\neg p \vee q)$	$(\neg q \vee \neg p)$	$(p \wedge q)$
T	T					
T	F					
F	T					
F	F					

Input		Output	
p	q	$mystery_1$	$mystery_2$
T	T	T	F
T	F	T	F
F	T	F	F
F	F	T	T

Input			Output
p	q	r	?
T	T	T	T
T	T	F	T
T	F	T	F
T	F	F	T
F	T	T	F
F	T	F	F
F	F	T	T
F	F	F	F

A compound proposition that gives output $mystery_1$ is: _____

A compound proposition that gives output $mystery_2$ is: _____

Extra example: A compound proposition that gives output ? is: _____

Definition A compound proposition is in **disjunctive normal form** (DNF) means that it is an OR of ANDs of variables and their negations.

Definition A compound proposition is in **conjunctive normal form** (CNF) means that it is an AND of ORs of variables and their negations.