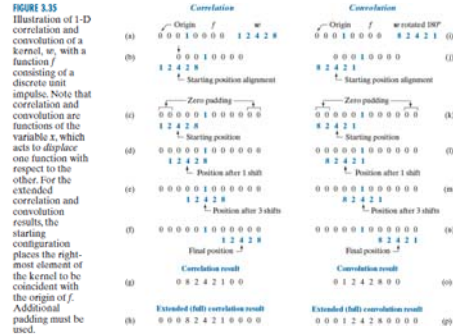


Spatial Filtering

Image Processing
CSE 166
Lecture 4

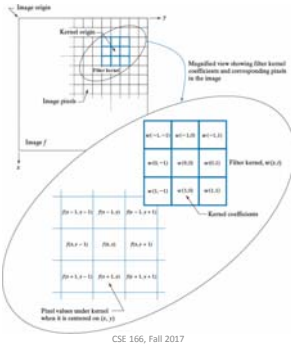
Correlation and convolution (1D)



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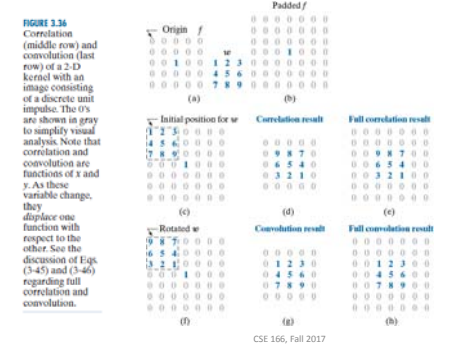
Spatial filtering (2D)



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Correlation and convolution (2D)



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Correlation and convolution

- Convolution is commutative and associative, correlation is not

TABLE 3.5

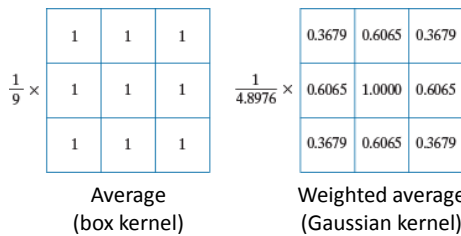
Some fundamental properties of convolution and correlation. A dash means that the property does not hold.

Properties	Convolution	Correlation
Commutative	$f * g = g * f$	—
Associative	$f * (g * h) = (f * g) * h$	—
Distributive	$f * (g + h) = (f * g) + (f * h)$	$f \circ (g + h) = (f \circ g) + (f \circ h)$

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Smoothing kernels



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Smoothing with box kernel

Input image 3x3

11x11 21x21

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Smoothing with Gaussian kernel

FIGURE 3.41 (a) Sampling a Gaussian function to obtain a discrete Gaussian kernel. The values shown are for $K = 1$ and $\sigma = 1$. (b) Resulting 3×3 kernel [this is the same as Fig. 3.37(b)].

Standard deviation σ	Percent of total volume under surface
1	39.35
2	86.47
3	98.89

Volume under surface greater than 3σ is negligible

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Smoothing with Gaussian kernel

$\sigma = 7$ 43x43

$\sigma = 7$ 85x85

Difference

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Smoothing with Gaussian kernel

Input image $\sigma = 3.5$ 21x21 $\sigma = 7$ 43x43

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Border padding

Zero padding when $v = 0$

Constant padding

Replicate padding

Mirror padding

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Border padding

Zero padding

Mirror padding

Replicate padding

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