CSE 160 Lecture 2

Programming with Threads Parallel Sorting

Scott B. Baden

Announcements

- Makeup on 10/7
- Quiz #1 on Weds 10/9
- SVN

Today's lecture

- Two applications with multithreading
- Synchronization
- Parallel Sorting

Recall the Threads Programming model

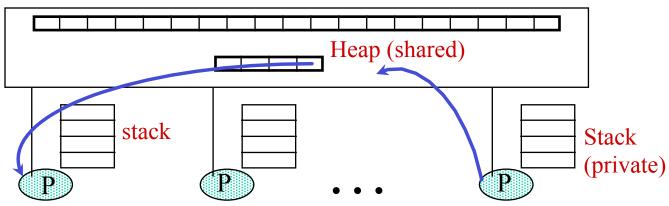
• Start with a single root thread

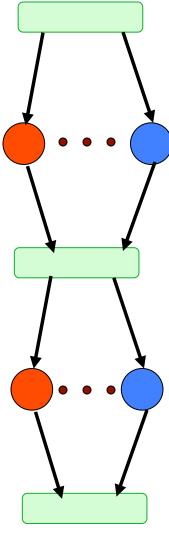
• Fork-join parallelism to create concurrently executing threads

• Threads communicate via shared memory

• A spawned thread executes asynchronously until it completes

• Threads may or may not execute on different processors





C++11 Threads

- Via <thread>, C++ supports a threading interface similar to pthreads, though a bit more user friendly
- Async is a higher level interface suitable for certain kinds of applications
- New memory model
- Atomic template

Hello world with <Threads>

```
#include <thread>
void Hello(int TID) {
   cout << "Hello from thread " << TID << endl;
int main(int argc, char *argv[]){
 thread *thrds = new thread[NT];
// Spawn threads
for(int t=0;t< NT;t++){
    thrds[t] = thread(Hello, t);
// Join threads
for(int t=0;t< NT;t++)
    thrds[t].join();
```

```
$./hello th 3
Hello from thread 0
Hello from thread 1
Hello from thread 2
$./hello th 3
Hello from thread 1
Hello from thread 0
Hello from thread 2
$./hello th 4
Running with 4 threads
Hello from thread 0
Hello from thread 3
Hello from thread Hello from
thread 21
```

\$PUB/Examples//Threads/Hello-Th

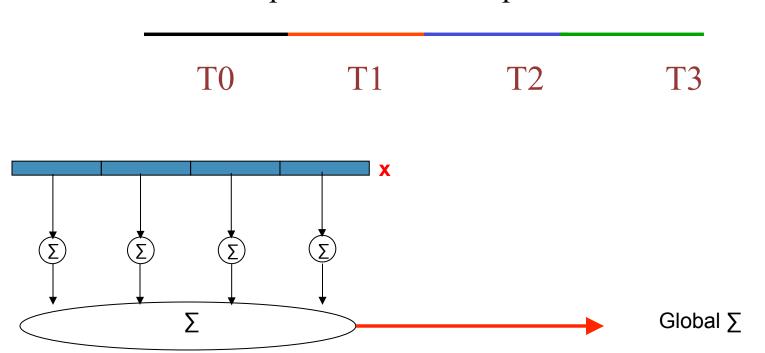
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Steps in writing multithreaded code

- We write a *thread function* that gets called each time we spawn a new thread
- Spawn threads by constructing objects of class Thread (in the C++ library)
- Each thread runs on a separate processing core (If more threads than cores, the threads share cores)
- Join threads so we know when they are done

A first application

- Sum a list of integers for i = 0:N-1 sum = sum + x[i];
- Partition x[] into intervals, assign each to a unique thread
- Each thread sweeps over a reduced problem



First version of summing code

```
void sum(int TID, int N, int NT){
  int64 t i0 = TID*(N/NT), i1 = i0 + (N/NT);
  int64 t local sum=0;
  for (int i=i0; i<i1; i++)
     local sum += x[i];
  global sum += local sum
                               int* x;
                             Main():
                               int64_t global_sum;
                               for(int t=0; t<NT; t++){
                                 thrds[t] = thread(sum,t,N,NT);
```

Steps in writing multithreaded code (II)

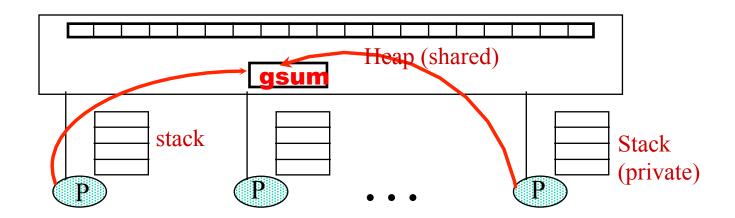
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- *Join* threads so we know when they are done
- Threads share memory

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Results

- The program usually runs correctly
- But sometimes it produces incorrect results: Result verified to be INCORRECT, should be 549756338176
- What happened?
- There is a conflict when updating global_sum: a *data race*



Data race

- A date race arises when there is at least one writer on shared data
- There are multiple writers of global sum

```
int64_t global_sum;
void sum(int TID, int N, int NT){
    int64_t i0 = TID*(N/NT), i1 = i0 + (N/NT);
    int64_t localSum=0;
    for (int i=i0; i<i1; i++)
        localSum += x[i];
    global_sum += local_sum
}</pre>
```

Avoiding the data race

- Perform the global summation in main()
- After a thread joins, add its contribution to the global sum, one thread at a time
- We need to wrap ref() around ref arguments, int64_t &, compiler needs the hint

```
int64_t global_sum, local_sum;
...
int *locSims = new int[NT];
for(int t=0; t<NT; t++)
    thrds[t] = thread(sum,t,N,NT,ref(locSums[t]);
for(int t=0; t<NT; t++){
    thrds[t].join();
    global_sum += local_sum;
}</pre>
```

Steps in writing multithreaded code (III)

- We write a *thread function* that gets called each time we spawn a new thread
- *Spawn* threads by constructing objects of class Thread (in the C++ library)
- Each thread runs on a separate processing core (If more threads than cores, the threads share cores)
- *Join* threads so we know when they are done
- Threads share memory
- Avoid data races to ensure correctness

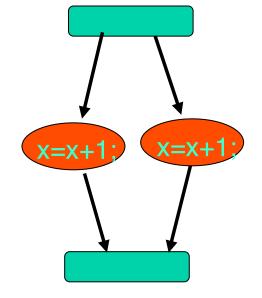
Race conditions

Consider the following thread function, where x is initially 0 void threadFn(int TID) {
 x++;
 }

- Let run on 2 threads
- What is the value of x after both threads have joined?
- A *race condition* arises because the timing of accesses to shared data can affect the outcome
- We say we have a *non-deterministic* computation
- Normally, if we repeat a computation using the same inputs we expect to obtain the same results
- This is true because we have a *side effect* (global variables, I/O and random number generators)

Under the hood of a race condition

- Assume x is initially 0 x=x+1;
- Generated assembly code



Possible interleaving with two threads

<u>P1</u>	<u>P2</u>	
$r1 \leftarrow x$		r1(P1)
	$r1 \leftarrow x$	r2(P2)
$r1 \leftarrow r1 + #1$		r1(P1)
	$r1 \leftarrow r1 + #1$	<i>r1(P1)</i>
$x \leftarrow r1$		P1 writ
	$x \leftarrow r1$	P2 writ

Avoiding race conditions

- We need to take steps to avoid race conditions through appropriate program synchronization
 - Migrate shared updates into main
 - Critical sections
 - Barriers
 - Atomics

Critical Sections

- In some cases it is costly (or inconvenient) to join and re-spawn threads to synchronize
- Instead, we synchronize inside the thread function
- We must allow only 1 thread at a time to write to the shared memory location(s)
- The code performing the operation is called a *critical section*
- We use *mutual exclusion* to implement a critical section
- A critical section is non-parallelizing computation.. sensible guidelines?

Begin Critical Section X++;

End Critical Section

Using mutexes in C++

- The <mutex> library provides a mutex class
- A mutex (AKA a "lock") may be CLEAR or SET
 - **Lock()** waits if the lock is set, else sets the lock
 - Unlock() clears the lock if set
- Mutexes are global variables. Why?



```
void sum(int TID, int N, int NT){
    ...
for (int i=i0; i<i1; i++)
    localSum += x[i];
// Critical section
    mutex_sum.lock();
    global_sum += localSum;
    mutex_sum.unlock();
}</pre>
```

```
int* x;

mutex mutex_sum;
int64_t global_sum;
Main():
// Spawn threads
```

Results

- ./sum 1 1000000001.30 seconds
- ./sum 2 10⁹
 0.79 seconds [speedup = 1.64]
- ./sum 4 10⁹
 0.69 seconds [incremental speedup = 1.14]
- ./sum 8 10⁹
 0.68 seconds [incremental speedup = 1.01]

Using a more expensive kernel

- for (int i=i0; i<i1; i++) sum += sin(x[i]);
- ./sumSine 1 10⁸
 6.50 seconds
- ./sumSine 2 10⁸
 3.27 seconds [speedup = 1.99]
- ./sumSine 4 10⁸
 1.63 seconds [incremental speedup = 2.0]
- ./sumSine 8 10⁸
 0.82 seconds [incremental speedup = 1.99]

How do we explain the results?

- Expensive kernel gets perfect speedup on 4 cores
- Inexpensive kernel gets a speedup of 1.9

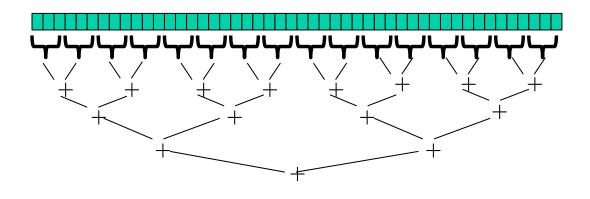


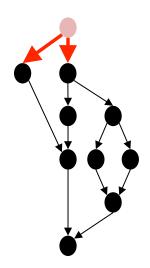
2nd application: testing for primality

- Given a list of numbers, which are prime?
 primes <# threads> 2 17 31 3415501328329
- Code in \$PUB/Examples/Threads/Primes
- 3 Versions: Threads, Async (later), Pthreads

Other kinds of threading structures

• We may create elaborate threading structures, for example, divide and conquer





Steve Wolfman, based on work by Dan Grossman

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Parallel Sorting

- Sorting is fundamental algorithm in data processing
 - Given an unordered set of keys $x_0, x_1, ..., x_{N-1}$
 - Return the keys in sorted order
- The keys may be character strings, floating point numbers, integers, or any object for which the relations >, <, and == hold
- We'll assume integers here
- Will talk about other algorithms later on

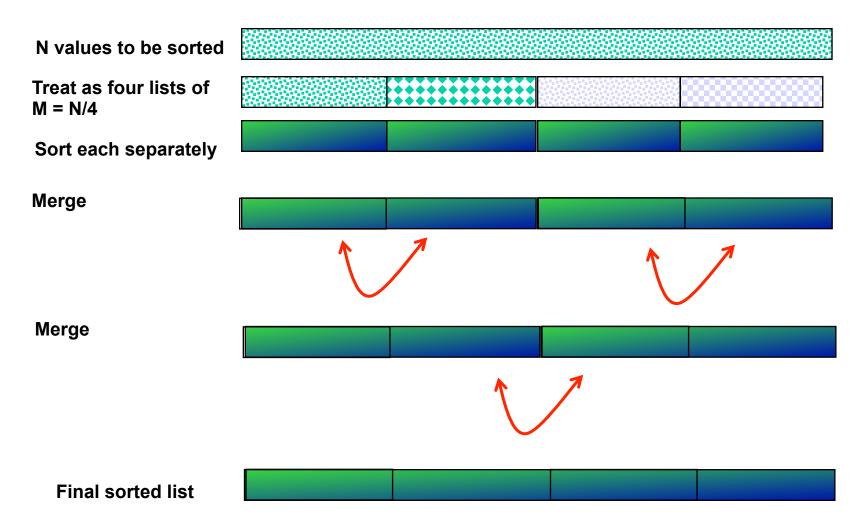
Parallel sorting algorithms

- We'll consider in-memory sorting of integer keys
 - Merge Sort
 - Bucket sort
 - Sample sort
 - Bitonic sort
- In practice, we sort on external media, i.e. disk
 - See: http://sortbenchmark.org
 - ➤ TritonSort (UCSD): 0.725 x 10¹² bytes/minute

Merge Sort algorithm

- A divide and conquer algorithm
- When we reach a certain size, we stop the recursion: each thread locally sorts its data using a fast serial algorithm like quicksort
- Threads merge their data in odd-even pairs
- Each thread applies a local merge sort to extract the smallest (largest) N/P values, discards the rest
- What is the running time?

Merge sort in action



Serial Merge



- Merge Step
- Left most thread does the merging
 - -1 3 7 9 11 2 4 8 12 14
- Sorts the merged list
 - -1 2 3 4 7 8 9 11 2 14



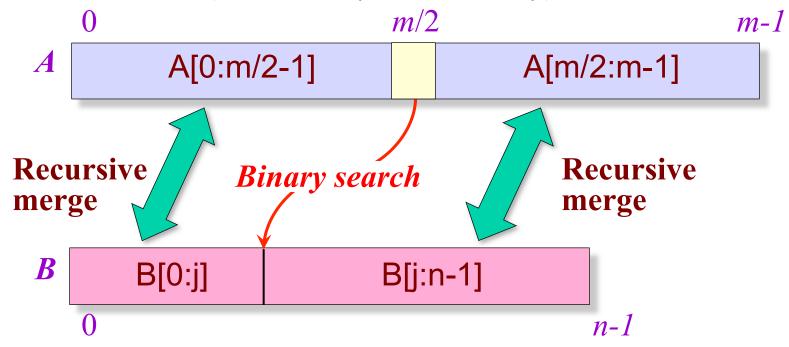
- Parallelism diminishes as we move up the recursion tree
- There is only O(log n) parallelism, but if we stop the recursion before reaching the bottom of the tree, it's much smaller

Parallel Merge

• If there are N = m+n elements, then the larger of the recursive merges processes $\sqrt[3]{4}N$ elements



• Assume $m \ge n$ (switch arrays if necessary)



Charles Leiserson

Assignment #1

- Implement parallel merge sort
- Implement parallel merge and determine how much it helps
- Observe speedups
- Develop on leng6, benchmarking on Bang
- Use SVN for you code development
 - Starter code available via SVN
 - Required to use SVN repository on Bang
 - Do not use github or other repositories
 - Any sharing of code is a breach of Academic Integrity
 - SVN Discussion in section on Wednesday
 - ▶ Be sure to respond to posting about registering your team
- A4 will be posted by Wednesday evening