Advanced Computer Graphics
CSE 163 [Spring 2018], Lecture 5
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To Do
- Assignment 1, Due Apr 27.
  - This lecture only extra credit and clear up difficulties
  - Questions/difficulties so far in doing assignment?

Digital Image Compositing
1996: Academy scientific and engineering achievement award (oscar ceremony) "For their pioneering inventions in digital image compositing"

Image Compositing
Separate an image into elements
- Each part is rendered separately
- Then pasted together or composited into a scene

Blue Screen Matting
- Photograph or create image of object against blue screen (blue usually diff from colors like skin)
- Then extract foreground (non-blue pixels)
- Add (composite) to new image
- Problem: aliasing [hair] (no notion of partial coverage/blue)

Outline
- Compositing
  - Blue screen matting
  - Alpha channel
  - Porter-Duff compositing algebra (Siggraph 84)
- Morphing (Beier-Neely, Siggraph 92)
**Alpha Channel**

- In general, 32 bit RGBA images
- Alpha encodes coverage (0=transparent, 1=opaque)
- Simple compositing: \( \text{OUT} = \alpha F + (1 - \alpha)B \)

**Example:** \( \alpha = 0.3 \)

\[ \begin{array}{c}
\text{Partial Coverage} \\
\text{or}
\end{array} \]

- Semi-Transparent

**Pixels with Alpha: Conventions**

Pre-multiplication
- Color \( C = (r, g, b) \) and coverage alpha is often represented as \((\alpha r, \alpha g, \alpha b, \alpha)\)
- One benefit: color components are directly displayed (analogous to homogeneous coordinates)

What is \((\alpha, C)\) for the following?
- \((0, 1, 0, 1)\) = Full green, full coverage
- \((0, \frac{1}{2}, 0, 1)\) = Half green, full coverage
- \((0, \frac{1}{2}, 0, \frac{1}{2})\) = Full green, half (partial) coverage
- \((0, \frac{1}{2}, 0, 0)\) = No coverage

**Compositing with Alpha**

- Suppose we put \( A \) over \( B \) over background \( G \)

  - How much of \( B \) is blocked by \( A \)?
    \[ \alpha_A \]
  - How much of \( B \) shows through \( A \)
    \[ (1 - \alpha_A) \]
  - How much of \( G \) shows through both \( A \) and \( B \)?
    \[ (1 - \alpha_A)(1 - \alpha_B) \]

**Opaque Objects**

- In this case, \( \alpha \) controls the amount of pixel covered (as in blue screening).
- How to combine 2 partially covered pixels? 4 possible outcomes.

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### Compositing Algebra
- 12 reasonable combinations (operators)

![Compositing Operators Diagram](image)

### Computing Colors with Compositing
- Coverages shown previously only examples
- We only have $\alpha$, not exact coverage, so we assume coverages of A and B are uncorrelated
- How to compute net coverage for operators?

### Example: C = A over B
- For colors that are not premultiplied:
  - $C = \alpha_A A + (1-\alpha_A) \alpha_B B$
  - $\alpha = \alpha_A + (1-\alpha_A) \alpha_B$
- For colors that are premultiplied:
  - $C' = A' + (1-\alpha_A) B'$
  - $\alpha = \alpha_A + (1-\alpha_A) \alpha_B$

**Assumption:** coverages of A and B are uncorrelated for each pixel

### Image Compositing Example
  - [https://www.youtube.com/watch?v=F2AltTP15U0](https://www.youtube.com/watch?v=F2AltTP15U0)

### Examples
- Easy enough to implement: assignment in many courses (we show example from CMU course):
  - No music, but the good poor man’s alternative

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The idea in morphing

- User marks line segments
- These are used to warp image 1 and image 2
- Images are then blended
- Key step is warping
  - Why is it needed? Why not just cross-dissolve or blend two images based on alpha (how far between them)?
  - How is it to be done with line segments?

Simple Cross-Dissolve

- Blend images with "over" operator
  - alpha of bottom image is 1.0
  - alpha of top image varies from 0.0 to 1.0

\[
\text{blend}(i,j) = (1-t) \cdot \text{src}(i,j) + t \cdot \text{dst}(i,j) \quad (0 \leq t \leq 1)
\]

Feature-Based Warping

- To warp image 1 into image 2, we must establish correspondence between like features
- Then, those features transform (and rest of image moves with them)
- In Beier-Neely, features are user-specified line segments (nose, face outline etc.)
- Warping is an image transformation (generally more complex than scale or shift, but same basic idea)
- Morphing takes two warped images, cross-dissolves
Warping with Line Segments
- We know how line warps, but what about whole img?
- Given $p$ in dest image, where is $p'$ in source image?

$u$ is a fraction
$v$ is a length (in pixels)

Warping with one Line Pair
- What happens to the $F$?

Translation!!

Warping with one Line Pair
- What happens to the $F$?

Similar ideas apply to rotation, other similarity transforms

Scale !!

Warping with Multiple Line Pairs
- Use weighted combination of points defined by each pair of corresponding lines

Details
- Use weighted combination of points defined by each pair of corresponding lines

$w[i] = \left( \frac{\text{length}(i)}{a + \text{dist}(i)} \right)^{\rho}$

Where:
- $\text{length}(i)$ is the length of $L[i]$
- $\text{dist}(i)$ is the distance from $X$ to $L[i]$
- $a$, $b$, $\rho$ are constants that control the warp

Weighting effect of each line pair
- To weight the contribution of each line pair, Beier & Neeley use:
Warping Pseudocode

WarpImage(Image, L[...], L[...])
begin
  foreach destination pixel p do
    psnum = (0,0)
    wsum = 0
    foreach line L[i] in destination do
      p'[i] = p transformed by (L[i], L[i])
      psnum = psnum + p'[i] * weight[i]
      wsum += weight[i]
    end
    p' = psnum / wsum
    Result(p) = Image(p')
  end
end

Morphing Pseudocode

GenerateAnimation(Image₀, L₀[...], Image₁, L₁[...])
begin
  foreach intermediate frame time t do
    for i = 1 to number of line pairs do
      L[i] = line i-th of the way from L₀[i] to L₁[i]
    end
    Warp₀ = WarpImage(Image₀, L₀, L)
    Warp₁ = WarpImage(Image₁, L₁, L)
    foreach pixel p in FinalImage do
      Result(p) = (1-t) Warp₀ + t Warp₁
    end
  end
end

Examples

Discrete Reconstruction
Equivalent to multiplying by comb function (a)
Convolving with similar fn in frequency domain (b). Separation in frequency domain depends on spatial sampling rate
Replicated Fourier spectra (when is this safe?)

Bonus: Reconstruction
- Section 14.10.5 of textbook (in handout)
- Some interesting, more technical ideas
- Discuss briefly if time permits

Replicated Fourier Spectra
- One can window to eliminate unwanted spectra
- Equivalent to convolution with sinc
- No aliasing if spectra well enough separated (initial spatial sampling rate high enough)
- In practice, we use some reconstruction filter (not sinc), such as triangle or Mitchell filter
Adequate Sampling Rate

Inadequate Sampling Rate

Filter first

Non-Ideal Reconstruction

In practice, convolution never with sinc

Sampling frequency must be even higher than Nyquist, or we get substantial aliasing

In figure, samples trace out original modulated by a low-frequency sine wave. Low freq amplitude modulation remains, compounded by rastering if reconstruct box filter