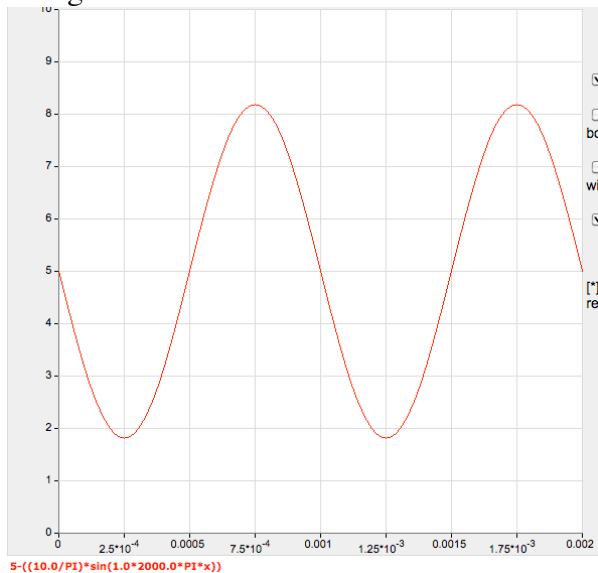


1. Fourier Analysis

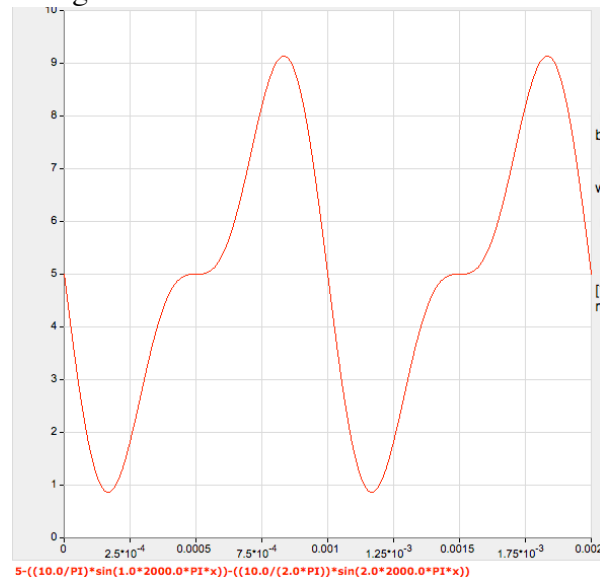
t	f1(t)	f2(t)	f3(t)	f(t)
0.000000	-0.000000	-0.000000	-0.000000	5.000000
0.000100	-1.870979	-1.513653	-1.009102	0.606266
0.000200	-3.027307	-0.935490	0.623659	1.660863
0.000300	-3.027307	0.935489	0.623659	3.531842
0.000400	-1.870979	1.513654	-1.009102	3.633573
0.000500	0.000000	-0.000000	0.000000	5.000000
0.000600	1.870979	-1.513654	1.009102	6.366427
0.000700	3.027307	-0.935490	-0.623659	6.468158
0.000800	3.027307	0.935488	-0.623660	8.339136
0.000900	1.870979	1.513654	1.009102	9.393735
0.001000	-0.000001	-0.000001	-0.000000	4.999997
0.001100	-1.870979	-1.513653	-1.009102	0.606266
0.001200	-3.027307	-0.935489	0.623661	1.660865
0.001300	-3.027306	0.935490	0.623659	3.531842
0.001400	-1.870979	1.513654	-1.009102	3.633572
0.001500	0.000000	-0.000000	0.000000	5.000000
0.001600	1.870977	-1.513653	1.009103	6.366427
0.001700	3.027307	-0.935488	-0.623661	6.468158
0.001800	3.027307	0.935489	-0.623661	8.339136
0.001900	1.870978	1.513653	1.009102	9.393734
0.002000	-0.000001	-0.000001	-0.000000	4.999994

2 periods of the signal can be seen in the first 2 msec.

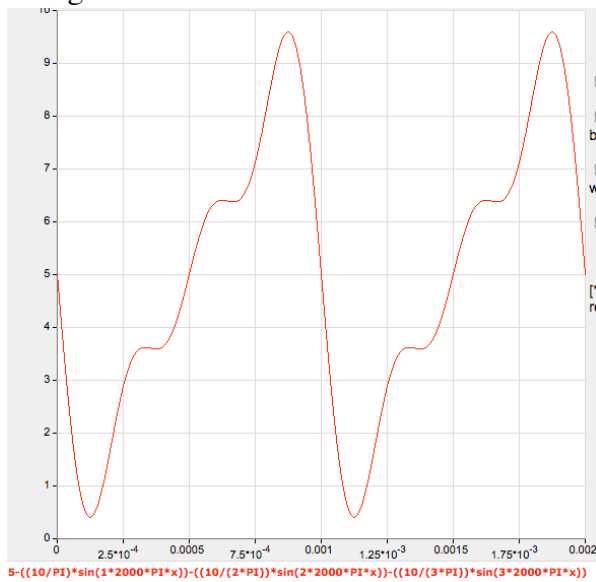
Using 1 harmonic:



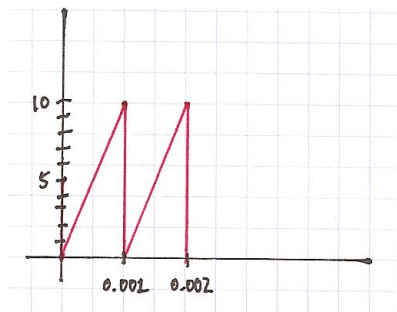
Using 2 harmonics:



Using 3 harmonics:

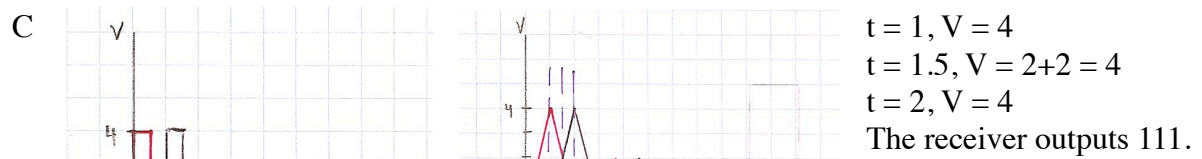
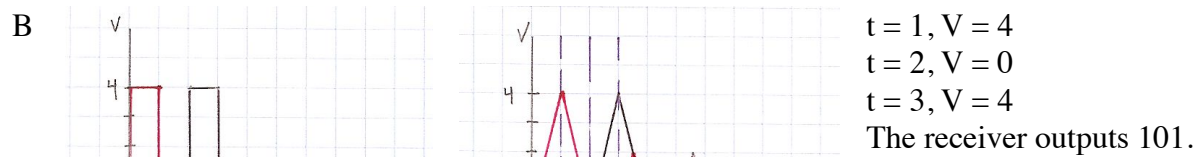
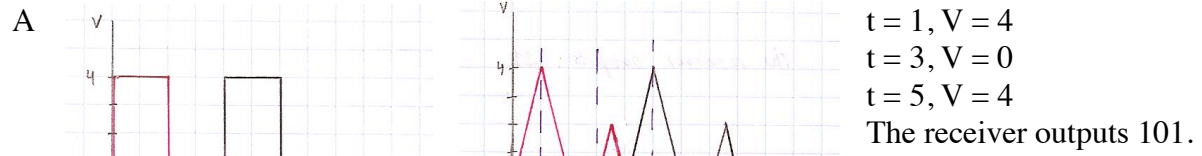


The final output shape will look like the following graph when there is enough bandwidth to pass all harmonics:

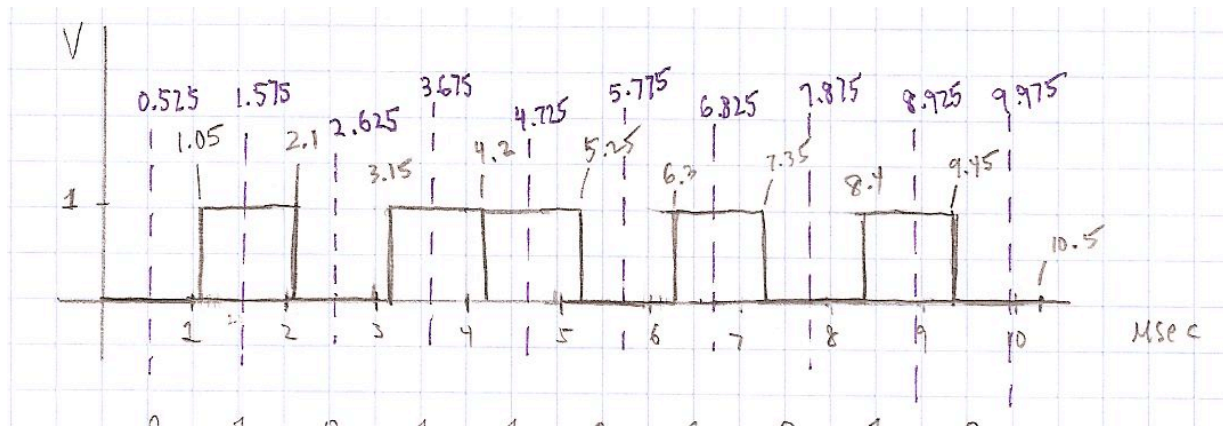


If the input signal is passed through a channel of bandwidth 1000 Hz, only the first harmonic would pass through. The general form for a harmonic is $\sin(2\pi ft)$, so the frequency of the first harmonic, $\sin(1 \cdot 2000\pi t)$, is $f = 1000$. Therefore, the output would look like the first graph.

2. Nyquist Limit



3. Clock Recovery



The tenth bit is sent from 9.45 μ sec to 10.5 μ sec.

$$(9.45 + 10.5)/2 = 9.975$$

Without clock recovery code, sampling occurs at 9.5 μ sec.

Sampling is off by 9.975 μ sec - 9.5 μ sec = 0.475 μ sec.

See the graph above for sampling instants (marked in purple).

The spike at 0.4 μ sec will not affect sampling times, because the time starts at 0.5 μ sec.

The spike at 2.4 μ sec will cause the lag to be adjusted. This adjustment will change the sampling times. The sampling times will be adjusted and correct again when a transition occurs at 5.25 μ sec.

Extra Credit:

If a spike occurs, the voltage will change back to its original value before the duration of the bit is over. To deal with spikes, make sure the voltage (V) is still the same at a time that is after the duration of a spike and before the duration of the bit is over when a transition occurs. For example, when the bit transitions from 0 to 1, check to make sure that the voltage is still one 0.75 μ sec after bit (assuming the spike lasts less than 0.75 μ sec). The following is modified pseudo-code:

```
In parallel with Wait look for a Transition if any
  If (Transition is detected at actual time A and
      Voltage at (A + 0.75  $\mu$ sec) == V)
    lag = A - P;
```