INSTRUCTIONS

Homework solutions should be neatly written or typed and submitted through Gradescope. No work can be accepted outside of this system, and no late work will be accepted. Please ensure that your submission is legible (neatly written and not too faint) or your homework may not be graded. You may update your submission as many times as you’d like up to the deadline. Only the most recent submission will be graded.

Thirty problems from homework assignments will be graded randomly throughout the quarter. You will not know in advance which problems, if any, will be graded on each assignment.

You may consult your textbook, class notes, lecture slides, instructors, TAs, and tutors for help with homework. You may also discuss homework questions with classmates, but you may not share written work with classmates. You must write up your solutions alone, in your own words. The assignments have been developed to facilitate your learning and to provide a method for fairly evaluating your knowledge and abilities, not the knowledge and abilities of others. To facilitate learning, you are authorized to discuss assignments with others; however, to ensure fair evaluations, you are not authorized to view or share written work with another person, or to write your submission in collaboration with another person. You should not look for answers to homework problems in other texts or sources, including the internet.

Do not post about homework questions on Piazza. For help with homework, please consult the course textbook, lecture slides, class notes, and podcasts, or come visit us in office hours.

READING: Sipser 3.1
1. Prove that the regular languages are a subset of the languages that can be recognized by some Turing machine (called the Turing-recognizable languages).

To do this, let \( L \) be a regular language that is recognized by some DFA \( M = (Q, \Sigma, \delta, q_0, F) \), and define a Turing machine \( \hat{M} = (\hat{Q}, \hat{\Sigma}, \hat{\Gamma}, \hat{\delta}, \hat{q}_0, \hat{q}_{\text{acc}}, \hat{q}_{\text{rej}}) \) that also recognizes \( L \).

Be sure to give the formal definition of each of the seven components that define \( \hat{M} \), being especially careful with the transition function \( \hat{\delta} \). Also include a few sentences describing the strategy behind your construction.