The Memory Hierarchy

In the book: 5.1-5.3, 5.7, 5.10
Quiz 6

• True/False
  • Squashing instructions and stalling both result in increased CPI. -- T
  • Squashing can be used to resolve control hazards. -- T
  • Stalling cannot be used to resolve control hazards. -- F
  • Static branch predictors use tables of 2-bit counters. -- F

• Briefly explain why resolving branches in decode is necessary in the MIPS 5-stage pipeline (assuming it does not do branch prediction, and assuming MIPS has one delay slot).
  • The delay slot only covers one of the two instructions that will be fetched between when the branch is fetched and when it is resolved execute. Resolving the branch in decode ensures that only one instruction will be fetched before the branch resolves.

• Give two examples of why branch behavior is often predictable.
  • The branch at the bottom of a loop is usually taken
  • The behavior of two branches can be correlated (e.g., they use the same condition)
  • A branch operand may be a run-time constant.

• If we double the number of pipeline stages in the MIPS 5-stage design by dividing each existing stage in half, what would the new branch delay penalty be (assume branches resolve at the end of decode)?
  • 3 cycles. We have stages F1, F2, D1, D2, E1, E2. Instruction fetch starts in F1. Branches resolve in D2, 3 stages later.

• On a scale of 1-10 (1 being completely unfair and 10 being completely fair), how fair was the midterm?
Quiz 6

- F: 9 students
- D-: 2 students
- D+: 3 students
- C: 4 students
- B-: 7 students
- B+: 5 students
- A: 4 students
Goals for this Class

• Understand how CPUs run programs
  • How do we express the computation the CPU?
  • How does the CPU execute it?
  • How does the CPU support other system components (e.g., the OS)?
  • What techniques and technologies are involved and how do they work?

• Understand why CPU performance (and other metrics) varies
  • How does CPU design impact performance?
  • What trade-offs are involved in designing a CPU?
  • How can we meaningfully measure and compare computer systems?

• Understand why program performance varies
  • How do program characteristics affect performance?
  • How can we improve a program's performance by considering the CPU running it?
  • How do other system components impact program performance?
Memory

Abstraction: Big array of bytes
Main points for today

• What is a memory hierarchy?
• What is the CPU-DRAM gap?
• What is locality? What kinds are there?
• Learn a bunch of caching vocabulary.
Processor vs Memory Performance

- Memory is very slow compared to processors.
Memory’s impact

\[ M = \% \text{ mem ops} \]
\[ \text{Mlat (cycles)} = \text{average memory latency} \]
\[ \text{BCPI} = \text{base CPI with single-cycle data memory} \]

\[ \text{CPI} = \]
Memory’s impact

\( M = \% \text{ mem ops} \)

\( M\text{lat (cycles)} = \text{average memory latency} \)

\( \text{TotalCPI} = \text{BaseCPI} + M \times M\text{lat} \)

Example:

- \( \text{BaseCPI} = 1; \ M = 0.2; \ M\text{lat} = 240 \text{ cycles} \)
- \( \text{TotalCPI} = 49 \)
- \( \text{Speedup} = 1/49 = 0.02 \Rightarrow 98\% \text{ drop in performance} \)

Remember!: Amdahl’s law does not bound the slowdown. Poor memory performance can make your program arbitrarily slow.
Memory Cache

• Memory cost
  • >> capacity -> more $$$
  • >> speed/bw -> more $$$
  • >> speed -> larger (less dense)

• Build several memories with different trade-offs
• How do you use it? Build a “memory hierarchy”
• What should it mean for the memory abstraction?
Memory Cache

- Memory cost
  - \( \gg \) capacity -> more $$
  - \( \gg \) speed/bw -> more $$
  - \( \gg \) speed -> larger (less dense)

- Build several memories with different trade-offs
- How do you use it? Build a “memory hierarchy”
- What should it mean for the memory abstraction?
A typical memory hierarchy

<table>
<thead>
<tr>
<th>Type</th>
<th>Capacity</th>
<th>Cost</th>
<th>Access Time</th>
</tr>
</thead>
<tbody>
<tr>
<td>on-chip cache</td>
<td>KBs</td>
<td>2.5 $/MB</td>
<td>&lt; 1ns</td>
</tr>
<tr>
<td>off-chip cache</td>
<td>MBs</td>
<td>0.07 $/MB</td>
<td>5ns</td>
</tr>
<tr>
<td>main memory</td>
<td>GBs</td>
<td>0.0004 $/MB</td>
<td>60ns</td>
</tr>
<tr>
<td>Disk</td>
<td>TBs</td>
<td>0.0004 $/MB</td>
<td>10,000,000ns</td>
</tr>
</tbody>
</table>
How far away is the data?

- $10^9$ Tape / Optical Robot: 2,000 Years
- $10^6$ Disk: 2 Years
- 100 Memory: 1.5 hr
- 10 On Board Cache: 10 min
- 2 On Chip Cache: 1 min
- 1 Registers: 1 min

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Why should we expect caching to work?

- Why did branch prediction work?
Why should we expect caching to work?

- Why did branch prediction work?
- Where is memory access predictable
  - Predictably accessing the same data
    - In loops: for(i = 0; i < 10; i++) {s += foo[i];}
    - foo = bar[4 + configuration_parameter];
  - Predictably accessing different data
    - In linked lists: while(l != NULL) {l = l->next;}
    - In arrays: for(i = 0; i < 10000; i++) {s += data[i];}
    - structure access: foo(some_struct.a, some_struct.b);
The Principle of Locality

• “Locality” is the tendency of data access to be predictable. There are two kinds:

  • Spatial locality: The program is likely to access data that is close to data it has accessed recently

  • Temporal locality: The program is likely to access the same data repeatedly.
Locality in Action

- Label each access with whether it has temporal or spatial locality or neither
  - 1
  - 2
  - 3
  - 4
  - 10
  - 11
  - 30
  - 1800
  - 190
  - 30
  - 12
  - 13
  - 182
  - 1004
Locality in Action

• Label each access with whether it has temporal or spatial locality or neither
  • 1 n
  • 2 s
  • 3 s
  • 10 n
  • 4 s
  • 1800 n
  • 11 s
  • 30 n

• 1 t
• 2 s, t
• 3 s,t
• 4 s,t
• 10 s,t
• 190 n
• 11 s,t
• 30 s
• 12 s
• 13 s
• 182 n?
• 1004 n
Locality in Action

- Label each access with whether it has temporal or spatial locality or neither
  - 1 n
  - 2 s
  - 3 s
  - 10 n
  - 4 s
  - 1800 n
  - 11 s
  - 30 n
  - 1 t
  - 2 s, t
  - 3 s,t
  - 4 s,t
  - 10 s,t
  - 190 n
  - 11 s,t
  - 30 s
  - 12 s
  - 13 s
  - 182 n?
  - 1004 n

There is no hard and fast rule here. In practice, locality exists for an access if the cache performs well.
Cache Vocabulary

- **Hit** - The data was found in the cache
- **Miss** - The data was not found in the cache
- **Hit rate** - hits/total accesses
- **Miss rate** = 1 - Hit rate
- **Locality** - see previous slides
- **Cache line** - the basic unit of data in a cache. Generally several words.
- **Tag** - the high order address bits stored along with the data to identify the actual address of the cache line.
- **Hit time** -- time to service a hit
- **Miss time** -- time to service a miss (this is a function of the lower level caches.)
Cache Vocabulary

- There can be many caches stacked on top of each other
- If you miss in one you try in the "lower level cache". Lower level, mean higher number.
- There can also be separate caches for data and instructions. Or the cache can be "unified".
- In the 5-stage MIPS pipeline
  - The L1 data cache (d-cache) is the one nearest processor. It corresponds to the "data memory" block in our pipeline diagrams.
  - The L1 instruction cache (i-cache) corresponds to the "instruction memory" block in our pipeline diagrams.
  - The L2 sits underneath the L1s.
  - There is often an L3 in modern systems.
Typical Cache Hierarchy

- Fetch/ 
  L1 
  Icache 
  16KB

- Decode

- EX

- Mem 
  L1 
  Dcache 
  16KB

- Write 
  back

- Unified L2 
  8MB

- Unified L3 
  32MB

- DRAM 
  Many GBs
Data vs Instruction Caches

• Why have different I and D caches?
Data vs Instruction Caches

• Why have different I and D caches?
  • Different areas of memory
  • Different access patterns
    • I-cache accesses have lots of spatial locality. Mostly sequential accesses.
    • I-cache accesses are also predictable to the extent that branches are predictable
    • D-cache accesses are typically less predictable
  • Not just different, but often across purposes.
    • Sequential I-cache accesses may interfere with the data the D-cache has collected.
    • This is “interference” just as we saw with branch predictors
  • At the L1 level it avoids a structural hazard in the pipeline
  • Writes to the I cache by the program are rare enough that they can be slow (i.e., self modifying code)
Midterm Fairness (mean=6.2)

• Biggest complaint: Not enough time
Mid Term Grades

<table>
<thead>
<tr>
<th>Grade</th>
<th># of students</th>
</tr>
</thead>
<tbody>
<tr>
<td>F</td>
<td>0</td>
</tr>
<tr>
<td>F+</td>
<td>10</td>
</tr>
<tr>
<td>D=</td>
<td>15</td>
</tr>
<tr>
<td>D</td>
<td>20</td>
</tr>
<tr>
<td>D+</td>
<td>25</td>
</tr>
<tr>
<td>C-</td>
<td>30</td>
</tr>
<tr>
<td>C</td>
<td>35</td>
</tr>
<tr>
<td>C+</td>
<td>39</td>
</tr>
<tr>
<td>B-</td>
<td>44</td>
</tr>
<tr>
<td>B</td>
<td>47</td>
</tr>
<tr>
<td>B+</td>
<td>52</td>
</tr>
<tr>
<td>A-</td>
<td>56</td>
</tr>
<tr>
<td>A</td>
<td>60</td>
</tr>
<tr>
<td>A+</td>
<td>64</td>
</tr>
</tbody>
</table>
Fairness vs Grade

Graph showing the relationship between fairness and grade.
Midterm Grade Questions

• Math errors -- i.e., we added up your points wrong
  • Come to office hours.

• Other errors
  • *E-mail* us requesting a regrade, and explaining why you think there was an error
    • You must explain why you think there was an error
    • You must send the email.
    • You cannot just show up at office hours.
  • We will regrade your entire exam (i.e., your grade could go down)

• No exceptions.
• We photocopied a random sampling of the exams before turning them back to you.