
First Name:

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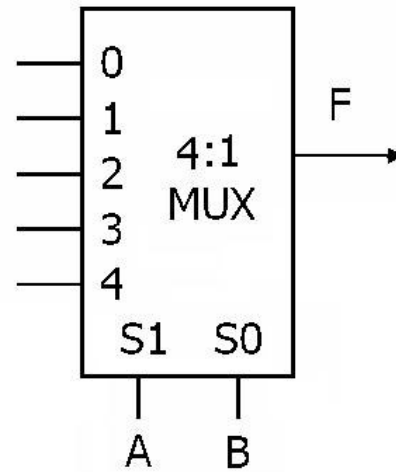
1. **(10 points)**

Implement the function F using a 4:1 multiplexer shown below.

$$F(A,B,C,D) = \sum m(5, 6, 7, 8, 11, 12, 13) + d(2, 15)$$

Use minimum number of gates to implement the function.

You cannot assume that negated values of inputs are available.



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3. (15 points)

A sequential circuit has two inputs w_1 and w_2 , and an output, z . Its function is to compare the input sequences on the two inputs. If $w_1=w_2$ during any four consecutive clock cycles, the circuit produces $z=1$; otherwise, $z=0$.

For example:

W1: 0110111000110

W2: 1110101000111

Z : 0000100001110

Draw the state diagram using at most 5 states.

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4. (20 points)

An FSM is defined by the following state transition table.

Present State $Q_1 Q_0$	Next state		Output Z
	W=0 $Q_1^+ Q_0^+$	W=1 $Q_1^+ Q_0^+$	
00	10	11	0
01	00	00	0
10	10	00	0
11	10	00	1

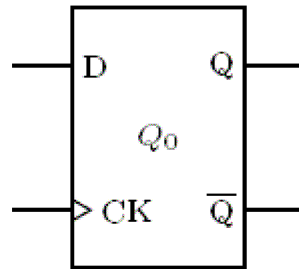
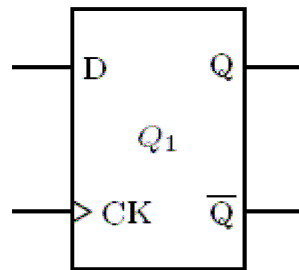
(a) Derive the next state and output equations.

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(b) Provide the logic schematic of this machine using only D flip-flops, AND gates, OR gates, and NOT gates.

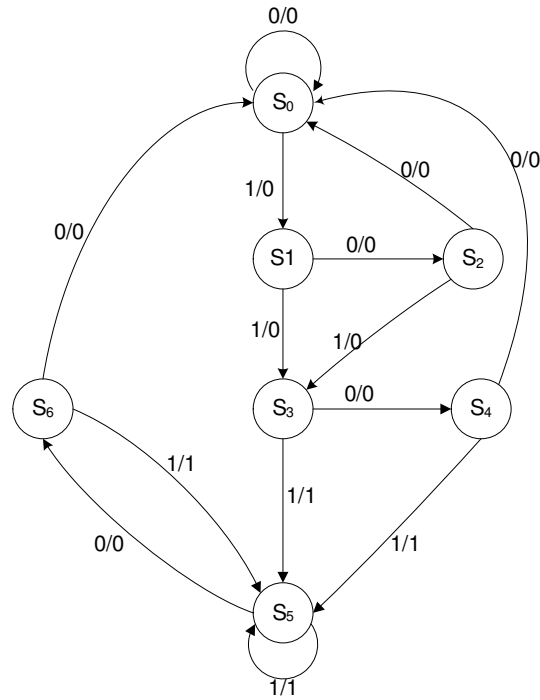


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5. (25 marks) Consider the following state diagram:



(a) Fill out the blanks in the state table

Present State	Next State		Output Y	
	A = 0	A = 1	A = 0	A = 1
S ₀	S ₀	S ₁	0	0
S ₁	S ₂	S ₃	0	0
S ₂	S ₀	S ₃	0	0
S ₃	S ₄	S ₅		
S ₄	S ₀		0	
S ₅				
S ₆		S ₅		1

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(b) Label the rows and columns with states, and then fill the implication table.

S_0

(c) List all the original states, grouped into maximal classes of compatibility. Use only as many groups as necessary.

$g_0 =$ _____

$g_1 =$ _____

$g_2 =$ _____

$g_3 =$ _____

$g_4 =$ _____

$g_5 =$ _____

$g_6 =$ _____

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(d) Show the minimized state transition and output table. Fill in only as many rows of the table as necessary.

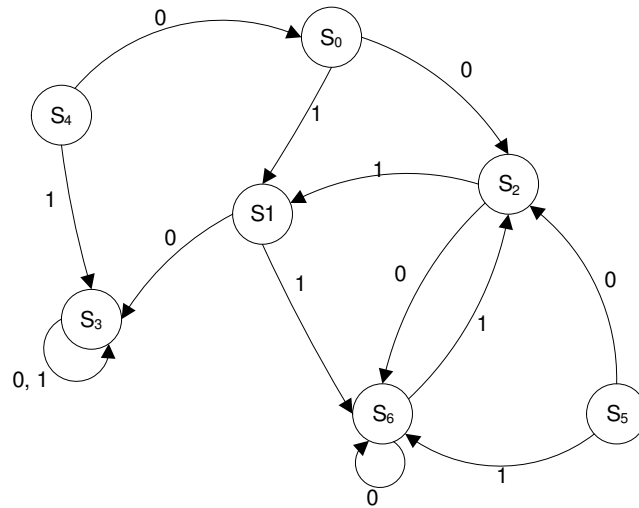
Present State	Next State		Output Y	
	A = 0	A = 1	A = 0	A = 1
g ₀				
g ₁				
g ₂				
g ₃				
g ₄				
g ₅				
g ₆				

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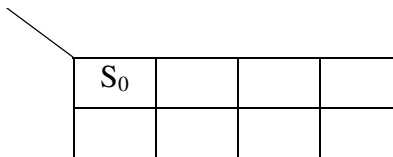
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6. (10 marks) Consider the finite state machine shown below.



Implement a state assignment using the minimum bit-change heuristic. Show your result in both K-map and the table.



State Name	Assignment		
	Q ₂	Q ₁	Q ₀
S ₀			
S ₁			
S ₂			
S ₃			
S ₄			
S ₅			
S ₆			

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