CSE 258 — Lecture 3 Web Mining and Recommender Systems

Classification

Learning outcomes

This week we want to:

- Explore techniques for **classification**
- Try some simple solutions, and see why they might fail
- Explore more complex solutions, and their advantages and disadvantages
- Understand the relationship between classification and regression
- Examine how we can reliably
 evaluate classifiers under different conditions

CSE 258 – Lecture 3 Web Mining and Recommender Systems





Last week we started looking at supervised learning problems

$$f(\text{data}) \xrightarrow{?} \text{labels}$$



We studied **linear regression**, in order to learn linear relationships between features and parameters to predict **realvalued** outputs



Last week...

Pitch Black - Unrated Director's Cut R co



Watch Trailer

***** 777 MDb 7.1/10

When their ship crash-lands on a remote planet, the marconed passengers and learn that escaped convict Riddick (Vin Diesel) isn't the only thing they have to fear. Deadly creation lurk in the shadows, waiting to attack in the dark, and the planet is rapidly plunging into the > See More.

Starring: Vin Diesel, Radha Mitchell Runtime: 1 hour, 53 minutes Available to watch on supported devices

Product Details

Genres	Science Fiction Action Hurst
Director	David Twohy
Starring	Vin Diesel, Radha Mitchell
Supporting actors	Cole Hauser, Keith David, Lewis Fitz-Gerald, Claudia Black, Rhiana Gr Angela Moore, Peter Chiang, Ken Twohy
Studio	NBC Universal
MPAA rating	R (Restricted)
Captions and subtitles	English Details 🔻
Rental rights	24 hour viewing period. Details 💌
Purchase rights	Stream instantly and download to 2 locations Details *
Format	Amazon Instant Video (streaming online video and digital download)

$f(\text{user features}, \text{movie features}) \xrightarrow{?} \text{star rating}$

ratings features

1) Regression can be cast in terms of maximizing a likelihood

 $Y_{i} = X_{i} \cdot O + \mathcal{N}(0, \sigma)$ $Y_{i} = \prod_{i} \sum_{j \in \mathcal{N}} (y_{i} - X_{i} \cdot O)^{2}$ $= \prod_{i} \sum_{j \in \mathcal{N}} (y_{i} - X_{i} \cdot O)^{2}$

2) Gradient descent for model optimization

1. Initialize θ at random 2. While (not converged) do $\theta := \theta - \alpha f'(\theta)$

3) Regularization & Occam's razor

Regularization is the process of penalizing model complexity during training

$$\arg\min_{\theta} = \frac{1}{N} \|y - X\theta\|_2^2 + \lambda \|\theta\|_2^2$$

How much should we trade-off accuracy versus complexity?

4) Regularization pipeline

- 1. Training set select model parameters
- 2. Validation set to choose amongst models (i.e., hyperparameters)
- 3. Test set just for testing!

Valid Jest choose & J choose & J choose & J g choose & choose nodels generalization performence

A **validation set** is constructed to "tune" the model's parameters

- Training set: used to optimize the model's parameters
- Test set: used to report how well we expect the model to perform on **unseen data**
- Validation set: used to **tune** any model parameters that are not directly optimized

A few "theorems" about training, validation, and test sets

- The training error **increases** as lambda **increases**
- The validation and test error are at least as large as the training error (assuming infinitely large random partitions)
- The validation/test error will usually have a "sweet spot" between under- and over-fitting



How can we predict **binary** or **categorical** variables?

 $f(\text{data}) \xrightarrow{?} \text{labels} \{1, \dots, N\}$

Today...



Will I **purchase** this product? (yes)



Will I **click on** this ad? (no)



What animal appears in this image? (mandarin duck)



Today...

What are the **categories** of the item being described?

(book, fiction, philosophical fiction)

From Booklist

Houellebecq's deeply philosophical novel is about an alienated young man searching for happiness in the computer age. Bored with the world and too weary to try to adapt to the foibles of friends and coworkers, he retreats into himself, descending into depression while attempting to analyze the passions of the people around him. Houellebecq uses his nameless narrator as a vehicle for extended exploration into the meanings and manifestations of love and desire in human interactions. Ironically, as the narrator attempts to define love in increasingly abstract terms, he becomes less and less capable of experiencing that which he is so desperate to understand. Intelligent and well written, the short novel is a thought-provoking inspection of a generation's confusion about all things sexual. Houellebecq captures precisely the cynical disillusionment of disaffected youth. Bonnie Johnston --This text refers to an out of print or unavailable edition of this title.



We'll attempt to build **classifiers** that make decisions according to rules of the form

$$y_i = \begin{cases} 1 & \text{if } X_i \cdot \theta > 0 \\ 0 & \text{otherwise} \end{cases}$$



Assumes an **independence** relationship between the features and the class label and "learns" a simple model by counting

2. Logistic regression

Adapts the **regression** approaches we saw last week to binary problems

3. Support Vector Machines

Learns to classify items by finding a hyperplane that separates them



Ranking results in order of how likely they are to be relevant

tea station									
tou st	auon								
Web	Maps	Shopping	Images	News	More 👻	Search tools			
About 20,900,000 results (0.61 seconds)									
Tea Station 加州茶棧 teastationusa.com/ マ 12 Tea Station locations in California and Nevada making Tea Station the We'd like to take this moment to thank you all tea lovers for your continued support. 3.8 ★★★★★ 19 Google reviews · Write a review · Google+ page									
 7315 Clairemont Mesa Boulevard, San Diego, CA 92111 (858) 268-8198 Menu - About - Ten Ren Products - San Gabriel 									
Tea Station - Kearny Mesa - San Diego, CA Yelp									

www.velp.com > Restaurants > Chinese - Yelp -



Evaluating classifiers

- False positives are nuisances but false negatives are disastrous (or vice versa)
 - Some classes are very rare
 - When we only care about the "most confident" predictions



e.g. which of these bags contains a weapon?



We want to associate a probability with a label and its negation:

p(label|data) $p(\neg label|data)$

(classify according to whichever probability is greater than 0.5)

Q: How far can we get just by counting?

e.g. p(movie is "action" | schwarzenneger in cast)



Just count! #fims with Arnold = 45 #**action** films with Arnold = 32^{7} p(movie is "action" | schwarzenneger in cast) = 32/45

What about: p(movie is "action" | schwarzenneger in cast and release year = 2017 and mpaa rating = PG and budget < \$1000000)

#(training) fims with Arnold, released in 2017, rated PG, with a budged below \$1M = 0 #(training) action fims with Arnold, released in 2017, rated PG, with a budged below \$1M = 0

Q: If we've never seen this combination of features before, what can we conclude about their probability?

A: We need some **simplifying assumption** in order to associate a probability with this feature combination



Naïve Bayes assumes that features are conditionally independent given the label

 $(feature_i \perp\!\!\!\perp feature_j | label)$

 $(feature_i \perp feature_i | label)$ $\begin{array}{c} \alpha \coprod b \Rightarrow p(a,b) = p(a) p(b) \\ \alpha \coprod b < \Rightarrow p(a,b|c) = p(a|c) p(b|c) \end{array}$

C = 1'm vea-ily shorts b = you're vea-ily shorts c = it's summer

Conditional independence?

 $(a \perp\!\!\!\perp b|c)$ (a is conditionally independent of b, given c)

"if you know **c**, then knowing **a** provides no additional information about **b**"

(I remembered my umbrella \perp the streets are wet | it's raining)

$\begin{array}{c} (feature_i \perp feature_j | label) \\ \downarrow \\ p(feature_i, feature_j | label) \\ = \\ p(feature_i | label) p(feature_j | label) \end{array}$

posterior likelihood prior p(label|features)= ? (labe !) p(features | 26e) P(Perstures) p(a|b) = p(a)p(L|a)evidence T. P(label) TTp(feature; ||abel) p(-Peartires)

$$p(label|features) = \frac{p(label)\prod_{i}p(feature_{i}|label)}{p(features)}$$

$$p(\gamma|ale||features) = p(\gamma|s6e|)\prod_{i}p(feat_{i}||s6e|)$$

$$p(features)$$

The denominator doesn't matter, because we really just care about

$$p(label|features)$$
 vs. $p(\neg label|features)$

both of which have the same denominator

$$P(y) T(f(y)) > P(\gamma) T(f(y)) > P(\gamma) T(f(y)) > P(\gamma) T(f(y)) ?$$

The denominator doesn't matter, because we really just care about

$$p(label|features)$$
 vs. $p(\neg label|features)$

both of which have the same denominator

Example 1

Amazon editorial descriptions:

Amazon.com Review

For most children, summer vacation is something to look forward to. But not for our 13-year-oluncle, and cousin who detest him. The third book in J.K. Rowling's <u>Harry Potter series</u> catapults Dursleys' dreadful visitor Aunt Marge to inflate like a monstrous balloon and drift up to the ceili (and from officials at Hogwarts School of Witchcraft and Wizardry who strictly forbid students to out into the darkness with his heavy trunk and his owl Hedwig.

As it turns out, Harry isn't punished at all for his errant wizardry. Instead he is mysteriously restriple-decker, violently purple bus to spend the remaining weeks of summer in a friendly inn ca his third year at Hogwarts explains why the officials let him off easily. It seems that Sirius Blac loose. Not only that, but he's after Harry Potter. But why? And why do the Dementors, the guar are unaffected? Once again, Rowling has created a mystery that will have children and adults cl Fortunately, there are four more in the works. (Ages 9 and older) --Karin Snelson --This text re

50k descriptions:

http://jmcauley.ucsd.edu/cse258/data/amazon/book_descriptions_50000.json



P(book is a children's book | "wizard" is mentioned in the description **and** "witch" is mentioned in the description)

Code available on:

http://jmcauley.ucsd.edu/cse258/code/week2.py

Example 1

Conditional independence assumption:

"if you know a book is for children, then knowing that wizards are mentioned provides no additional information about whether witches are mentioned"

obviously ridiculous

Q: What would happen if we trained two regressors, and attempted to "naively" combine their parameters?

Double-counting

$$H = 1.2U + 1555.$$

Double-counting

A: Since both features encode essentially the same information, we'll end up double-counting their effect

Logistic Regression also aims to model

p(label|data)

By training a classifier of the form

 $y_i = \begin{cases} 1 & \text{if } X_i \cdot \theta > 0 \\ 0 & \text{otherwise} \end{cases}$

Last week: regression

$$y_i = X_i \cdot \theta$$

This week: logistic regression

$$y_i = \begin{cases} 1 & \text{if } X_i \cdot \theta > 0 \\ 0 & \text{otherwise} \end{cases}$$

Q: How to convert a realvalued expression $(X_i \cdot \theta \in \mathbb{R})$ Into a probability $(p_{\theta}(y_i|X_i) \in [0,1])$



Training:

$X_i \cdot \theta$ should be maximized when y_i is positive and minimized when y_i is negative

 $\begin{array}{c} TT \quad \mathcal{P}_{0}\left(y_{i} \middle| X_{i}\right) \quad \chi \quad TT \left(1 - \mathcal{P}_{0}\left(y_{i} \middle| X_{i}\right)\right) \\ y_{i=1} \quad \mathcal{O}\left(X_{i}^{*} \circ\right) \quad \chi \quad TT \left(1 - \mathcal{O}\left(X_{i}^{*} \circ\right)\right) \\ y_{i=1} \quad \mathcal{O}\left(X_{i}^{*} \circ\right) \quad \chi \quad TT \left(1 - \mathcal{O}\left(X_{i}^{*} \circ\right)\right) \\ y_{i=1} \quad \mathcal{O}\left(X_{i}^{*} \circ\right) \quad \chi \quad TT \left(1 - \mathcal{O}\left(X_{i}^{*} \circ\right)\right) \\ y_{i=1} \quad \mathcal{O}\left(X_{i}^{*} \circ\right) \quad \chi \quad TT \left(1 - \mathcal{O}\left(X_{i}^{*} \circ\right)\right) \\ y_{i=1} \quad \mathcal{O}\left(X_{i}^{*} \circ\right) \quad \chi \quad TT \left(1 - \mathcal{O}\left(X_{i}^{*} \circ\right)\right) \\ y_{i=1} \quad \mathcal{O}\left(X_{i}^{*} \circ\right) \quad \chi \quad TT \left(1 - \mathcal{O}\left(X_{i}^{*} \circ\right)\right) \\ y_{i=1} \quad \mathcal{O}\left(X_{i}^{*} \circ\right) \quad \chi \quad TT \left(1 - \mathcal{O}\left(X_{i}^{*} \circ\right)\right) \\ y_{i=1} \quad \mathcal{O}\left(X_{i}^{*} \circ\right) \quad \chi \quad TT \left(1 - \mathcal{O}\left(X_{i}^{*} \circ\right)\right) \\ y_{i=1} \quad \mathcal{O}\left(X_{i}^{*} \circ\right) \quad \chi \quad TT \left(1 - \mathcal{O}\left(X_{i}^{*} \circ\right)\right) \\ y_{i=1} \quad \mathcal{O}\left(X_{i}^{*} \circ\right) \quad \chi \quad TT \left(1 - \mathcal{O}\left(X_{i}^{*} \circ\right)\right) \\ y_{i=1} \quad \mathcal{O}\left(X_{i}^{*} \circ\right) \quad \chi \quad TT \left(1 - \mathcal{O}\left(X_{i}^{*} \circ\right)\right) \\ y_{i=1} \quad \mathcal{O}\left(X_{i}^{*} \circ\right) \quad \chi \quad TT \left(1 - \mathcal{O}\left(X_{i}^{*} \circ\right)\right) \\ y_{i=1} \quad \mathcal{O}\left(X_{i}^{*} \circ\right) \quad \chi \quad TT \left(1 - \mathcal{O}\left(X_{i}^{*} \circ\right)\right) \\ y_{i=1} \quad \mathcal{O}\left(X_{i}^{*} \circ\right) \quad \chi \quad TT \left(1 - \mathcal{O}\left(X_{i}^{*} \circ\right)\right) \\ y_{i=1} \quad \mathcal{O}\left(X_{i}^{*} \circ\right) \quad \chi \quad TT \left(1 - \mathcal{O}\left(X_{i}^{*} \circ\right)\right) \\ y_{i=1} \quad \mathcal{O}\left(X_{i}^{*} \circ\right) \quad \chi \quad TT \left(1 - \mathcal{O}\left(X_{i}^{*} \circ\right)\right) \\ y_{i=1} \quad \mathcal{O}\left(X_{i}^{*} \circ\right) \quad \chi \quad TT \left(1 - \mathcal{O}\left(X_{i}^{*} \circ\right)\right) \\ y_{i=1} \quad \mathcal{O}\left(X_{i}^{*} \circ\right) \quad \chi \quad TT \left(1 - \mathcal{O}\left(X_{i}^{*} \circ\right)\right) \\ y_{i=1} \quad \mathcal{O}\left(X_{i}^{*} \circ\right) \quad \chi \quad TT \left(1 - \mathcal{O}\left(X_{i}^{*} \circ\right)\right) \\ y_{i=1} \quad \mathcal{O}\left(X_{i}^{*} \circ\right) \quad \chi \quad TT \left(1 - \mathcal{O}\left(X_{i}^{*} \circ\right)\right)$ $\operatorname{arg} \max_{\theta}$

How to optimize?

 $L_{\theta}(y|X) = \prod_{y_i=1} p_{\theta}(y_i|X_i) \prod_{y_i=0} (1 - p_{\theta}(y_i|X_i))$

- Take logarithm
- Subtract regularizer
 - Compute gradient
- Solve using gradient **ascent**

 $L_{\theta}(y|X) = \prod_{y_i=1} p_{\theta}(y_i|X_i) \prod_{y_i=0} (1 - p_{\theta}(y_i|X_i))$ $\begin{array}{c} \mathcal{L}_{\Theta}(\mathcal{Y}|X) - \mathcal{E}log \quad \sigma(X:\mathcal{O}) + \mathcal{E}log \left(\left| -\sigma(X;\mathcal{O}) \right| \right) \\ \mathcal{Y}_{i} = l \quad \mathcal{Y}_{i} = l \end{array}$ $= \underbrace{\sum_{j=1}^{y_{i=1}} g\left(\frac{1}{1+e^{-X_{i}\cdot o}}\right)}_{y_{i=1}} + \underbrace{\sum_{j=1}^{y_{i=0}} \log\left(\frac{e^{-X_{i}\cdot o}}{1+e^{-X_{i}\cdot o}}\right)}_{y_{i=1}}$ 9:50 $= \frac{\sum_{i=0}^{n} \log(1+e^{-\chi_{i}^{*}} \circ \theta)}{y_{i=0}} + \frac{\sum_{i=0}^{n} \chi_{i}^{*} \circ \theta}{y_{i=0}}$



Log-likelihood:

$$l_{\theta}(y|X) = \sum_{i} -\log(1 + e^{-X_{i} \cdot \theta}) + \sum_{y_{i}=0} -X_{i} \cdot \theta - \lambda \|\theta\|_{2}^{2}$$

Derivative:

 $\frac{\partial l}{\partial \theta_k} = \sum_i X_{ik} (1 - \sigma (X_i \cdot \theta)) + \sum_{y_i=0} -X_{ik} - 2\lambda \theta_k$

Multiclass classification

The most common way to generalize **binary** classification (output in {0,1}) to **multiclass** classification (output in {1 ... N}) is simply to train a binary predictor for each class

e.g. based on the description of this book:

- Is it a Children's book? {yes, no}
- Is it a Romance? {yes, no}
- Is it Science Fiction? {yes, no}

• .

In the event that predictions are inconsistent, choose the one with the highest confidence

Questions?

Further reading:

- On Discriminative vs. Generative classifiers: A comparison of logistic regression and naïve Bayes (Ng & Jordan '01)
 - Boyd-Fletcher-Goldfarb-Shanno algorithm (BFGS)

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Supervised Learning - Support Vector Machines

So far we've looked at **logistic regression**, which is a classification model of the form:

$$y_i = \begin{cases} 1 & \text{if } X_i \cdot \theta > 0\\ 0 & \text{otherwise} \end{cases}$$

- In order to do so, we made certain modeling assumptions, but there are many different models that rely on different assumptions
- In this lecture we'll look at another such model

Motivation: SVMs vs Logistic regression

Q: Where would a logistic regressor place the decision boundary for these features?



SVMs vs Logistic regression

Q: Where would a logistic regressor place the decision boundary for these features?



SVMs vs Logistic regression

- Logistic regressors don't optimize the number of "mistakes"
- No special attention is paid to the "difficult" instances – every instance influences the model
- But "easy" instances can affect the model (and in a bad way!)
- How can we develop a classifier that optimizes the number of mislabeled examples?

Support Vector Machines: Basic idea

A classifier can be defined by the hyperplane (line) $\theta \mathbf{x} - \alpha = 0$



Support Vector Machines: Basic idea

Observation: Not all classifiers are equally good





 An SVM seeks the classifier (in this case a line) that is furthest from the nearest points

 This can be written in terms of a specific optimization problem:

> $\arg\min_{\theta,\alpha} \frac{1}{2} \|\theta\|_2^2$ such that $\forall_i y_i (\theta \cdot X_i - \alpha) \ge 1$

[&]quot;support vectors"

But: is finding such a separating hyperplane even possible?



Or: is it actually a good idea?





Want the margin to be as wide as possible



While penalizing points on the wrong side of it

Soft-margin formulation:

$$\arg\min_{\theta,\alpha,\xi>0} \frac{1}{2} \|\theta\|_2^2 + C\sum_i \xi_i$$

such that

$$\forall_i y_i (\theta \cdot X_i - \alpha) \ge 1 - \xi_i$$

Summary of Support Vector Machines

- SVMs seek to find a hyperplane (in two dimensions, a line) that optimally separates two classes of points
- The "best" classifier is the one that classifies all points correctly, such that the nearest points are as far as possible from the boundary
 - If not all points can be correctly classified, a penalty is incurred that is proportional to how badly the points are misclassified (i.e., their distance from this hyperplane)

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Supervised Learning - Code example

Judging a book by its cover



[0.723845, 0.153926, 0.757238, 0.983643, ...]

4096-dimensional image features

Images features are available for each book on

http://jmcauley.ucsd.edu/cse258/data/amazon/book_images_5000.json



http://caffe.berkeleyvision.org/

Judging a book by its cover

Example: train a classifier to predict whether a book is a children's book from its cover art

(code available on) http://jmcauley.ucsd.edu/code/week2.py

Judging a book by its cover

 The number of errors we made was extremely low, yet our classifier doesn't seem to be very good – why?
 (stay tuned next lecture!)

Summary

The classifiers we've seen today all attempt to make decisions by associating weights (theta) with features (x) and classifying according to

$$y_i = \begin{cases} 1 & \text{if } X_i \cdot \theta > 0\\ 0 & \text{otherwise} \end{cases}$$

Summary

Naïve Bayes

- Probabilistic model (fits p(label|data))
- Makes a conditional independence assumption of the form $(feature_i \perp feature_j | label)$ allowing us to define the model by computing $p(feature_i | label)$ for each feature
- Simple to compute just by counting

Logistic Regression

 Fixes the "double counting" problem present in naïve Bayes

• SVMs

• Non-probabilistic: optimizes the classification error rather than the likelihood

Questions?